



Anti-quantum cross-chain identity authentication approach using dynamic group signature*

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Abstract: To solve the privacy leakage and identity island in cross-chain interaction, we propose an anti-quantum cross-chain identity authentication approach based on dynamic group signature (DGS-AQCCIDAA) for smart education. The relay-based cross-chain model promotes interconnection in heterogeneous consortium blockchains. DGS is used as the endorsement strategy for cross-chain identity authentication. Our approach can ensure quantum security under the learning with error (LWE) and inhomogeneous small integer solution (ISIS) assumptions, and it uses non-interactive zero-knowledge proof (NIZKP) to protect user identity privacy. Our scheme has low calculation overhead and provides anonymous cross-chain identity authentication in the smart education system.

Key words: Cross-chain; Identity authentication; Dynamic group signature (DGS); Anti-quantum security; Zero-knowledge proof

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1 Introduction

Blockchain is a combination of cryptography, peer-to-peer communication, consensus mechanisms, smart contracts and other technologies. Blockchain is used to construct a trusted system (Ma et al., 2020) because of its decentralization and anti-tampering. There are three types of blockchain: the public blockchain is completely open and transparent with no identity authorization, the consortium blockchain includes the identity authorization access mechanism, and the private blockchain is maintained by a single node in the network.

PKI-based identity management in the consortium chain uses a certificate to authenticate the user identity. The certificate-based authentication

scheme cannot provide anonymous authentication services and will result in leakage of private information. In addition, because each consortium blockchain is independent with no unified identity management system, the identity island problem (Yang et al., 2019) exists. Providing a unified identity for different blockchains and protecting user information are vital problems of blockchain.

Cross-chain technology (Yu et al., 2024b) is an important method for consortium blockchain to achieve interoperability and improve scalability. Cross-chain identity authentication technology can achieve unified identity management and authentication between blockchains, and solves the problem of identity islands. There have been several previous cross-chain authentication schemes. An identity authentication model for cross-chain (Wang et al., 2022a) solves the identity authentication problem in heterogeneous application chains and eliminates duplicate authentication when the application chain accesses the cross-chain system, but identity infor-

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mation leakage still occurs in cross-chain transaction. The cross-chain identity authentication mechanism in the internet of things (IoT) using identity-based encryption (Shao et al., 2021) cause a performance bottleneck. Lightweight identity authentication (Wang et al., 2022b) in cross-chain cannot protect the identity of users in cross-chain interaction. The cross-chain authentication scheme based on certificate-less signcryption (Liu et al., 2024) has a high degree of decentralization and scalability, but it is unable to solve the problem of user identity information leakage in the identity authentication process. Currently, cross-chain identity authentication is mainly focused on decentralized identity management and authentication, no research has been reported on anonymous identity authentication.

The group signature is anonymous and traceable, so it can be used to construct anonymous authentication protocols. However, traditional group signature schemes are not resistant to quantum computing attacks. The lattice-based cryptosystem (Yu et al., 2024a, 2023) has attracted extensive attention due to its anti-quantum security. Doc et al. (2010) combined the preimage sampling function and zero-knowledge proof technique to achieve a lattice-based group signature, but this scheme has a long key and signature, the identity of group members cannot be changed in the initial phase and it cannot be applied in scenarios that have dynamic features. An anonymous authentication system using lattice-based group signatures (Libert et al., 2016) adds a group member access mechanism to allow new users to join the group, but the joining process is complex and there is no group member revocation mechanism. A fully dynamic group signature (DGS) (including access and revocation mechanisms) scheme in a lattice based on Merkle hash trees (Ling et al., 2017) has high calculation overhead and cannot easily revoke members. The verifier-local revocation (VLR) model (Boneh and Shacham, 2004) requires only the verifier to download the revocation list and the calculation cost in the revocation phase is very low in practical applications. Langlois et al. (2014) succeeded in using the VLR revocation mechanism in lattice-based group signature.

1.1 Contribution

In this article, we present an anti-quantum cross-chain identity authentication approach based

on dynamic group signature (DGS-AQCCIDAA) for smart education. The main contributions are as follows: (1) DGS-AQCCIDAA uses the group signature and relay architecture to realize cross-chain identity anonymous authentication, which protects the identity privacy of the users in the authentication process. (2) DGS-AQCCIDAA allows the relay chain administrator nodes to open the signature to trace the signer and ensures that the anonymity is not abused. (3) DGS-AQCCIDAA adds access and revocation functions to realize dynamic management of cross-chain users. (4) DGS-AQCCIDAA security is based on the hardness of LWE and the ISIS problems in the lattice, so it can resist quantum computing attacks in the smart education field.

2 Preliminaries

Preliminaries are introduced in this section. Notations used in this paper are listed in Table 1.

Table 1 Notations used in this paper

Notation	Description
\mathbb{Z}	Set of integers
\mathbb{R}	Set of real numbers
\mathbf{a}, \mathbf{b}	Vectors
\mathbf{A}, \mathbf{B}	Matrices
H	A hash function
\leftarrow_R	Sampling at random
$\ \cdot\ $	2-parameter of vector
$\ \cdot\ _\infty$	∞ -parameter of vector
ω, O	Standard asymptotic notations
Cert _{<i>i</i>}	Certificate for group member <i>i</i>
DID	Digital identifier of user

2.1 Lattice theory

Let $\mathbf{b}_1, \mathbf{b}_2, \dots, \mathbf{b}_m$ be m linearly independent vectors in the n -dimension Euclidean space \mathbb{R}^n . Lattice Λ is defined as the set of all linear combinations of integer coefficients on $\mathbf{b}_1, \mathbf{b}_2, \dots, \mathbf{b}_m$ where $\Lambda = L(\mathbf{B}) = L(\mathbf{b}_1, \mathbf{b}_2, \dots, \mathbf{b}_m) = \{\sum_{i=1}^m c_i \mathbf{b}_i | c_i \in \mathbb{Z}\}$, \mathbf{B} is the basis of Λ , m is the order of Λ and n is the dimension of Λ . Λ is called a full rank lattice when $m = n$.

