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Hierarchical algorithm for large-scale irregular packing problems

Key words: Large-scale packing; Hierarchical algorithm; Box stacking; Shape matching; Gravity packing; Principle of minimum potential energy

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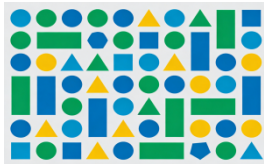
 ORCID: <http://orcid.org/0000-0003-2975-4749>

Problem & Challenges

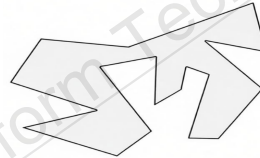
The Packing Problem:

Arrange parts on raw materials to maximize material utilization

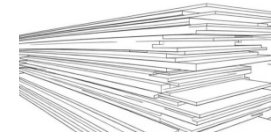
Industry Challenge: Large-scale manufacturing



Large Quantity of Parts



Complex geometries



Multiple Sheets

Research Gap:

- Existing studies: ≤ 450 parts, single sheet
- No integrated solution for large-scale irregular packing

Core Innovation: Hierarchical Classification

Key Insight: Not all parts should be packed the same way!

Three-Level Classification:

Level	Part Type	Criteria	Primary Strategy
1	Large Rectangular	$\text{Area} \geq 0.5 \text{ m}^2, C_b > 0.9$	Box Stacking
2	Large Irregular + Medium	$0.05 \text{ m}^2 \leq \text{Area} < 0.5 \text{ m}^2$	Shape Matching
3	Small + Failed	$\text{Area} < 0.05 \text{ m}^2$	Shape Matching \rightarrow Gravity



$C_b = 0.97$



$C_b = 0.923$



$C_b = 0.81$



$C_b = 0.766$



$C_b = 0.612$



$C_b = 0.607$



$C_b = 0.4997$



$C_b = 0.424$



$C_b = 0.39$

Block Coefficient C_b = Outer domain Area/Bounding Box Area
(measures "fullness")

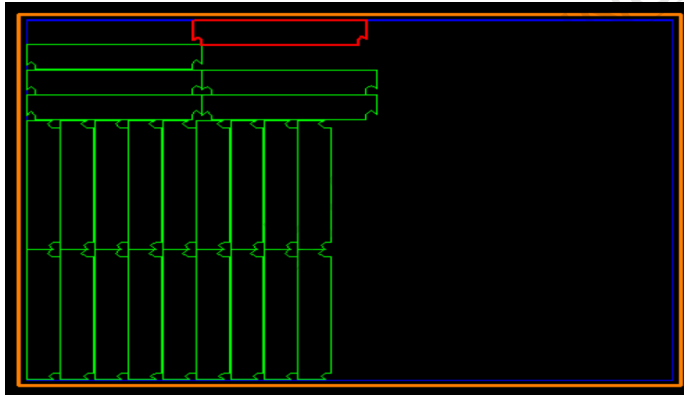
The Problem with Gravity Packing

Gravity Packing (HAPE):

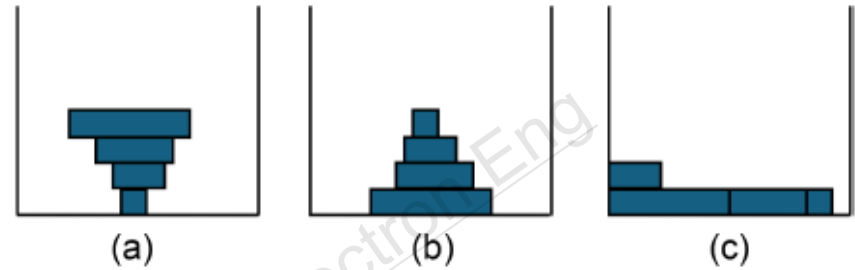
- Based on principle of minimum potential energy
- Parts seek the lowest center of gravity

The Hooking Problem:

- Local interlocking between adjacent parts
- Disorderly layout
- Sacrifices global efficiency for local optimization



Hooking of box parts caused by gravity packing (assuming that gravity is directed horizontally leftward)



Gravity packing (gravity directed vertically downward): (a) unstable (high center of gravity); (b) relatively stable (lower center of gravity); (c) the most stable (the lowest center of gravity)



Traffic congestion from cutting in line

Box Stacking (Level-1)

