

File S1 $m_w(z)$, $m_B(z)$, W_A , W_P , W_B , Q_{hA} , Q_{vA} , $Q_{hA}(t)$, $Q_{vA}(t)$, Q_{hP} , Q_{vP} , $Q_{hP}(t)$, $Q_{vP}(t)$, Q_{hB} , Q_{vB} , $Q_{hB}(t)$, $Q_{vB}(t)$, C_A , C_P , C_B , C_{AP} , C_{PB} , for the four cases ($m_w(z)$ can be divided into $m_A(z)$ and $m_P(z)$)

Case 1: $H \cot \beta < H_T \cot \xi$

$$H_{P11} = H_T - H \cot \beta \tan \xi, \quad H_{A2} = H \cot \beta \tan \xi, \quad H_{A1} = H + H_{A2}, \quad H_{P4} = H + H_T,$$

$$H_{B1} = H_B \cot \alpha \tan \eta, \quad H_{B2} = H_B (1 + \cot \alpha \tan \eta),$$

$$H_{P3} = [H_{A1} - H_{B2} + (B_T - H \cot \beta + H_T \cot \xi) \tan \eta] / (\cot \theta \tan \eta - 1), \quad H_A = H_{A1} + H_{P3},$$

$$H_{P2} = H_{B2} - H_{P3}, \quad H_{P1} = H_{P4} - H_{P2}, \quad H_P = H_{P4} + H_{P3};$$

$$C_P = c_P H_{P3} / \sin \theta, \quad C_{AP} = c H_{A1}, \quad C_{PB} = c H_{B2};$$

$$m_{A1}(z) = \rho z \cot \xi \quad (0 \leq z < H_{A2}), \quad m_{A2}(z) = \rho (H_{A1} - z) \cot \beta \quad (H_{A2} \leq z \leq H_{A1});$$

$$W_A = W_{A1} + W_{A2}, \quad W_{A1} = 0.5 \gamma H H_{A2} \cot \beta, \quad W_{A2} = 0.5 \gamma H^2 \cot \beta; \quad Q_{hA} = k_h W_A;$$

$$Q_{hA}(t) = Q_{hA1} + Q_{hA2},$$

$$Q_{hA1} / k_h \gamma = (f_a \cot \xi) (-TV_s / 2\pi) \{H_{A2} \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_A - H_{A2}) / TV_s) - \sin 2\pi(t / T - H_A / TV_s)]\} + [(1 - f_a) \cot \xi / H_A] (-TV_s / 2\pi) \{H_{A2}^2 \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - (TV_s / \pi) [H_{A2} \sin 2\pi(t / T - (H_A - H_{A2}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - \cos 2\pi(t / T - H_A / TV_s))]\},$$

$$Q_{hA2} / k_h \gamma = (f_a H_{A1} \cot \beta) (-TV_s / 2\pi) [\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s)] + [(1 - f_a) H_{A1} \cot \beta / H_A - f_a \cot \beta] (-TV_s / 2\pi) \{H_{A1} \cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - H_{A2} \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \sin 2\pi(t / T - (H_A - H_{A2}) / TV_s)]\} + [(f_a - 1) \cot \beta / H_A] (-TV_s / 2\pi) \{H_{A1}^2 \cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - H_{A2}^2 \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - (TV_s / \pi) [H_{A1} \sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) - H_{A2} \sin 2\pi(t / T - (H_A - H_{A2}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s))]\},$$

$$m_{P1}(z) = \rho [B_T + z(\cot \eta + \cot \xi)] \quad (0 \leq z < H_{P11}),$$

$$m_{P2}(z) = \rho (B_T + H_{P11} \cot \xi + z \cot \eta) \quad (H_{P11} \leq z < H_{P1}),$$

$$m_{P3}(z) = \rho H_{P3} \cot \theta \quad (H_{P1} \leq z < H_{P4}), \quad m_{P4}(z) = \rho (H_P - z) \cot \theta \quad (H_{P4} \leq z \leq H_P);$$

$$W_P = W_{P1} + W_{P2} + W_{P3} + W_{P4}, \quad W_{P1} = \gamma [H_{P11} B_T + 0.5 H_{P11}^2 (\cot \eta + \cot \xi)],$$

$$W_{P2} = \gamma (H_{P1} - H_{P11}) [B_T + H_{P11} \cot \xi + 0.5 (H_{P1} - H_{P11}) \cot \eta], \quad W_{P3} = \gamma H_{P2} H_{P3} \cot \theta,$$

$$W_{p4} = 0.5\gamma H_{p3}^2 \cot\theta; \quad Q_{hp} = k_h W_p; \quad Q_{hp}(t) = Q_{hp1} + Q_{hp2} + Q_{hp3},$$