Definition 1 Given $q, m, n \in \mathbb{Z}$, a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$ and a vector $\mathbf{u} \in \mathbb{Z}_q^n$, the special integer lattices are as follows:

$$\begin{cases} \mathbf{A}^\perp(\mathbf{A}) = \{\mathbf{e} \in \mathbb{Z}_q^m : \mathbf{A}\mathbf{e} = \mathbf{0}(\text{mod } q)\}, \\ \mathbf{A}_u^\perp(\mathbf{A}) = \{\mathbf{e} \in \mathbb{Z}_q^m : \mathbf{A}\mathbf{e} = \mathbf{u}(\text{mod } q)\}. \end{cases} \quad (1)$$

Definition 2 Given a lattice \mathbf{A} , a center vector $\mathbf{c} \in \mathbb{R}^n$ and $s \in \mathbb{R}^+$. For $\forall \mathbf{x} \in \mathbf{A}$, $\rho_{s,\mathbf{c}}(\mathbf{x}) = \exp(-\pi \frac{\|\mathbf{x}-\mathbf{c}\|^2}{s^2})$ and $\rho_{s,\mathbf{c}}(\mathbf{A}) = \sum_{\mathbf{x} \in \mathbf{A}} \rho_{s,\mathbf{c}}(\mathbf{x})$, the Gaussian distribution in \mathbf{A} is as follows:

$$D_{\mathbf{A},s,\mathbf{c}}(\mathbf{x}) = \frac{\rho_{s,\mathbf{c}}(\mathbf{x})}{\rho_{s,\mathbf{c}}(\mathbf{A})}, \quad (\forall \mathbf{x} \in \mathbf{A}). \quad (2)$$

2.2 Hard assumptions in the lattice

Hard assumptions of DGS-AQCBCIDAA are introduced in this subsection.

(1) Small integer solution (SIS) problem: Given an integer q , a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$ and a real number β , SIS problem is to find a non-zero vector $\mathbf{e} \in \mathbb{Z}^m$ such that $\mathbf{A}\mathbf{e} = \mathbf{0}(\text{mod } q)$ and $\|\mathbf{e}\| \leq \beta$.

(2) ISIS problem: Given an integer q , a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$, a real number β , and a vector $\mathbf{u} \in \mathbb{Z}_q^n$, ISIS problem is to find a non-zero vector $\mathbf{e} \in \mathbb{Z}^m$ such that $\mathbf{A}\mathbf{e} = \mathbf{u}(\text{mod } q)$, and $\|\mathbf{e}\| \leq \beta$.

(3) Split-SIS problem: Given $q, N \in \mathbb{Z}$, a matrix $\mathbf{A} = (\mathbf{A}_1 \parallel \mathbf{A}_2) \leftarrow_R \mathbb{Z}_q^{n \times 2m}$, and $\beta \in \mathbb{R}$, the split-SIS problem is to find a tuple $\mathbf{x} = ((\mathbf{x}_1, \mathbf{x}_2), h) \in \mathbb{Z}^{2m} \times \mathbb{Z}$ such that $\mathbf{x}_1 \neq \mathbf{0}$ (or $h\mathbf{x}_2 \neq \mathbf{0}$), $\|\mathbf{x}\| \leq \beta$, $h \in [1, N]$ and $\mathbf{A}_1\mathbf{x}_1 + h\mathbf{A}_2\mathbf{x}_2 = \mathbf{0}$.

(4) LWE problem: Given $q, \alpha \in \mathbb{R}^+$, a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$, and a vector $\mathbf{u} \in \mathbb{Z}_q^n$, where the modulus $q \geq 3$ and $\mathbf{e} \leftarrow_R \chi_\alpha^m$ is randomly extracted from the Gaussian noise distribution χ .

i. Searchable LWE problem: The searchable LWE problem is to calculate the vector $\mathbf{s} \in \mathbb{Z}_q^n$ with non-negligible probability such that $\mathbf{u} = \mathbf{A}\mathbf{s} + \mathbf{e}$.

ii. Decisional LWE problem: Given a random vector $\mathbf{s} \in \mathbb{Z}_q^n$, the decisional the LWE problem is to distinguish whether $\mathbf{u} \in \mathbb{Z}_q^n$ is obtained from an example of LWE problem ($\mathbf{u} = \mathbf{A}\mathbf{s} + \mathbf{e}$) or randomly chosen from the uniform distribution \mathbb{Z}_q^n .

(5) Extended-LWE (eLWE) problem: Given $q, \alpha \in \mathbb{R}^+$, a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$, a vector $\mathbf{b} \in \mathbb{Z}_q^m$, and $\mathbf{e} \leftarrow_R \chi_\alpha^m$, the eLWE problem is to find the non-zero vectors \mathbf{s} and \mathbf{x} such that $\mathbf{b} = \mathbf{A}^T \mathbf{s} + p\mathbf{e} + \mathbf{x}$, where $p \geq (\alpha q \sqrt{m} + \beta)m^2$ and $\|\mathbf{x}\| \leq \beta$.

2.3 Polynomial time algorithm in lattice

(1) Trapdoor generation algorithm: Given integers $n, q = \text{poly}(n)$ and $m = O(n \log q)$, the trap-

door generation algorithm TrapGen (q, m, n) outputs a random matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$ and a full rank lattice $\mathbf{T}_\mathbf{A} \subset \Lambda^\perp(\mathbf{A})$, where \mathbf{A} is indistinguishable from the uniform distribution on $\mathbb{Z}_q^{n \times m}$ and $\|\mathbf{T}_\mathbf{A}\| \leq \sqrt{O(n \log q)}$.

(2) Preimage sampling algorithm: Given a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$, a full rank lattice $\mathbf{T}_\mathbf{A} \subset \Lambda^\perp(\mathbf{A})$, a random vector $\mathbf{u} \in \mathbb{Z}_q^n$ and a Gaussian parameter $\sigma = O(\sqrt{n \log q})$, the preimage sampling algorithm SamplePre $(\mathbf{A}, \mathbf{T}_\mathbf{A}, \mathbf{u}, \sigma)$ outputs a vector $\mathbf{e} \leftarrow D_{\mathbf{A}_\mathbf{u}^\perp(\mathbf{A}), \sigma}$ such that $\|\mathbf{e}\| \leq \sigma \sqrt{m}$ and $\mathbf{A}\mathbf{e} = \mathbf{u}(\text{mod } q)$.

(3) Super sampling algorithm: Given the matrices $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$ and $\mathbf{C} \in \mathbb{Z}_q^n$, the super sampling algorithm SuperSamp (\mathbf{A}, \mathbf{C}) outputs a full rank matrix $\mathbf{T}_\mathbf{B} \subset \Lambda^\perp(\mathbf{B})$ and a matrix $\mathbf{B} \in \mathbb{Z}_q^{n \times m}$ such that $\mathbf{A}\mathbf{B}^T = \mathbf{C}$, where $\|\mathbf{T}_\mathbf{B}\| \leq m^{1.5} \omega(\sqrt{\log m})$.

(4) Lattice basis delegation algorithm: Given a matrix $\mathbf{A}' \in \mathbb{Z}_q^{n \times 2m}$, a full rank lattice $\mathbf{T}_\mathbf{A} \subset \Lambda^\perp(\mathbf{A})$, and a real $s = m\omega(\log m)$, the lattice basis delegation algorithm ExtBasis $(\mathbf{A}', \mathbf{T}_\mathbf{A}, s)$ outputs a matrix $\mathbf{T}_{\mathbf{A}'}$ such that $\|\mathbf{T}_{\mathbf{A}'}\| \leq m^{1.5} \omega(\sqrt{\log m})$.