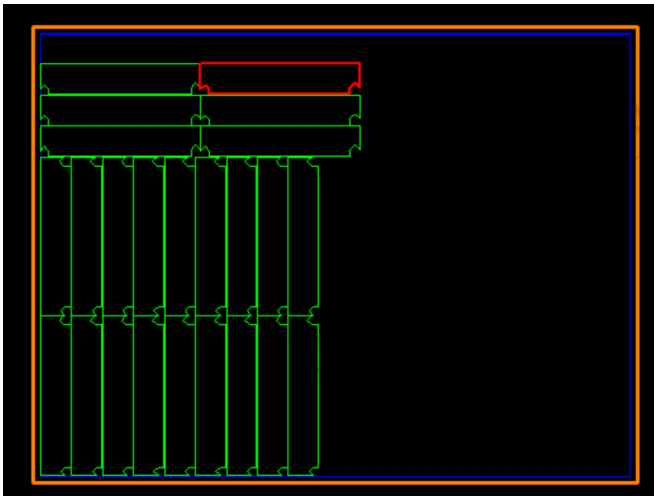
Purpose: Solve hooking for rectangular parts ($C_b > 0.9$)

Method: Align bounding box corners \rightarrow essentially **rectangular packing**

Process:

1. Align corners (bottom-left with bottom-right, etc.)
2. Check conflicts
3. Try all rotations (0° , 90° , 180° , 270°)
4. Select attitude with the smallest x coordinate of centroid

Result: Clean, orderly arrangement without hooking



Box stacking can avoid mutual hooking of box parts



Compliance with traffic rules

Shape Matching (Level-2&3)–the novel contribution

What it does: Two similar parts achieve **contour complementarity** through rotation and sliding



Why it matters:

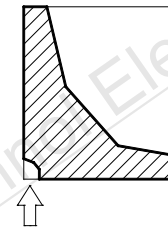
- Creates tighter packing
- Frees space for additional parts
- Prioritizes utilization over pure physics

Shape Matching Coefficient (SMC):

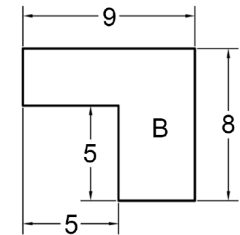
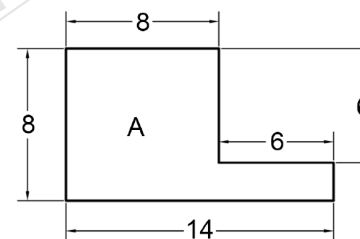
$$\text{SMC} = \frac{\text{detArea}}{\text{blankArea}} \times 100\%$$

- detArea:** Reduction in bounding box area
- blankArea:** Total blank area = $A_b(1 - C_b)$

The blank areas of parts A and B are 36 mm² and 25 mm², respectively, and their sum blankArea = 61 mm². After shape matching, the reduction in the parts' bounding box area detArea = 6 × 8 = 48 mm². SMC = 48/61 = 78.7%.

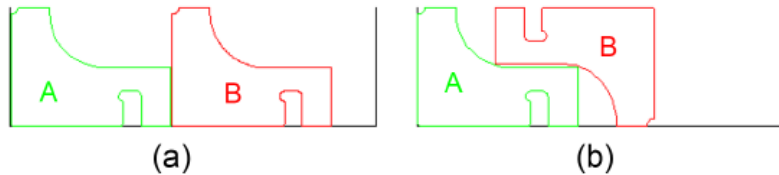


Part bounding box and its blank area



Threshold: SMC_min = 0.25 (fallback to Gravity if below)

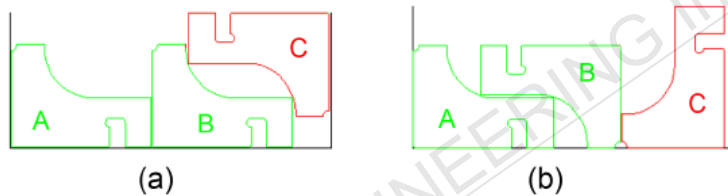
Shape Matching vs. Gravity–Demonstration 1



Two Parts:

- Gravity: Lower center, less efficient
- Shape Matching: Higher center, **more space freed**

Two-part packing (gravity directed downward):
(a) gravity packing; (b) shape matching