$$\begin{aligned} Q_{hp1} / k_h \gamma = & (f_a B_T)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_p - H_{p11}) / TV_s) - \cos 2\pi(t / T - H_p / TV_s)] + [f_a (\cot\eta + \cot\xi) \\ & + (1 - f_a) B_T / H_p](-TV_s / 2\pi)\{H_{p11} \cos 2\pi(t / T - (H_p - H_{p11}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_p - H_{p11}) \\ & / TV_s) - \sin 2\pi(t / T - H_p / TV_s)]\} + [(1 - f_a)(\cot\eta + \cot\xi) / H_p](-TV_s / 2\pi)\{H_{p11}^2 \cos 2\pi(t / T - (H_p - H_{p11}) \\ & / TV_s) - (TV_s / \pi)[H_{p11} \sin 2\pi(t / T - (H_p - H_{p11}) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_p - H_{p11}) / TV_s) - \cos 2\pi \\ & \cdot (t / T - H_p / TV_s))]\}, \end{aligned}$$

$$\begin{aligned} Q_{hp2} / k_h \gamma = & f_a (B_T + H_{p11} \cot\xi)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \cos 2\pi(t / T - (H_p - H_{p11}) / TV_s)] \\ & + [f_a \cot\eta + (1 - f_a)(B_T + H_{p11} \cot\xi) / H_p](-TV_s / 2\pi)\{H_{p1} \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - H_{p11} \cos 2\pi(t / T - (H_p \\ & - H_{p11}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \sin 2\pi(t / T - (H_p - H_{p11}) / TV_s)]\} + [(1 - f_a) \cot\eta / H_p] \\ & (-TV_s / 2\pi)\{H_{p1}^2 \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - H_{p11}^2 \cos 2\pi(t / T - (H_p - H_{p11}) / TV_s) - (TV_s / \pi)[H_{p1} \sin 2\pi(t / T \\ & - (H_p - H_{p1}) / TV_s) - H_{p11} \sin 2\pi(t / T - (H_p - H_{p11}) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \cos 2\pi(t / T \\ & - (H_p - H_{p11}) / TV_s))]\}, \end{aligned}$$

$$\begin{aligned} Q_{hp3} / k_h \gamma = & (f_a H_{p3} \cot\theta)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s)] \\ & + [(1 - f_a)(H_{p3} \cot\theta) / H_p](-TV_s / 2\pi)\{H_{p4} \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - H_{p1} \cos 2\pi(t / T - (H_p - H_{p1}) / \\ & TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \sin 2\pi(t / T - (H_p - H_{p1}) / TV_s)]\}, \end{aligned}$$

$$\begin{aligned} Q_{hp4} / k_h \gamma = & (f_a H_p \cot\theta)(-TV_s / 2\pi)[\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s)] + [(1 - f_a)(H_p \cot\theta) / H_p \\ & - f_a \cot\theta](-TV_s / 2\pi)\{H_p \cos 2\pi(t / T) - H_{p4} \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T) - \sin 2\pi \\ & (t / T - (H_p - H_{p4}) / TV_s)]\} + [(f_a - 1) \cot\theta / H_p](-TV_s / 2\pi)\{H_p^2 \cos 2\pi(t / T) - H_{p4}^2 \cos 2\pi(t / T - (H_p - H_{p4}) \\ & / TV_s) - (TV_s / \pi)[H_p \sin 2\pi(t / T) - H_{p4} \sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T) - \cos 2\pi(t / T \\ & - (H_p - H_{p4}) / TV_s))]\}. \end{aligned}$$

Case 2: $H_T \cot\xi \leq H \cot\beta < B_T + H_T \cot\xi$

$$H_{A1} = H + H_T, \quad H_{p4} = H_{A1}, \quad H_{B1} = H_B \cot\alpha \tan\eta, \quad H_{B2} = H_B (1 + \cot\alpha \tan\eta),$$

$$H_{p3} = [H_{A1} - H_{B2} + (B_T - H \cot\beta + H_T \cot\xi) \tan\eta] / (\cot\theta \tan\eta - 1), \quad H_A = H_{A1} + H_{p3},$$

$$H_{p2} = H_{B2} - H_{p3}, \quad H_{p1} = H_{p4} - H_{p2}, \quad H_p = H_{p4} + H_{p3};$$

$$C_p = c_p H_{p3} / \sin\theta, \quad C_{AP} = c H_{p4}, \quad C_{PB} = c H_{B2};$$

$$m_{A1}(z) = \rho(H \cot\beta - H_T \cot\xi + z \cot\xi) \quad (0 \leq z < H_T), \quad m_{A2}(z) = \rho(H_{A1} - z) \cot\beta \quad (H_T \leq z \leq H_{A1});$$

$$W_A = W_{A1} + W_{A2}, \quad W_{A1} = \gamma H_T (H \cot\beta - 0.5 H_T \cot\xi), \quad W_{A2} = 0.5 \gamma H^2 \cot\beta; \quad Q_{hA} = k_h W_A;$$