2.4 Non-interactive zero-knowledge proof

The NIZKP protocol is a two-party protocol and is an important tool in cryptographic protocols. The prover can prove to the verifier that he owns the knowledge, but does not reveal any information about the knowledge. The NIZKP reduces the number of interactions to a single one, and enables offline proof and public verification. Non-interactive zero-knowledge proof of knowledge (NIZKPoK) used in this study is as follows.

(1) NIZKPoK for ISIS relations (Laguillaumie et al., 2013) is:

$$R_{\text{ISIS}} = \left\{ \begin{array}{l} (\mathbf{A}, \mathbf{y}, \beta; \mathbf{x}) \in \mathbb{Z}_q^{n \times m} \times \mathbb{Z}_q^n \times \mathbb{R} \times \mathbb{Z}_q^m : \\ \mathbf{A}\mathbf{x} = \mathbf{y}, \|\mathbf{x}\| \leq \beta \end{array} \right\}. \quad (3)$$

(2) Given a matrix $\mathbf{A} = (\mathbf{A}_1 \parallel \mathbf{A}_2)$ and a vector $\mathbf{y} = (\mathbf{y}_1, \mathbf{y}_2) \in \mathbb{Z}_q^n \times \mathbb{Z}^m$, where $0 < \|\mathbf{y}_2\| \leq \beta \sqrt{m}$, the prover can provide a proof about $\mathbf{x} = (\mathbf{x}_1, \mathbf{x}_2, h) \in \mathbb{Z}^{2m+1}$ such that $f_\mathbf{A}(\mathbf{x}_1, \mathbf{x}_2, h) = (\mathbf{A}_1\mathbf{x}_1 + h\mathbf{A}_2\mathbf{x}_2, \mathbf{x}_2) = \mathbf{y}$ ($\|\mathbf{x}_1\| \leq \beta \sqrt{m}, h \in [1, N]$) when $\mathbf{x}_2 = \mathbf{y}_2$.

The NIZKPoK for split-SIS relations (Laguil-

laumie et al., 2013) is:

$$R_{\text{Split-SIS}} = \left\{ \begin{array}{l} (\mathbf{A}, \mathbf{y}, \beta, N; \mathbf{x}_1, h) \in \mathbb{Z}_q^{n \times 2m} \times \mathbb{Z}_q^n \times \\ \mathbb{Z}^m \times \mathbb{R} \times \mathbb{Z} \times \mathbb{Z}_q^m \times \mathbb{Z} : \mathbf{A}_1 \mathbf{x}_1 + \\ h \mathbf{A}_2 \mathbf{y}_2 = \mathbf{y}_1, \|\mathbf{x}_1\| \leq \beta \sqrt{m}, h \in [1, N] \end{array} \right\}. \quad (4)$$

(3) The NIZKPoK for LWE relations (Nguyen et al., 2015) is:

$$R_{\text{LWE}} = \left\{ \begin{array}{l} (\mathbf{A}, \mathbf{b}, \alpha; t) \in \mathbb{Z}_q^{n \times m} \times \mathbb{Z}_q^n \times \mathbb{R} \times \mathbb{Z}_q^n : \\ \|\mathbf{b} - \mathbf{A}^T t\| \leq \alpha q \sqrt{m} \end{array} \right\}. \quad (5)$$

(4) The NIZKPoK for eLWE relations (Laguilaumie et al., 2013) is:

$$R_{\text{eLWE}} = \left\{ \begin{array}{l} (\mathbf{A}, \mathbf{b}, \gamma; t, \mathbf{e}, \mathbf{x}) \in \mathbb{Z}_q^{n \times m} \times \mathbb{Z}_q^n \times \mathbb{R} \\ \times \mathbb{Z}_q^n \times \mathbb{Z}^m \times \mathbb{Z}^m : \mathbf{b} = \mathbf{A}t + \mathbf{p}\mathbf{e} + \mathbf{x}, \\ \gamma = \max(\alpha q \sqrt{m}, \beta), \|\mathbf{x}\| \leq \gamma, \|\mathbf{e}\| \leq \gamma \end{array} \right\}. \quad (6)$$

3 Model description

3.1 Cross-chain system model

Currently, cross-chain architecture solutions have a notary mechanism, sidechain/relay, distributed private key control and hash locking. The risk of centralization exists in a notary architecture; there are application limitations in the hash time locking and distributed private key control. The side chain increases the network complexity and includes a security risk. Relay chain architecture has wider application prospects and can meet the largest number of cross-chain requirements. DGS-AQCCIDAA relies on relay chain architecture (He et al., 2023) and the model of the cross-chain system as shown in Fig. 1. The cross-chain system model consists of three parts: the application chain, the relay chain, and the gateway.

(1) The relay chain is responsible for the cross-chain identity registration, identity authentication, identity management, and forwarding of cross-chain transactions. All entities involved in the cross-chain network maintain the relay chain via the consensus mechanism. Cross-chain information is stored in the relay chain ledger.

(2) The application chain is the connection of the consortium chains via the cross-chain system. It can join the cross-chain system with a unique identity and interact with other application chains in the

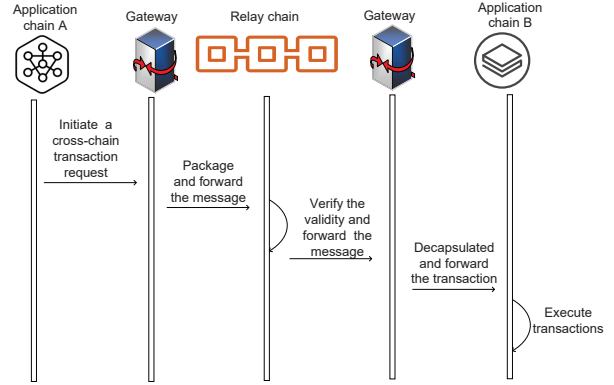


Fig. 1 Architecture model of cross-chain system.

cross-chain network. A cross-chain contract is deployed on the application chain to execute the cross-chain events.

(3) The cross-chain gateway is responsible for the monitoring, routing, proxy forwarding, and so on. The gateway submits the cross-chain transactions to the relay chain.

3.2 Identity registration process

To secure cross-chain transactions, each application chain obtains the digital identifier (DID) through execution of an identity registration contract. The registration process of a cross-chain DID is shown in Fig. 2.

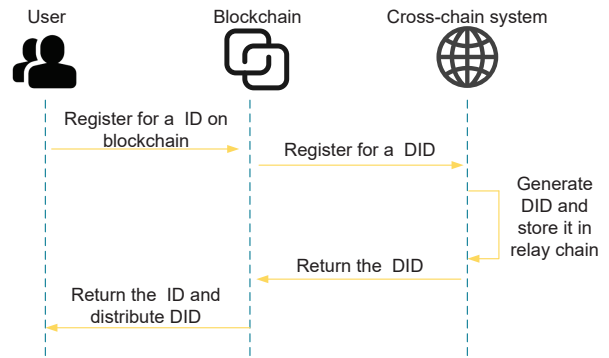


Fig. 2 Registration process of cross-chain DID.