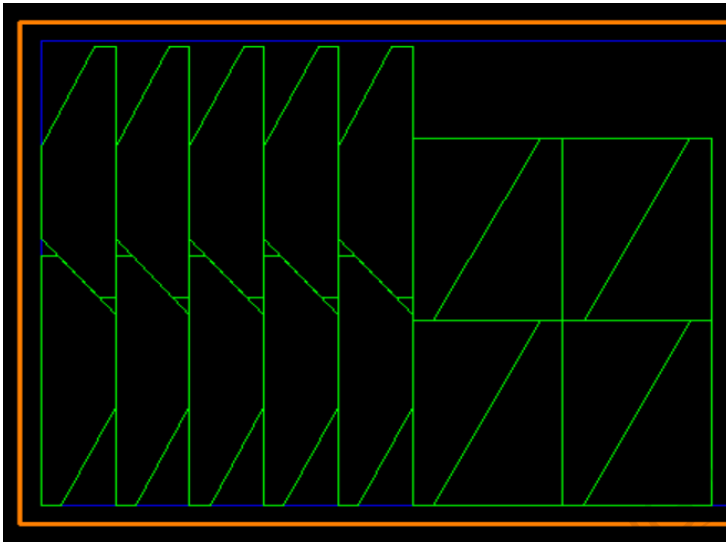


Three Parts:

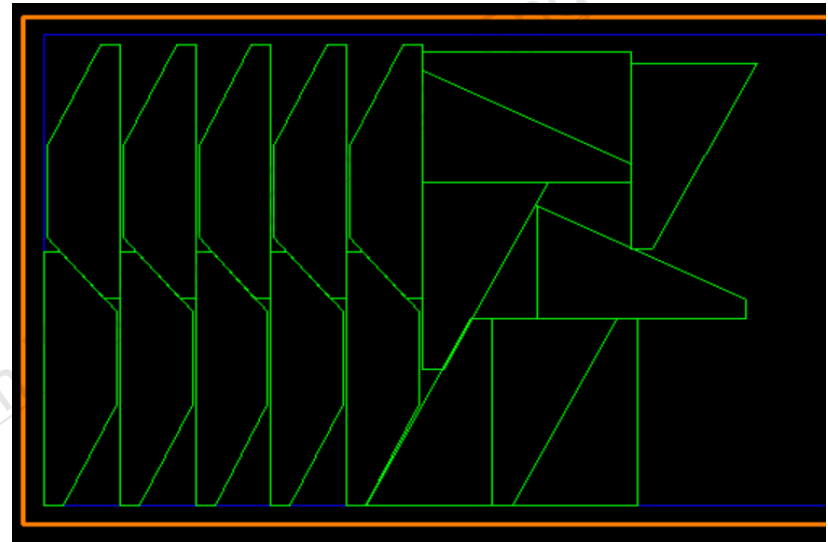
Shape matching frees bottom-right corner for Part C → better overall density

Three-part packing (gravity directed downward):
(a) gravity packing; (b) shape matching

Shape Matching vs. Gravity–Demonstration 2



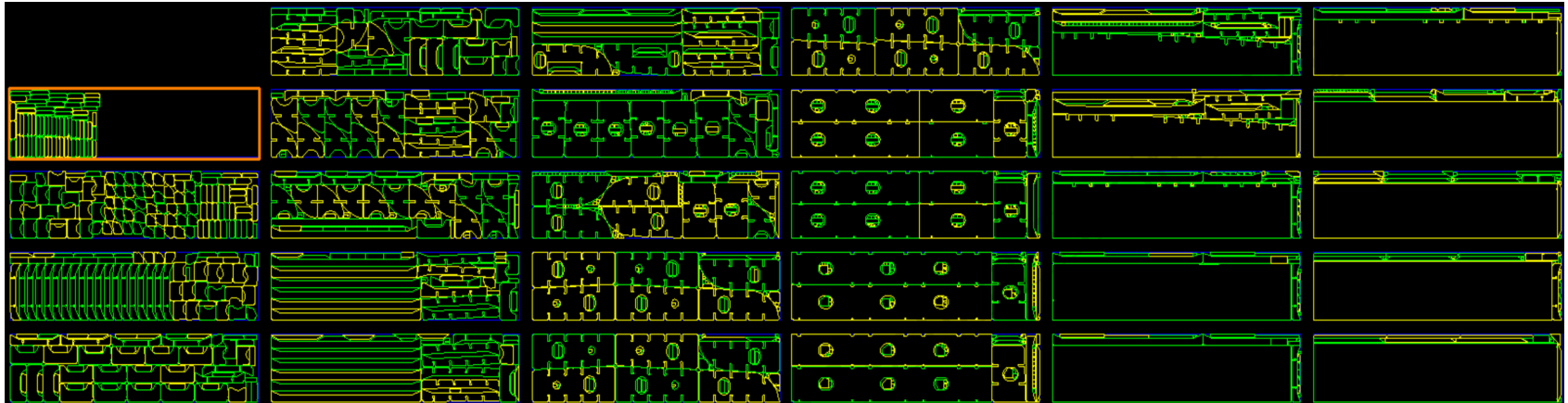
Shape Matching
(Packing density = 80.89%)