$$Q_{hA}(t) = Q_{hA1} + Q_{hA2},$$

$$\begin{aligned} Q_{hA1} / k_h \gamma = & f_a (H \cot\beta - H_T \cot\xi)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_A - H_T) / TV_s) - \cos 2\pi(t / T - H_A / TV_s)] + [f_a \cot\xi \\ & + (1 - f_a)(H \cot\beta - H_T \cot\xi) / H_A](-TV_s / 2\pi)\{H_T \cos 2\pi(t / T - (H_A - H_T) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_A \\ & - H_T) / TV_s) - \sin 2\pi(t / T - H_A / TV_s)]\} + [(1 - f_a) \cot\xi / H_A](-TV_s / 2\pi)\{H_T^2 \cos 2\pi(t / T - (H_A - H_T) / TV_s) - (TV_s \\ & / \pi)[H_T \sin 2\pi(t / T - (H_A - H_T) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_A - H_T) / TV_s) - \cos 2\pi(t / T - H_A / TV_s))]\}, \end{aligned}$$

$$Q_{hA2} / k_h \gamma = (f_a H_{A1} \cot \beta)(-TV_s / 2\pi) [\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \cos 2\pi(t / T - (H_A - H_T) / TV_s)] \\ + [(1 - f_a) H_{A1} \cot \beta H_A - f_a \cot \beta] (-TV_s / 2\pi) \{H_{A1} \cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - H_T \cos 2\pi(t / T - (H_A - H_T) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \sin 2\pi(t / T - (H_A - H_T) / TV_s)]\} + [(f_a - 1) \cdot \cot \beta / H_A] (-TV_s / 2\pi) \{H_{A1}^2 \cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - H_T^2 \cos 2\pi(t / T - (H_A - H_T) / TV_s) - (TV_s / \pi) [H_{A1} \sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) - H_T \sin 2\pi(t / T - (H_A - H_T) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \cos 2\pi(t / T - (H_A - H_T) / TV_s))]\},$$

$$m_{p1}(z) = \rho(B_T - H \cot \beta + H_T \cot \xi + z \cot \eta) \quad (0 \leq z < H_{p1}), \quad m_{p2}(z) = \rho H_{p3} \cot \theta \quad (H_{p1} \leq z < H_{p4}),$$

$$m_{p3}(z) = \rho(H_p - z) \cot \theta \quad (H_{p4} \leq z \leq H_p);$$

$$W_P = W_{p1} + W_{p2} + W_{p3}, \quad W_{p1} = \gamma[H_{p1}(B_T - H \cot \beta + H_T \cot \xi) + 0.5H_{p1}^2 \cot \eta], \quad W_{p2} = \gamma H_{p2} H_{p3} \cot \theta,$$

$$W_{p3} = 0.5\gamma H_{p3}^2 \cot \theta; \quad Q_{hp} = k_h W_P; \quad Q_{hp}(t) = Q_{hp1} + Q_{hp2} + Q_{hp3},$$

$$Q_{hp1} / k_h \gamma = f_a (B_T - H \cot \beta + H_T \cot \xi)(-TV_s / 2\pi) [\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \cos 2\pi(t / T - H_p / TV_s)] + [f_a \cot \eta + (1 - f_a)(B_T - H \cot \beta + H_T \cot \xi) / H_p] (-TV_s / 2\pi) \{H_{p1} \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \sin 2\pi(t / T - H_p / TV_s)]\} + [(1 - f_a) \cot \eta / H_p] (-TV_s / 2\pi) \{H_{p1}^2 \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / \pi) [H_{p1} \sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \cos 2\pi(t / T - H_p / TV_s))]\},$$

$$Q_{hp2} / k_h \gamma = (f_a H_{p3} \cot \theta)(-TV_s / 2\pi) [\cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s)] + [(1 - f_a)(H_{p3} \cot \theta) / H_p] (-TV_s / 2\pi) \{H_{p4} \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - H_{p1} \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \sin 2\pi(t / T - (H_p - H_{p1}) / TV_s)]\},$$

$$Q_{hp3} / k_h \gamma = (f_a H_p \cot \theta)(-TV_s / 2\pi) [\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s)] + [(1 - f_a)(H_p \cot \theta) / H_p - f_a \cot \theta] (-TV_s / 2\pi) \{H_p \cos 2\pi(t / T) - H_{p4} \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T) - \sin 2\pi(t / T - (H_p - H_{p4}) / TV_s)]\} + [(f_a - 1) \cot \theta / H_p] (-TV_s / 2\pi) \{H_p^2 \cos 2\pi(t / T) - H_{p4}^2 \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - (TV_s / \pi) [H_p \sin 2\pi(t / T) - H_{p4} \sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s))]\}.$$

$$\textbf{Case 3: } B_T + H_T \cot \xi \leq H \cot \beta \leq H_T (\cot \xi + \cot \eta)$$

$$H_{A1} = (H \cot \beta - H_T \cot \xi - B_T) \tan \eta, \quad H_{A3} = H_T + H, \quad H_{A2} = H_T - H_{A1}, \quad H_{p4} = H_{A2} + H,$$