DID (Zhong et al., 2021) is a type of decentralized identifier that belongs to Self-Sovereign Identity. Blockchain makes identity management decentralized, tamper-resistant, cost-effective, and controllable for users. Current architectures and applications of DID are mainly based on blockchain. The application chain sends the data (public key and transaction address) to the relay chain for cross-chain

identity registration. Registration proposal is valid after it passes the voting of relay chain nodes. The application chain can participate in the cross-chain system after obtaining the DID.

3.3 Authentication model

In the field of smart education, blockchain can be applied in the identity management of academics, teachers, and graduates to ensure the validity of education data due to the features of distributed data storage, peer-to-peer transmission, tamper-proofing and consensus confirmation. Usually, each user needs to register their identity once in different education institutions, but the users have multiple accounts in multiple blockchain systems. Leakage of unified and trusted digital identities in education will greatly increase the service cost of the application chain. A cross-chain mechanism can exchange and circulate the information and value between originally different blockchains using technical means, and can manage the trust and authentication between different blockchain systems in multi-chain scenarios.

The DGS-AQCCIDAA-based cross-chain identity authentication for smart education is shown in Fig. 3. This interactive process contains three entities: the user set, application chain, and relay chain. The model details in Fig. 3 are as follows.

(1) The user set is a collection of users involved in the smart education system, and includes the graduates, teachers, and other staff.

(2) The relay chain completes the creation of the group, generates the group public key and group private key, and publishes the group public key to all group members. The relay chain manages the group members by being responsible for the registration and revocation of group members. Entities in the cross-chain system need to request a group certificate from the relay chain for anonymous authentication.

(3) The application chain is applied in the identity management of the user set. The user uploads the data into the application chain. When cross-chain authentication is performed, the application chain nodes apply to join the group and interact with each other.

4 DGS-AQCCIDAA

Relay chain nodes act as the group managers to create the group and each application chain node acts as a group member. The DGS-AQCCIDAA algorithm is described in the following subsections.

4.1 Setup

The parameters $(1^n, 1^N)$ are inputted and the group manager outputs the system parameters, where n is the security parameter and N is the maximum number of group members. The parameters of DGS-AQCCIDAA are listed in Table 2.

Table 2 Parameters of DGS-AQCCIDAA

Parameter	Value or asymptotic bound
m	$m = 6n^{1+\delta}$
p	$p = m^4 \cdot \omega(\log^{1.5} m)$
q	$q = m^{2.5} \cdot \max(m^6 \cdot \omega(\log^{2.5} m), 4N)$
α	$\alpha = 2\sqrt{m}$
β	$\beta = m^{1.5} \cdot \omega(\log^{1.5} m)$
s	$s = m \cdot \omega(\log m)$
η	$\eta = m^2 \cdot \omega(\log^{1.5} m)$
δ	$n^{1+\delta} > \lceil (n+1) \log q + n \rceil$
t	$t = \omega(\log m)$
H	$H : \{0, 1\}^* \rightarrow \{0, 1\}^t$

The group manager selects a positive integer m , two primes $p, q \in \mathbb{Z}$, $s, \alpha, \beta, \eta, \delta \in \mathbb{R}$, $\mathbf{A}_0, \mathbf{A}_1 \leftarrow_R \mathbb{Z}_q^{n \times m}$, and a secure hash function H . The group manager publishes the system global parameter set as follows: $\phi = \{n, N, m, q, s, p, \alpha, \beta, \eta, \mathbf{A}_0, \mathbf{A}_1, H\}$.

4.2 KeyGen

Algorithm details concerning the key generation are as follows.

(1) $\text{KeyGen}_{\text{GM}}(\phi)$: The group manager generates $(\mathbf{A}, \mathbf{T}_{\mathbf{A}}) \leftarrow \text{TrapGen}(n, m, q)$ and $(\mathbf{B}, \mathbf{T}_{\mathbf{B}}) \leftarrow \text{SuperSamp}(n, m, q, \mathbf{A}, \mathbf{0})$. The master private key of the group manager is $\text{msk} = \mathbf{T}_{\mathbf{A}}$, the master public key is $\text{mpk} = \mathbf{A}$, the trace private key is $\text{tsk} = \mathbf{T}_{\mathbf{B}}$, and the trace public key is $\text{tpk} = \mathbf{B}$.

(2) $\text{KeyGen}_{\text{Gm}}(\phi)$: The group member samples a short vector $\mathbf{r}_i \leftarrow D_{\sigma}^n$ on the lattice, selects $\mathbf{F} \leftarrow_R \mathbb{Z}_q^{m \times n}$ and calculates $\mathbf{u}_i = \mathbf{F}\mathbf{r}_i \pmod{q}$. The signature private key of the group member is $\text{usk} = \mathbf{s}_i$ and the public key is $\text{upk} = \mathbf{u}_i$.

It should be noted that the group public key is $\text{gpk} = (\mathbf{A}, \mathbf{B}, \mathbf{F}, \mathbf{u}_i)$.

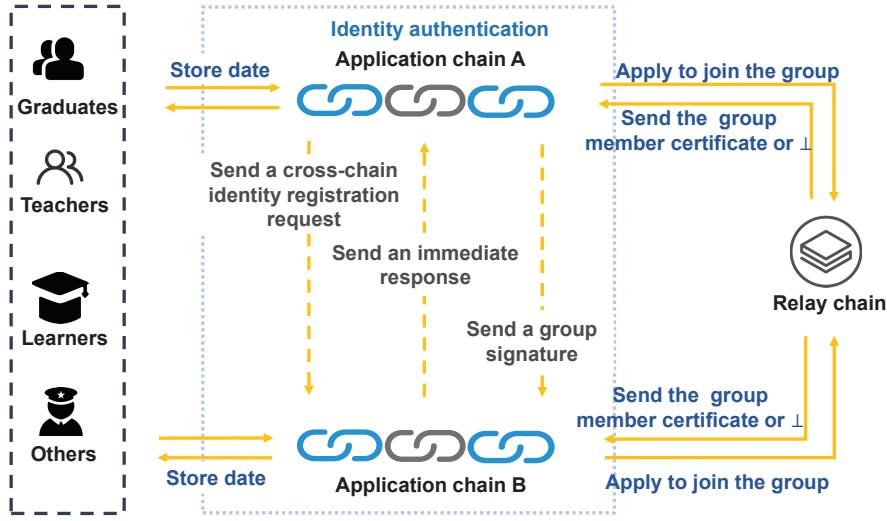


Fig. 3 DGS-AQCCIDAA-based cross-chain identity authentication model in smart education