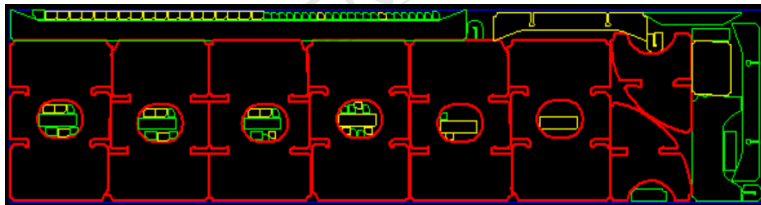
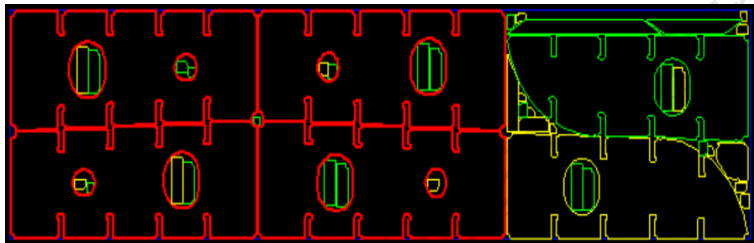
Gravity Packing
(Packing density = 74.16%)

Experimental Results

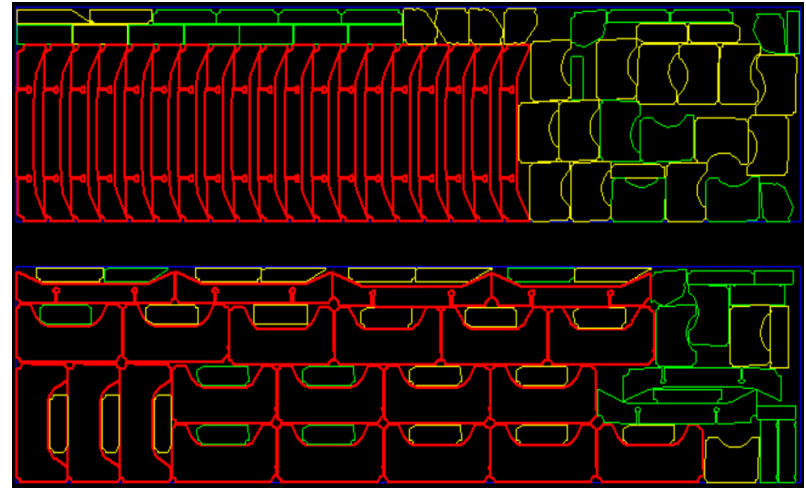
Experiment 1: Shipbuilding (1400 parts, 29 sheets, Computation time = 157.39 s)



Multi-plate hierarchical packing (global view)



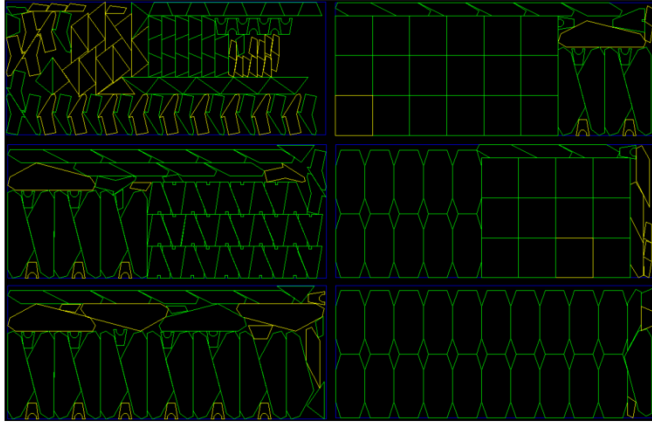
(a) Shape Matching (local view)