$$H_{B1} = H_B \cot \alpha \tan \eta, \quad H_{B2} = H_B (1 + \cot \alpha \tan \eta), \quad H_{p3} = (H_{p4} - H_{B2}) / (\cot \theta \tan \eta - 1),$$

$$H_A = H_{A3} + H_{p3}, \quad H_{p2} = H_{B2} - H_{p3}, \quad H_{p1} = H_{p4} - H_{p2}, \quad H_p = H_{p4} + H_{p3};$$

$$C_p = c_p H_{p3} / \sin \theta, \quad C_{AP} = c H_{p4}, \quad C_{PB} = c H_{B2};$$

$$m_{A1}(z) = \rho[B_T + z(\cot \eta + \cot \xi)] \quad (0 \leq z < H_{A1}),$$

$$m_{A2}(z) = \rho(B_T + H_{A1} \cot \eta + z \cot \xi) \quad (H_{A1} \leq z < H_T), \quad m_{A3}(z) = \rho(H_{A3} - z) \cot \beta \quad (H_T \leq z \leq H_{A3});$$

$$W_A = W_{A1} + W_{A2} + W_{A3}, \quad W_{A1} = \gamma[B_T H_{A1} + 0.5H_{A1}^2 (\cot \eta + \cot \xi)],$$

$$W_{A2} = 0.5\gamma H_{A2}[2B_T + H_{A1}(2\cot\eta + \cot\xi) + H_T\cot\xi], \quad W_{A3} = 0.5\gamma H^2\cot\beta; \quad Q_{hA} = k_h W_A;$$

$$Q_{hA}(t) = Q_{hA1} + Q_{hA2} + Q_{hA3},$$

$$Q_{hA1} / k_h \gamma = (f_a B_T)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \cos 2\pi(t / T - H_A / TV_s)] + [f_a(\cot\eta + \cot\xi) + (1 - f_a)B_T / H_A](-TV_s / 2\pi)\{H_{A1}\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \sin 2\pi(t / T - H_A / TV_s)]\} + [(1 - f_a)(\cot\eta + \cot\xi) / H_A](-TV_s / 2\pi)\{H_{A1}^2\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - (TV_s / \pi)[H_{A1}\sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - \cos 2\pi(t / T - H_A / TV_s))]\},$$

$$Q_{hA2} / k_h \gamma = f_a(B_T + H_{A1}\cot\eta)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_A - H_T) / TV_s) - \cos 2\pi(t / T - (H_A - H_{A1}) / TV_s)] + [f_a\cot\xi + (1 - f_a)(B_T + H_{A1}\cot\eta) / H_A](-TV_s / 2\pi)\{H_T\cos 2\pi(t / T - (H_A - H_T) / TV_s) - H_{A1}\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_A - H_T) / TV_s) - \sin 2\pi(t / T - (H_A - H_{A1}) / TV_s)]\} + [(1 - f_a)\cot\xi / H_A](-TV_s / 2\pi)\{H_T^2\cos 2\pi(t / T - (H_A - H_T) / TV_s) - H_{A1}^2\cos 2\pi(t / T - (H_A - H_{A1}) / TV_s) - (TV_s / \pi)[H_T\sin 2\pi(t / T - (H_A - H_T) / TV_s) - H_{A1}\sin 2\pi(t / T - (H_A - H_{A1}) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_A - H_T) / TV_s) - \cos 2\pi(t / T - (H_A - H_{A1}) / TV_s))]\},$$

$$Q_{hA3} / k_h \gamma = (f_a H_{A3}\cot\beta)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - \cos 2\pi(t / T - (H_A - H_T) / TV_s)] + [(1 - f_a)H_{A3}\cot\beta / H_A - f_a\cot\beta](-TV_s / 2\pi)\{H_{A3}\cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - H_T\cos 2\pi(t / T - (H_A - H_T) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_A - H_{A3}) / TV_s) - \sin 2\pi(t / T - (H_A - H_T) / TV_s)]\} + [(f_a - 1)\cot\beta / H_A](-TV_s / 2\pi)\{H_{A3}^2\cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - H_T^2\cos 2\pi(t / T - (H_A - H_T) / TV_s) - (TV_s / \pi)[H_{A3}\sin 2\pi(t / T - (H_A - H_{A3}) / TV_s) - H_T\sin 2\pi(t / T - (H_A - H_T) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - \cos 2\pi(t / T - (H_A - H_T) / TV_s))]\}.$$

$$m_{p1}(z) = \rho z \cot\eta \quad (0 \leq z < H_{p1}), \quad m_{p2}(z) = \rho H_{p3} \cot\theta \quad (H_{p1} \leq z < H_{p4}),$$

$$m_{p3}(z) = \rho(H_p - z) \cot\theta \quad (H_{p4} \leq z \leq H_p);$$

$$W_P = W_{p1} + W_{p2} + W_{p3}, \quad W_{p1} = 0.5\gamma H_{p1}^2 \cot\eta, \quad W_{p2} = \gamma H_{p2} H_{p3} \cot\theta, \quad W_{p3} = 0.5\gamma H_{p3}^2 \cot\theta;$$