4.3 Group member joining

The application chain sends $(DID, \mathbf{u}_i, \text{sig}(\mathbf{u}_i))$ to the group manager. The group manager verifies the validity of the signature using the public key information submitted by the application chain node during the identity registration to judge whether the node is a legitimate user in the cross-chain system and whether the node can join the group. If the identity of node is invalid or the DID is a group member, the joining process is terminated; otherwise the group manager carries out the following:

(1) For the DID, the group manager selects $i \in [1, N]$ to calculate $\bar{\mathbf{A}}_i = [\mathbf{A} \parallel \mathbf{A}_0 + i\mathbf{A}_1] \in \mathbb{Z}_q^{n \times 2m}$. The group manager generates $\mathbf{T}_{\bar{\mathbf{A}}_i} \leftarrow \text{ExtBasis}(\bar{\mathbf{A}}_i, \mathbf{T}_A, s)$, where $\mathbf{T}_{\bar{\mathbf{A}}_i} \in \mathbb{Z}_q^{m \times m}$ and $\|\tilde{\mathbf{T}}_{\bar{\mathbf{A}}_i}\| \leq s\sqrt{m}$.

(2) The group manager sets $\mathbf{w}_i = \mathbf{A}\mathbf{u}_i \pmod{q}$ and generates $(\mathbf{x}_0, \mathbf{x}_1) \leftarrow \text{SamplePre}(\bar{\mathbf{A}}_i, \mathbf{T}_{\bar{\mathbf{A}}_i}, \beta, \mathbf{w}_i)$, where $(\mathbf{x}_0, \mathbf{x}_1) \in D_{\mathbb{Z}^{2m}, \beta}$. $\text{Tag}_i = \mathbf{A}_0\mathbf{u}_i \pmod{q} \in \mathbb{Z}_q^n$ is the revocation tag of the group member.

(3) The group manager sends $\text{Cert}_i = (i, \mathbf{x}_0, \mathbf{x}_1, \mathbf{w}_i, \text{Tag}_i)$ to the application chain node via a secure channel. The group manager updates $\text{gpk} = (\mathbf{A}, \mathbf{B}, \mathbf{F}, \mathbf{u}_i, \mathbf{w}_i)$.

4.4 Group member revocation algorithm

The algorithm details for group member revocation are as follows.

(1) $\text{Revoke}_{\text{GM}}$: The group manager adds Tag_i to

the revocation list RL. If the revocation is successful, this algorithm returns 1 and 0 otherwise.

(2) $\text{Revoke}_{\text{GM}}$: The group member sends $(\text{Tag}_i, \mathbf{u}_i, \text{sig}(\mathbf{u}_i))$ to the group manager. If the identity of the group member is valid, the group administrator adds Tag_i to the revocation list RL. If the revocation is successful, this algorithm returns 1 and 0 otherwise.

4.5 Group signature

Input $(\text{gpk}, \text{usk}, \text{Cert}_i, m)$, this group algorithm carries out the following:

(1) The group member selects $\mathbf{s} \leftarrow_R \mathbb{Z}_q^n$, $\mathbf{e}_0 \leftarrow_R \chi_\alpha$, and calculates $\mathbf{c}_0 = \mathbf{B}^T \mathbf{s} + p\mathbf{e}_0 + \mathbf{x}_0$ to generate a proof π_0 about $(\mathbf{s}, \mathbf{e}_0, \mathbf{x}_0)$ such that $(\mathbf{B}, \mathbf{c}_0, \eta; \mathbf{s}, \mathbf{e}_0, \mathbf{x}_0) \in R_{\text{eLWE}}$.

(2) The group member selects $\mathbf{e}_i \leftarrow_R \chi_\alpha$ and calculates $\mathbf{c}_1 = \mathbf{B}^T \text{Tag}_i + \mathbf{e}_i$ to produce a proof π_1 about $(\text{Tag}_i, \mathbf{e}_i)$ such that $(\mathbf{B}, \mathbf{c}_1, \alpha; \text{Tag}_i, \mathbf{e}_i) \in R_{\text{LWE}}$.

(3) The group member produces a proof π_2 about \mathbf{r}_i , such that $(\mathbf{F}, \mathbf{u}_i, \beta; \mathbf{r}_i) \in R_{\text{ISIS}}$.

(4) Let $\bar{\beta} = \lfloor \beta \rfloor$, $l = \lceil \log_{\bar{\beta}} N \rceil$, $\mathbf{b} = \mathbf{A}_1 \mathbf{x}_1$, $\mathbf{y}_0 = \mathbf{e}_i$, $\mathbf{y}_1 = \mathbf{x}_0$, $\mathbf{y}_2 = \mathbf{v}_i$, $\mathbf{v}_i = (\mathbf{v}_0, \dots, \mathbf{v}_{l-1}) \in \mathbb{Z}_{\bar{\beta}}^l$, and $D = (\mathbf{b}, \bar{\beta}\mathbf{b}, \dots, \bar{\beta}^{l-1}\mathbf{b}) \in \mathbb{Z}_q^{n \times l}$, the group member generates a proof π_3 about $(\mathbf{y}_0, \mathbf{y}_1, \mathbf{y}_2)$ such that:

$$R_{\text{Com}} = \left\{ \begin{array}{l} (A, D, \mathbf{u}_0, \mathbf{u}_1, \eta; \mathbf{y}_0, \mathbf{y}_1, \mathbf{y}_2) \in \mathbb{Z}_q^{n \times m}, \\ \mathbb{Z}_q^{n \times l}, \mathbb{Z}_q^n, \mathbb{Z}_q^m, \mathbb{R}, \mathbb{Z}_q^m, \mathbb{Z}_q^m, \mathbb{Z}_q^l : \\ \mathbf{t}_0 = p\mathbf{A}\mathbf{y}_0 - D\mathbf{y}_2, \\ \mathbf{t}_1 = p\mathbf{A}\mathbf{y}_0 + \mathbf{A}\mathbf{y}_1, \mathbf{y}_j < \eta, j = 0, 1, 2 \end{array} \right\}, \quad (7)$$

where Com is a promise message, and $H(\mathbf{x}_1, \pi_0, \pi_1, \pi_2, m, \text{Com})$ is the challenge of π_3 . Protocol π_3 with a single-bit challenge is as shown in Fig. 4.

Group member finally outputs the signature $\Sigma = (\mathbf{c}_0, \mathbf{c}_1, \mathbf{x}_1, \pi_0, \pi_1, \pi_2, \pi_3)$ to the verifier.