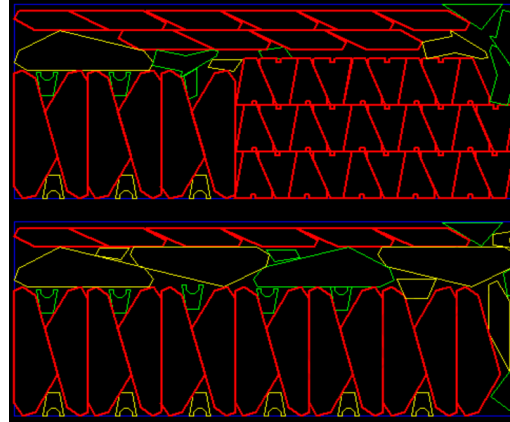
(b) Box Stacking (local view)

Experimental Results

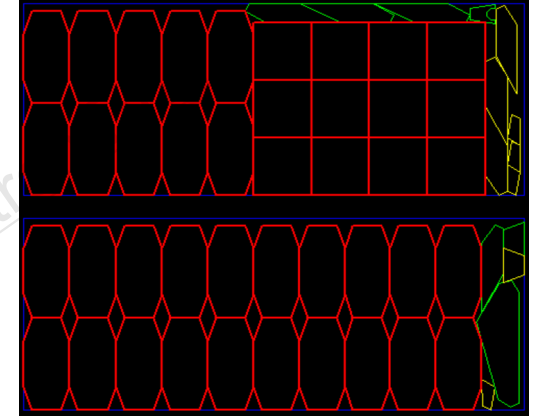
Experiment 2: Benchmarks (DAGLIx10, Marquesx10)



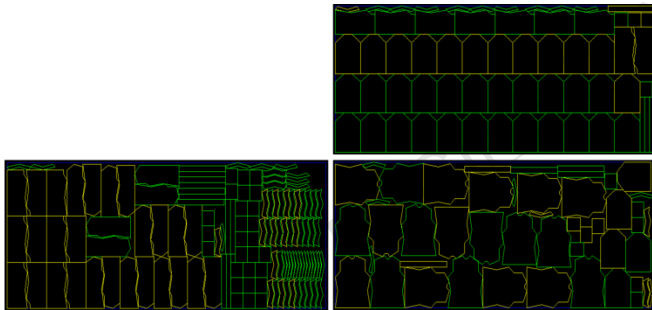
Hierarchical Packing (global view, DAGLIx10), where the number of parts=300 and computation time=1.23 s



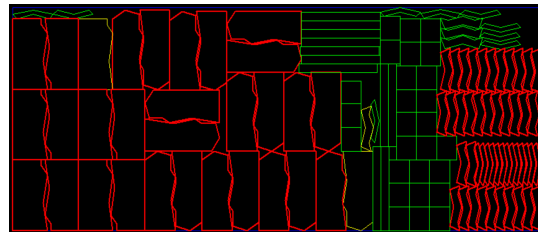
(a) Shape Matching (local view)



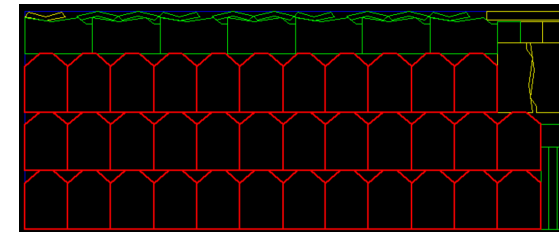
(b) Box Stacking (local view)



Hierarchical Packing (global view, Marquesx10), where the number of parts=240 and computation time=0.81 s



(a) Shape Matching (local view)



(b) Box Stacking (local view)

Conclusions

Key Contributions:

1. **Hierarchical algorithm:** handling 1400+ irregular parts across multiple sheets
2. **Shape Matching (novel):** Achieves contour complementarity for higher utilization
3. **Box Stacking:** Eliminates hooking for rectangular parts
4. **Systematic enhancement:** Gravity packing as fallback, not replacement

Benefits:

- Higher material utilization
- Faster computation (Box Stacking = rectangle packing speed)
- Practical for real engineering (5.43 s/plate)

The program and experiment data can be downloaded from the following website:

<http://www.huagongchuanhai.cn/packing/HierarchicalPacking.rar>



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