$$Q_{hP} = k_h W_P; \quad Q_{hP}(t) = Q_{hP1} + Q_{hP2} + Q_{hP3},$$

$$Q_{hP1} / k_h \gamma = (f_a \cot\eta)(-TV_s / 2\pi)\{H_{p1}\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \sin 2\pi(t / T - H_p / TV_s)]\} + [(1 - f_a)\cot\eta / H_p](-TV_s / 2\pi)\{H_{p1}^2\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / \pi)[H_{p1}\sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) + (TV_s / 2\pi)(\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \cos 2\pi(t / T - H_p / TV_s))]\},$$

$$Q_{hP2} / k_h \gamma = (f_a H_{p3} \cot\theta)(-TV_s / 2\pi)[\cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s)] + [(1 - f_a)(H_{p3} \cot\theta) / H_p](-TV_s / 2\pi)\{H_{p4}\cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - H_{p1}\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / 2\pi)[\sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \sin 2\pi(t / T - (H_p - H_{p1}) / TV_s)]\},$$

$$\begin{aligned} Q_{\text{hP3}} / k_{\text{h}} \gamma = & (f_{\text{a}} H_{\text{p}} \cot \theta) (-TV_{\text{s}} / 2\pi) [\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_{\text{p}} - H_{\text{p4}}) / TV_{\text{s}})] + [(1 - f_{\text{a}})(H_{\text{p}} \\ & \cot \theta) / H_{\text{p}} - f_{\text{a}} \cot \theta] (-TV_{\text{s}} / 2\pi) \{H_{\text{p}} \cos 2\pi(t / T) - H_{\text{p4}} \cos 2\pi(t / T - (H_{\text{p}} - H_{\text{p4}}) / TV_{\text{s}}) - (TV_{\text{s}} / 2\pi) \\ & [\sin 2\pi(t / T) - \sin 2\pi(t / T - (H_{\text{p}} - H_{\text{p4}}) / TV_{\text{s}})]\} + [(f_{\text{a}} - 1) \cot \theta / H_{\text{p}}] (-TV_{\text{s}} / 2\pi) \{H_{\text{p}}^2 \cos 2\pi(t / T) \\ & - H_{\text{p4}}^2 \cos 2\pi(t / T - (H_{\text{p}} - H_{\text{p4}}) / TV_{\text{s}}) - (TV_{\text{s}} / \pi) [H_{\text{p}} \sin 2\pi(t / T) - H_{\text{p4}} \sin 2\pi(t / T - (H_{\text{p}} - H_{\text{p4}}) / \\ & TV_{\text{s}}) + (TV_{\text{s}} / 2\pi) (\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_{\text{p}} - H_{\text{p4}}) / TV_{\text{s}}))]\}. \end{aligned}$$

Case 4: $H \cot \beta > H_{\text{T}} (\cot \xi + \cot \eta)$

$$H_{\text{A1}} = [H \cot \beta - B_{\text{T}} - H_{\text{T}} (\cot \eta + \cot \xi)] \tan \eta, \quad H_{\text{A2}} = H_{\text{T}} + H_{\text{A1}}, \quad H_{\text{A3}} = H_{\text{T}} + H,$$

$$H_{\text{p4}} = H - H_{\text{A1}},$$

$$H_{\text{B1}} = H_{\text{B}} \cot \alpha \tan \eta, \quad H_{\text{B2}} = H_{\text{B}} (1 + \cot \alpha \tan \eta), \quad H_{\text{p3}} = (H_{\text{p4}} - H_{\text{B2}}) / (\cot \theta \tan \eta - 1),$$

$$H_{\text{A}} = H_{\text{A3}} + H_{\text{p3}}, \quad H_{\text{p2}} = H_{\text{B2}} - H_{\text{p3}}, \quad H_{\text{p1}} = H_{\text{p4}} - H_{\text{p2}}, \quad H_{\text{p}} = H_{\text{p4}} + H_{\text{p3}};$$

$$C_{\text{p}} = c_{\text{p}} H_{\text{p3}} / \sin \theta, \quad C_{\text{AP}} = c H_{\text{p4}}, \quad C_{\text{PB}} = c H_{\text{B2}};$$

$$m_{\text{A1}}(z) = \rho [B_{\text{T}} + z (\cot \eta + \cot \xi)] \quad (0 \leq z < H_{\text{T}}),$$

$$m_{\text{A2}}(z) = \rho [B_{\text{T}} + H_{\text{T}} (\cot \beta + \cot \xi) + z (\cot \eta - \cot \beta)] \quad (H_{\text{T}} \leq z < H_{\text{A2}}),$$

$$m_{\text{A3}}(z) = \rho (H_{\text{A3}} - z) \cot \beta \quad (H_{\text{A2}} \leq z \leq H_{\text{A3}});$$