4.6 Verify

$\text{GVerify}(\text{gpk}, m, \Sigma, \text{RL}) \rightarrow 0/1$: The verifier first checks the validity of RL. For $\text{Tag}_i \in \text{RL}$, the verifier calculates $\mathbf{e}'_i = \mathbf{c}_1 - \mathbf{B}^T \text{Tag}_i$. If $\|\mathbf{e}'_i\| \leq \alpha q \sqrt{m}$, the user identity i has been revoked and the signature is rejected. Otherwise, the verifier checks the validity of $\pi_0 \sim \pi_3$, $\|\mathbf{x}_1\| \leq \beta \sqrt{m}$ and $\mathbf{A}_1 \mathbf{x}_1 \neq \mathbf{0}$. The verifier outputs 1 if the signature is legal and 0 otherwise.

4.7 Open signature

$\text{Gopen}(\text{gpk}, \text{gtsk}, \Sigma) \rightarrow i$: The group manager obtains \mathbf{c}_0 using \mathbf{T}_B and calculates $\mathbf{z}_1 = \mathbf{A}_1 \mathbf{x}_1$, $\mathbf{z}_2 = \mathbf{A} \mathbf{x}_0 + \mathbf{A}_0 \mathbf{x}_1$. If $\mathbf{z}_1 \neq \mathbf{0}$ and $\exists i \in [1, N]$ satisfying $\mathbf{z}_2 + i\mathbf{z}_1 = \mathbf{w}_i$, the group manager i and \perp otherwise.

5 Correctness analysis

The analysis of DGS-AQCCIDAA for correctness is as follows.

5.1 Correctness of group signature algorithm

According to $\beta = s\sqrt{2m} \cdot \omega(\sqrt{\log 2m}) \geq \|\tilde{\mathbf{T}}_{\mathbf{A}_i}\| \cdot \omega(\sqrt{\log 2m})$, $\mathbf{x}_0, \mathbf{x}_1 \in D_{\mathbb{Z}^m, \beta}$, $\|\mathbf{x}_j\| \leq \beta \sqrt{m}$ ($j \in \{0, 1\}$), $\|\mathbf{e}_k\| \leq \alpha q \sqrt{m}$, ($k \in \{0, 1, \dots, N\}$), and $\eta = \max(\beta, \alpha q \sqrt{m})$, the signature algorithms can generate $\mathbf{c}_0, \mathbf{c}_1$ and NIZKP $\pi_0 \sim \pi_3$. Because $\mathbf{x}_1 \in D_{\mathbb{Z}^m, \beta}$, $\Pr[\mathbf{A}_1 \mathbf{x}_1 = \mathbf{0}] \leq O(q^{-n})$ and $\pi_0 \sim \pi_3$ is complete [12], $\Sigma = (\mathbf{c}_0, \mathbf{c}_1, \mathbf{x}_1, \pi_0, \pi_1, \pi_2, \pi_3)$ is shown to be correct.

5.2 Correctness of open signature algorithm

For DGS-AQCCIDAA, we know that $(\mathbf{T}_B^T) \mathbf{c}_0 = \mathbf{T}_B^T (p\mathbf{e}_0 + \mathbf{x}_0) \text{mod} q$, $\mathbf{T}_B \in \mathbb{Z}^{m \times m}$

is a full rank matrix, and $\mathbf{T}_B^T (p\mathbf{e}_0 + \mathbf{x}_0)_\infty \leq 3m^8 \omega(\log^{3.5} m) \leq q/2$. Therefore, we have $\mathbf{x}'_0 = p\mathbf{e}_0 + \mathbf{x}_0$ for Gaussian elimination.

Because $\beta = m^{1.5} \omega(\log^{1.5} m)$, $p = m^{2.5} \beta$, $\|\mathbf{x}_0\|_\infty \leq \|\mathbf{x}_0\| \leq p$, the group manager can obtain $\mathbf{x}_0 = \mathbf{x}'_0 \text{mod} p$. The group manager can calculate $\mathbf{w}_i = \bar{\mathbf{A}}_i(\mathbf{x}_0, \mathbf{x}_1) = \mathbf{A} \mathbf{x}_0 + (\mathbf{A}_0 + i\mathbf{A}_1) \mathbf{x}_1 = \mathbf{z}_2 + i\mathbf{z}_1$, and so successfully determine the user i .

6 Security analysis

DGS-AQCCIDAA also meets the CPA-anonymity and traceability requirements (Nguyen et al., 2015). The process of proving its security is as follows.

6.1 Anonymity

Theorem 1 If an adversary A can attack the CPA anonymity under chosen-plaintext attacks (CPA-anonymity) of DGS-AQCCIDAA with non-negligible advantage ε , there must exist a challenge algorithm Γ to solve the LWE problem.

Proof CPA-anonymity proof relies on two games G_0 and G_1 . Game G_0 is as follows.

(1) Γ obtains $\text{gpk} = (\mathbf{A}, \mathbf{B}, \mathbf{F}, \mathbf{u}_i, \mathbf{w}_i)$, $\text{usk} = \mathbf{r}_i$, $i \in [1, N]$, $\text{tsk} = \mathbf{T}_B$ and group member certificate Cert_i . Γ initializes the revocation list RL and the set U of corrupted users. Γ sends gpk to the adversary A .

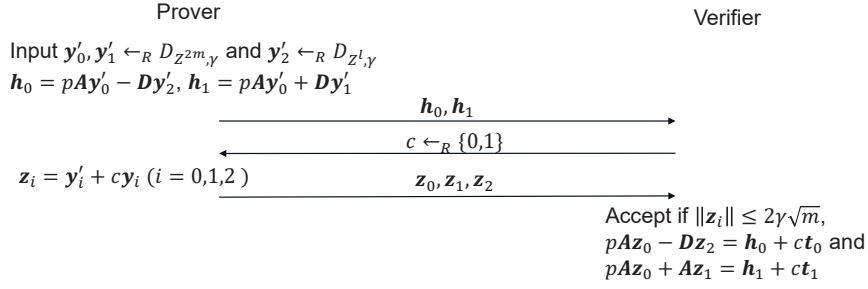
(2) A may issue an adaptive query about the signature of arbitrary message m to any group member, and Γ runs the group signature algorithm to answer it. A also issues a corruption query to group member i . Γ updates $U = U \cup \{i\}$ and returns Cert_i to A . For each revocation query to the group member i , Γ updates the revocation list $RL = RL \cup \{i\}$ and returns the Tag_i to A .

(3) A selects a message m^* and two identity identifiers $i_0, i_1 \in [1, N]$, where $i_b \notin U$ and $\text{Tag}_{i_b} \notin RL$ ($b \in \{0, 1\}$).

(4) Γ selects $b \leftarrow_R \{0, 1\}$, generates a legal signature $\Sigma = (\mathbf{c}_0, \mathbf{c}_1, \mathbf{x}_1, \pi_0, \pi_1, \pi_2, \pi_3)$, and then sends Σ to A .