$$W_{\text{A}} = W_{\text{A1}} + W_{\text{A2}} + W_{\text{A3}}, \quad W_{\text{A1}} = \gamma [B_{\text{T}} H_{\text{T}} + 0.5 H_{\text{T}}^2 (\cot \eta + \cot \xi)],$$

$$W_{\text{A2}} = \gamma \{H_{\text{A1}} [B_{\text{T}} + H_{\text{T}} (\cot \beta + \cot \xi)] + 0.5 H_{\text{A1}} (H_{\text{T}} + H_{\text{A2}}) (\cot \eta - \cot \beta)\},$$

$$W_{\text{A3}} = 0.5 \gamma (H_{\text{A3}} - H_{\text{A2}})^2 \cot \beta; \quad Q_{\text{hA}} = k_{\text{h}} W_{\text{A}}; \quad Q_{\text{hA}}(t) = Q_{\text{hA1}} + Q_{\text{hA2}} + Q_{\text{hA3}},$$

$$\begin{aligned} Q_{\text{hA1}} / k_{\text{h}} \gamma = & (f_{\text{a}} B_{\text{T}}) (-TV_{\text{s}} / 2\pi) [\cos 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) - \cos 2\pi(t / T - H_{\text{A}} / TV_{\text{s}})] + [f_{\text{a}} (\cot \eta \\ & + \cot \xi) + (1 - f_{\text{a}}) B_{\text{T}} / H_{\text{A}}] (-TV_{\text{s}} / 2\pi) \{H_{\text{T}} \cos 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) - (TV_{\text{s}} / 2\pi) [\sin 2\pi(t / T - \\ & (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) - \sin 2\pi(t / T - H_{\text{A}} / TV_{\text{s}})]\} + [(1 - f_{\text{a}}) (\cot \eta + \cot \xi) / H_{\text{A}}] (-TV_{\text{s}} / 2\pi) \{H_{\text{T}}^2 \cos 2\pi(t / T \\ & - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) - (TV_{\text{s}} / \pi) [H_{\text{T}} \sin 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) + (TV_{\text{s}} / 2\pi) (\cos 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) \\ & / TV_{\text{s}}) - \cos 2\pi(t / T - H_{\text{A}} / TV_{\text{s}}))]\}, \end{aligned}$$

$$\begin{aligned} Q_{\text{hA2}} / k_{\text{h}} \gamma = & f_{\text{a}} [B_{\text{T}} + H_{\text{T}} (\cot \beta + \cot \xi)] (-TV_{\text{s}} / 2\pi) [\cos 2\pi(t / T - (H_{\text{A}} - H_{\text{A2}}) / TV_{\text{s}}) - \cos 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) \\ & / TV_{\text{s}})] + \{f_{\text{a}} (\cot \eta - \cot \beta) + (1 - f_{\text{a}}) [B_{\text{T}} + H_{\text{T}} (\cot \beta + \cot \xi)] / H_{\text{A}}\} (-TV_{\text{s}} / 2\pi) \{H_{\text{A2}} \cos 2\pi(t / T - (H_{\text{A}} - H_{\text{A2}}) / \\ & TV_{\text{s}}) - H_{\text{T}} \cos 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) - (TV_{\text{s}} / 2\pi) [\sin 2\pi(t / T - (H_{\text{A}} - H_{\text{A2}}) / TV_{\text{s}}) - \sin 2\pi(t / T - (H_{\text{A}} - \\ & H_{\text{T}}) / TV_{\text{s}})]\} + [(1 - f_{\text{a}}) (\cot \eta - \cot \beta) / H_{\text{A}}] (-TV_{\text{s}} / 2\pi) \{H_{\text{A2}}^2 \cos 2\pi(t / T - (H_{\text{A}} - H_{\text{A2}}) / TV_{\text{s}}) - H_{\text{T}}^2 \cos 2\pi(t / T - \\ & (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) - (TV_{\text{s}} / \pi) [H_{\text{A2}} \sin 2\pi(t / T - (H_{\text{A}} - H_{\text{A2}}) / TV_{\text{s}}) - H_{\text{T}} \sin 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}) + (TV_{\text{s}} / \\ & 2\pi) (\cos 2\pi(t / T - (H_{\text{A}} - H_{\text{A2}}) / TV_{\text{s}}) - \cos 2\pi(t / T - (H_{\text{A}} - H_{\text{T}}) / TV_{\text{s}}))]\}, \end{aligned}$$

$$Q_{hA3} / k_h \gamma = (f_a H_{A3} \cot \beta) (-TV_s / 2\pi) [\cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s)] \\ + [(1 - f_a) H_{A3} \cot \beta / H_A - f_a \cot \beta] (-TV_s / 2\pi) \{H_{A3} \cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - H_{A2} \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_A - H_{A3}) / TV_s) - \sin 2\pi(t / T - (H_A - H_{A2}) / TV_s)]\} + [(f_a - 1) \cot \beta / H_A] (-TV_s / 2\pi) \{H_{A3}^2 \cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - H_{A2}^2 \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s) - (TV_s / \pi) [H_{A3} \sin 2\pi(t / T - (H_A - H_{A3}) / TV_s) - H_{A2} \sin 2\pi(t / T - (H_A - H_{A2}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_A - H_{A3}) / TV_s) - \cos 2\pi(t / T - (H_A - H_{A2}) / TV_s))]\}.$$