Subsequently, A can do the same query as before, but A cannot query Cert_{i_b} and Tag_{i_b} , where $b \in \{0, 1\}$. Γ finally returns a guess b' about b to A .

Game G_1 is essentially same as G_0 , but with the following revision in Step 4. A simulated signature is used instead of a legal signature.

Fig. 4 Protocol π_3 with single-bit challenge

The simulated signature for message m^* is $\Sigma^* = (c_0^*, c_1^*, x_1^*, \pi_0^*, \pi_1^*, \pi_2^*, \pi_3^*)$, where:

(1) $(\pi_0^*, \pi_1^*, \pi_2^*, \pi_3^*)$ are generated by the NIZKP simulator $(\pi_0, \pi_1, \pi_2, \pi_3)$ are generated by random oracles in G_0 . Based on NIZKP, $(\pi_0^*, \pi_1^*, \pi_2^*, \pi_3^*)$ and $\pi_0, \pi_1, \pi_2, \pi_3$ are statistically close to each other.

(2) Γ chooses $\mathbf{x}_1^* \leftarrow_R D_{\mathbb{Z}^m, \beta}$. Based on the SamplePre $(\mathbf{A}, \mathbf{T}_A, \mathbf{u}, \sigma)$, \mathbf{x}_1^* and \mathbf{x}_1 chosen in G_1 and G_0 are statistically close.

(3) $\mathbf{g}_i \leftarrow_R \mathbb{Z}_q^n$. Γ computes $\mathbf{c}_1^* = B^T \mathbf{g}_i + \mathbf{e}_i$. Based on the LWE assumption, \mathbf{c}_1^* and \mathbf{c}_1 chosen in G_1 and G_0 are statistically indistinguishable.

(4) $\mathbf{d} \leftarrow_R \mathbb{Z}_q^m$. Γ computes $\mathbf{c}_0^* = \mathbf{d} + \mathbf{x}_0^*$. Based on the LWE assumption, \mathbf{c}_0^* and \mathbf{c}_0 chosen in G_1 and G_0 are statistically indistinguishable.

In summary, because G_1 is statistically indistinguishable from G_0 and Σ^* is independent from $b \in \{0,1\}$, the probability that $b' = b$ is close to $1/2$ (Nguyen et al., 2015), and the advantage that the adversary A wins in the game G_1 is negligible. Therefore, DGS-AQCBCIDAA has CPA-anonymity under the LWE assumption.

6.2 Full traceability

Theorem 2 If an adversary A can attack the traceability of DGS-AQCBCIDAA with non-negligible advantage ε , there must exist a challenge algorithm C to solve the ISIS problem.

Proof Given a matrix $\mathbf{A} \in \mathbb{Z}_q^{n \times m}$ and a vector $\mathbf{u} \in \mathbb{Z}_q^n$, a non-zero vector $\mathbf{x} \in \mathbb{Z}_q^m$ can be found to satisfy $\|\mathbf{x}\| \leq \text{poly}(m)$ and $\mathbf{A}\mathbf{x} = \mathbf{u} \pmod{q}$. C is required to perform the following action: C selects $R \leftarrow_R \{-1,1\}^m$ and a integer $i^* \leftarrow_R [-4m^{2.5}N + 1, 4m^{2.5}N - 1]$, and obtains $(\mathbf{A}, \mathbf{T}_A) \leftarrow \text{TrapGen}(n, m, q)$, and $(\mathbf{B}, \mathbf{T}_B) \leftarrow \text{SuperSamp}(n, m, q, \mathbf{A}, 0)$. Then, C chooses $\mathbf{F} \leftarrow_R \mathbb{Z}_q^{n \times m}$, samples $\mathbf{r}_i \leftarrow D_\sigma^n$ and computes

$\mathbf{u}_i = \mathbf{F}\mathbf{r}_i \pmod{q}$ and $\mathbf{w}_i = \mathbf{A}\mathbf{x}_0 + \mathbf{A}_0\mathbf{x}_1 + i^* \mathbf{A}_1\mathbf{x}_1$. C sets $\text{RL} = \emptyset$ and $U = \emptyset$.

C calculates the following answers for all $i \in [1, N]$ and $i \neq i^*$.

(1) C calculates $\bar{\mathbf{A}}_i = [\mathbf{A} \parallel \mathbf{A}_0 + i\mathbf{A}_1] = [\mathbf{A} \parallel \mathbf{A}\mathbf{R} + (i - i^*)\mathbf{A}_1]$ and obtains $\mathbf{T}_{\bar{\mathbf{A}}_i} \leftarrow \text{ExtBasis}(\bar{\mathbf{A}}_i, \mathbf{T}_A, s)$.

(2) C calculates $\text{Tag}_i = \mathbf{A}_0\mathbf{u}_i \pmod{q}$ and sends it to A . Here, $\text{gpk} \leftarrow (\mathbf{A}, \mathbf{B}, \mathbf{F}, \mathbf{u}_i, \mathbf{w}_i)$ and Tag_i are statistically close to the real scenario. A cannot know i^* . C sends $(\text{gpk}, \text{Tag}_i)$ to A .

Queries: after C receives a corruption query about i from A , C stops and aborts if $i = i^*$ or $i \notin [1, N]$. Otherwise C sets $U = U \cup \{i\}$ and sends \mathbf{z}_i to A .

A issues a signature query about group member i and message m to a random oracle. Then, A sends the signature to C . If $i \notin [1, N]$, C rejects the signature; if $i = i^*$, C uses the NIZKP simulator to generate $\pi_0^* \sim \pi_3^*$ and sends new signature to A . Otherwise, C sends a $\Sigma = (c_0, c_1, \mathbf{x}_1, \pi_0, \pi_1, \pi_2, \pi_3)$ to A as a signature of i .

Forgery phase: A returns a message m^* , a set RL^* of revocation lists and a forged signature $\Sigma^* = (c_0^*, c_1^*, x_1^*, \pi_0^*, \pi_1^*, \pi_2^*, \pi_3^*)$ with the probability ε . Running the tracing algorithm will cause tracing failure or output an identity index $i \in U \setminus \text{RL}^*$. $i \in U \setminus \text{RL}^*$ indicates the set of users in the corruption list but not in the forged revocation list RL^* .

C extracts $\mathbf{x}_0^*, \mathbf{x}_1^*$ and the success probability of extraction is at least $\varepsilon(\varepsilon/q_h - 2^{-t})$ (Bellare and Neven, 2006), where q_h is the maximum number of times that A accesses the hash function. Consider two cases:

(1) If $i \neq i^*$, C aborts and fails. The probability of $i \neq i^*$ is at most $(8m^{2.5} - 1) / 8m^{2.5}N$.