$$m_{p1}(z) = \rho z \cot \eta \quad (0 \leq z < H_{p1}), \quad m_{p2} = \rho H_{p3} \cot \theta \quad (H_{p1} \leq z < H_{p4}),$$

$$m_{p3}(z) = \rho (H_p - z) \cot \theta \quad (H_{p4} \leq z \leq H_p);$$

$$W_p = W_{p1} + W_{p2} + W_{p3}, \quad W_{p1} = 0.5 \gamma H_{p1}^2 \cot \eta, \quad W_{p2} = \gamma H_{p2} H_{p3} \cot \theta, \quad W_{p3} = 0.5 \gamma H_{p3}^2 \cot \theta;$$

$$Q_{hp} = k_h W_p; \quad Q_{hp}(t) = Q_{hp1} + Q_{hp2} + Q_{hp3},$$

$$Q_{hp1} / k_h \gamma = (f_a \cot \eta) (-TV_s / 2\pi) \{H_{p1} \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \sin 2\pi(t / T - H_p / TV_s)]\} + [(1 - f_a) \cot \eta / H_p] (-TV_s / 2\pi) \{H_{p1}^2 \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / \pi) [H_{p1} \sin 2\pi(t / T - (H_p - H_{p1}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - \cos 2\pi(t / T - H_p / TV_s))]\},$$

$$Q_{hp2} / k_h \gamma = (f_a H_{p3} \cot \theta) (-TV_s / 2\pi) [\cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s)] + [(1 - f_a) (H_{p3} \cot \theta) / H_p] (-TV_s / 2\pi) \{H_{p4} \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - H_{p1} \cos 2\pi(t / T - (H_p - H_{p1}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) - \sin 2\pi(t / T - (H_p - H_{p1}) / TV_s)]\},$$

$$Q_{hp3} / k_h \gamma = (f_a H_p \cot \theta) (-TV_s / 2\pi) [\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s)] + [(1 - f_a) (H_p \cot \theta) / H_p - f_a \cot \theta] (-TV_s / 2\pi) \{H_p \cos 2\pi(t / T) - H_{p4} \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T) - \sin 2\pi(t / T - (H_p - H_{p4}) / TV_s)]\} + [(f_a - 1) \cot \theta / H_p] (-TV_s / 2\pi) \{H_p^2 \cos 2\pi(t / T) - H_{p4}^2 \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s) - (TV_s / \pi) [H_p \sin 2\pi(t / T) - H_{p4} \sin 2\pi(t / T - (H_p - H_{p4}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T) - \cos 2\pi(t / T - (H_p - H_{p4}) / TV_s))]\}.$$

The four cases having the same C_A, C_B, Q_{hb} , and $Q_{hb}(t)$, as follows:

$$C_A = c_A H / \sin \beta, \quad C_B = c_B [D_B + H_B (\cot \zeta + \cot \alpha)];$$

$$m_{B1}(z) = \rho z \cot \eta \quad (0 \leq z < H_{B1}), \quad m_{B2}(z) = \rho (H_{B2} - z) \cot \alpha \quad (H_{B1} \leq z \leq H_{B2}),$$

$$m_{B3}(z) = \rho_B [D_B + z (\cot \zeta + \cot \alpha)] \quad (0 \leq z \leq H_B);$$

$$W_B = W_{B1} + W_{B2} + W_{B3}, \quad W_{B1} = 0.5 \gamma H_{B1}^2 \cot \eta, \quad W_{B2} = 0.5 \gamma H_B^2 \cot \alpha,$$

$$W_{B3} = \gamma_B [H_B D_B + 0.5 H_B^2 (\cot \zeta + \cot \alpha)]; \quad Q_{hb} = k_h W_B; \quad Q_{hb}(t) = Q_{hb1} + Q_{hb2} + Q_{hb3},$$

$$Q_{hb1} / k_h \gamma = (f_a \cot \eta) (-TV_s / 2\pi) \{H_{B1} \cos 2\pi(t / T - (H_{B2} - H_{B1}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t / T - (H_{B2} - H_{B1}) / TV_s) - \sin 2\pi(t / T - H_{B2} / TV_s)]\} + [(1 - f_a) \cot \eta / H_{B2}] (-TV_s / 2\pi) \{H_{B1}^2 \cos 2\pi(t / T - (H_{B2} - H_{B1}) / TV_s) - (TV_s / \pi) [H_{B1} \sin 2\pi(t / T - (H_{B2} - H_{B1}) / TV_s) + (TV_s / 2\pi) (\cos 2\pi(t / T - (H_{B2} - H_{B1}) / TV_s) - \cos 2\pi(t / T - H_{B2} / TV_s))]\},$$

$$Q_{hB2} / k_h \gamma = (f_a H_{B2} \cot \alpha) (-TV_s / 2\pi) [\cos 2\pi(t/T) - \cos 2\pi(t/T - (H_{B2} - H_{B1}) / TV_s)] + [(1 - 2f_a) \cot \alpha] (-TV_s / 2\pi) \{H_{B2} \cos 2\pi(t/T) - H_{B1} \cos 2\pi(t/T - (H_{B2} - H_{B1}) / TV_s) - (TV_s / 2\pi) [\sin 2\pi(t/T) - \sin 2\pi(t/T - (H_{B2} - H_{B1}) / TV_s)]\} + [(f_a - 1) \cot \alpha / H_{B2}] (-TV_s / 2\pi) \{H_{B2}^2 \cos 2\pi(t/T) - H_{B1}^2 \cos 2\pi(t/T - (H_{B2} - H_{B1}) / TV_s) - (TV_s / \pi) [H_{B2} \sin 2\pi(t/T) - H_{B1} \sin 2\pi(t/T - (H_{B2} - H_{B1}) / TV_s)] + (TV_s / 2\pi) (\cos 2\pi(t/T) - \cos 2\pi(t/T - (H_{B2} - H_{B1}) / TV_s))\},$$

$$Q_{hB3} / k_h \gamma_B = (f_a D_B) (-TV_{sB} / 2\pi) [\cos 2\pi(t/T) - \cos 2\pi(t/T - H_B / TV_{sB})] + [f_a (\cot \zeta + \cot \alpha) + (1 - f_a) D_B / H_B] (-TV_{sB} / 2\pi) \{H_B \cos 2\pi(t/T) - (TV_{sB} / 2\pi) [\sin 2\pi(t/T) - \sin 2\pi(t/T - H_B / TV_{sB})]\} + [(1 - f_a) (\cot \zeta + \cot \alpha) / H_B] (-TV_{sB} / 2\pi) \{H_B^2 \cos 2\pi(t/T) - (TV_{sB} / \pi) [H_B \sin 2\pi(t/T) + (TV_{sB} / 2\pi) (\cos 2\pi(t/T) - \cos 2\pi(t/T - H_B / TV_{sB}))]\}.$$

Q_{vA} , Q_{vB} , and Q_{vP} , for the four cases, as follows:

k_v substitutes k_h in Q_{hA} , Q_{hB} , and Q_{hP} , that turn into Q_{vA} , Q_{vB} , and Q_{vP} , respectively.

$Q_{vA}(t)$, $Q_{vB}(t)$, and $Q_{vP}(t)$, for the four cases, as follows:

k_v substitutes k_h in $Q_{hA}(t)$, $Q_{hB}(t)$, and $Q_{hP}(t)$, that turn into $Q_{vA}(t)$, $Q_{vB}(t)$, and $Q_{vP}(t)$, respectively.

File S2 FS_{min} and FS_{max}

FS_{min} can be obtained by the following equation:

$$(\cos \theta + \sin \theta \tan \delta_p / FS) \{[(W_B + Q_{vB}(t)) \tan \delta_B / FS - Q_{hB}(t) + C_B / FS] - [(W_A + Q_{vA}(t)) (\sin \beta - \cos \beta \tan \delta_A / FS) - C_A / FS + Q_{hA}(t) (\cos \beta + \sin \beta \tan \delta_A / FS)] / (\cos \beta + \sin \beta \tan \delta_A / FS)\} = (W_P + Q_{vP}(t)) (\sin \theta - \cos \theta \tan \delta_p / FS) - C_P / FS + Q_{hP}(t) (\cos \theta + \sin \theta \tan \delta_p / FS).$$

FS_{max} can be obtained by the following equation:

$$[(\cos \theta + \sin \theta \tan \delta_p / FS) + (\sin \theta - \cos \theta \tan \delta_p / FS) \tan \phi / FS] \{[(W_B + Q_{vB}(t) + C_{PB} / FS) \tan \delta_B / FS - Q_{hB}(t) + C_B / FS] / (1 - \tan \delta_B \tan \phi / FS^2) - [(W_A + Q_{vA}(t) - C_{AP} / FS) (\sin \beta - \cos \beta \tan \delta_A / FS) - C_A / FS + Q_{hA}(t) (\cos \beta + \sin \beta \tan \delta_A / FS)] / [(\cos \beta + \sin \beta \tan \delta_A / FS) + (\sin \beta - \cos \beta \tan \delta_A / FS) \tan \phi / FS]\} = (W_P + Q_{vP}(t) + C_{AP} / FS - C_{PB} / FS) (\sin \theta - \cos \theta \tan \delta_p / FS) - C_P / FS + Q_{hP}(t) (\cos \theta + \sin \theta \tan \delta_p / FS).$$