(2) $[\mathbf{A} \parallel \mathbf{A}\mathbf{R} + (i - i^*)\mathbf{A}_1] (\mathbf{x}_0^*, \mathbf{x}_1^*) = \mathbf{A}\mathbf{x}_0^* +$

$AR\mathbf{x}_1^* = \mathbf{w}_i = \mathbf{A}\mathbf{u}_i$ while $i = i^*$, where $i \leq 4\eta m^2$. Then, $\mathbf{x} = \mathbf{x}_0^* + R\mathbf{x}_1^*$ is the ISIS problem solution. Because $i^* \leftarrow_R [-4m^{2.5}N + 1, 4m^{2.5}N - 1]$, the probability of $i = i^*$ is at least $1/8m^{2.5}N$, then the probability that C can solve the ISIS problem is at least $\varepsilon(\varepsilon/q_h - 2^{-t})/8m^{2.5}N$.

Based on above description, DGS-AQCCIDAA satisfies the full traceability under the ISIS assumption.

7 Performance analysis

In this section, we analyze the performance of DGS-AQCCIDAA and existing group signatures ((Li et al., 2019; Libert et al., 2016; Ling et al., 2017). Experiment environment: the processor is Intel(R) Core(TM) i5-1135G7 @ 2.40GHz; OS is 64-bit windows 10.

Table 3 lists the average running time for cryptographic operations. The PBC library is called to calculate the average time cost of each cryptographic operation. In the simulation experiments, the lattice dimension m is set to 1000 for sufficient security of cryptographic schemes, and n is selected such that $m \geq 5n \log q$. Because the generation of large prime numbers is random, we obtain an average result by multiple experiments.

Table 3 Average time of cryptographic operations

Operation types	Time (ms)
A hash function	$1T_H = 11.69$
A Gaussian sampling algorithm	$1T_G = 23.03$
A matrix or vector multiplication operation	$1T_{MV} = 8.32$
A polynomial modular multiplication operation	$1T_{PM} = 3.94$
A matrix or vector addition operation	$1T_{PA} = 1.32$

A performance comparison of several schemes are shown in Table 4, where n is the security parameter, N is the number of group members, $q \in \mathbb{Z}$ is the modulus, and $t = \omega(\log m)$ ($m = 6n^{1+\delta}$) is the number of interactions between the prover and verifier in the zero-knowledge proof π_3 . According to Table 4, the public and private key sizes are small and independent of N in DGS-AQCCIDAA. Compared with Libert et al. (2016), the revocation function is achieved in DGS-AQCCIDAA and the implementation of the VLR mechanism is simple. Compared with Li et al. (2019), the process of group members access and revocation requires interaction with a turing machine in the Li et al. (2019), which com-

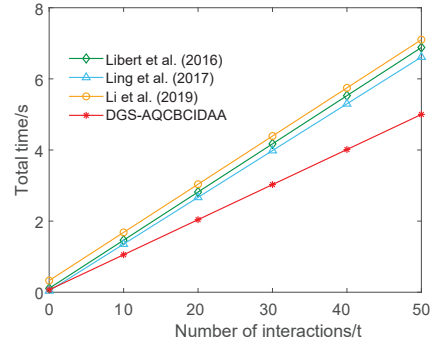


Fig. 5 Total times comparison of several schemes

plicates the process of identity authentication. In addition, Libert et al. (2016), Ling et al. (2017), and Li et al. (2019) use the Stern-type protocol for the authentication. Soundness error of single bit schemes in Libert et al. (2016), Ling et al. (2017), and Li et al. (2019) is $2/3$, but the soundness error of DGS-AQCCIDAA is just $1/2$, where the soundness error is the probability of a malicious prover convincing an honest verifier that a false statement is true.

Table 5 shows a comparison of the characteristics of DGS-AQCCIDAA and other cross-chain authentication schemes of Wang et al. (2022a), Shao et al. (2021), and Wang et al. (2022b). Compared to other schemes, DGS-AQCCIDAA does not have a single point of failure and can realize anonymous authentication to protect the privacy of users, so our scheme is more flexible in user identity management.

MATLAB software is used to manage the simulation experiments, where t is the number of interactions between the prover and verifier in the NIZKP π_3 . Fig. 5 shows that, with the increasing of t , the time cost of total time increases linearly. But increasing of DGS-AQCCIDAA is slowest. To sum up, our DGS-AQCCIDAA has lower calculation overhead than the schemes of Libert et al. (2016), Ling et al. (2017), and Li et al. (2019).

8 Summary

We propose a security model based on DGS that is well adapted to cross-blockchain services and identity authentication. The relay chain administrator node acts as the group manager, which meets the privacy protection requirements of the relay chain. Our scheme meets the identity authentication requirement of the application chain in a cross-chain system. In addition, DGS-AQCCIDAA has no frame attack

Table 4 Performance comparison of several schemes

Schemes	Public key size	Private key size	Signature size	Total time cost	Revocation model
Libert et al. (2016)	$O(mn \log N \log q)$	$O(m)$	$O(tm \log q)$	$(9t + 9)T_{MV} + (11t + 8)T_{PA} + 2tT_G + 2T_H$	/
Ling et al. (2017)	$O(mn \log N \log q)$	$O(mn \log N \log q)$	$O(tm \log N \log q \log \beta)$	$(9t + 3)T_{MV} + (8t + 1)T_{PA} + 2tT_G + T_H$	Merkle tree
Li et al. (2019)	$O(mn \log q)$	$O(m)$	$O(tm \log q)$	$(9t + 10)T_{MV} + (11t + 10)T_{PA} + (2t + 7)T_G + 6T_H$	VLR
DGS-AQCBCIDAA	$O(mn \log q)$	$O(m)$	$O(tm \log q)$	$(6t + 6)T_{MV} + (7t + 5)T_{PA} + 2tT_G + T_H$	VLR

Table 5 Characteristics comparison of several schemes

Schemes	Cross-chain mechanism	Single point of failure	Protection of identity privacy	Anonymous authentication	Anti-quantum attacks	Revocation of identity
Wang et al. (2022a)	Relay	×	×	×	×	×
Shao et al. (2021)	Notary	✓	×	×	×	×
Wang et al. (2022b)	Relay	×	×	×	×	×
DGS-AQCBCIDAA	Relay	×	✓	✓	✓	✓

because the private key of user i is a short vector \mathbf{r}_i generated by a Gaussian sampling algorithm and the public key is $\mathbf{u}_i = \mathbf{F}\mathbf{r}_i \pmod{q}$ ($\mathbf{F} \leftarrow_{\mathbb{R}} \mathbb{Z}_q^{m \times n}$). If the group manager or colluded group member wants to forge a signature for i , they must to generate a NIZKP π_2 . Because of the reliability of π_2 , the group manager or colluded group member does not know \mathbf{r}_i and therefore cannot generate a π_2 .

Contributors

Huifang YU designed the research. Huifang YU and Mengjie HUANG drafted and revised the paper.

Conflict of interest

Huifang YU and Mengjie HUANG declare that they have no conflict of interest.

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