

Rasha SHOITAN, Zaki NOSSAIR, I. I. IBRAHIM, Ahmed TOBAL 2018.  
Improving the reconstruction efficiency of sparsity adaptive matching pursuit based on the Wilkinson matrix. *Frontiers of Information Technology & Electronic Engineering*, 19(4):503-512. <https://doi.org/10.1631/FITEE.1601588>

# Improving the reconstruction efficiency of sparsity adaptive matching pursuit based on the Wilkinson matrix

**Keywords:** Block compressive sensing; Sparsity adaptive matching pursuit; Greedy algorithm; Wilkinson matrix

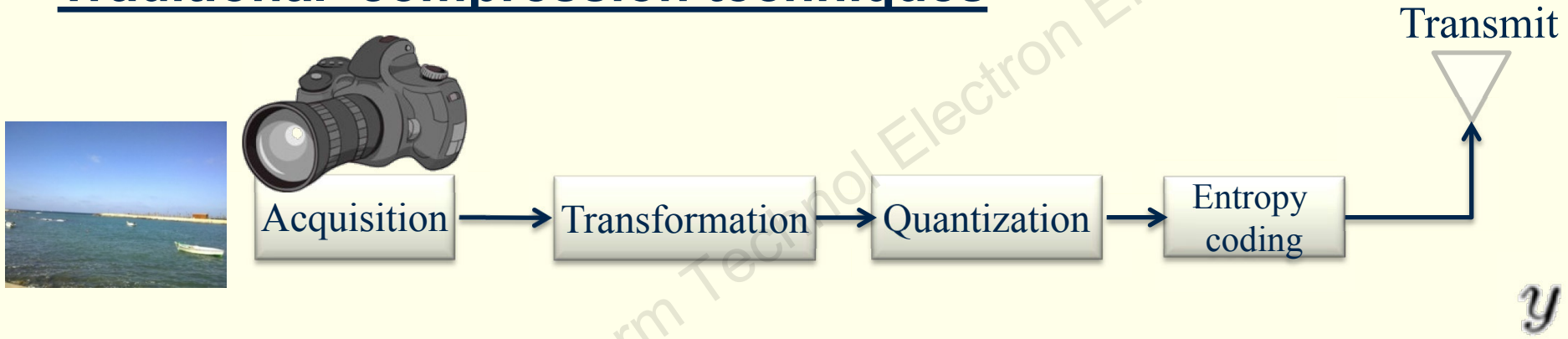
Corresponding author: Rasha SHOITAN

E-mail: [Rasha.shoitan@eri.sci.eg](mailto:Rasha.shoitan@eri.sci.eg)

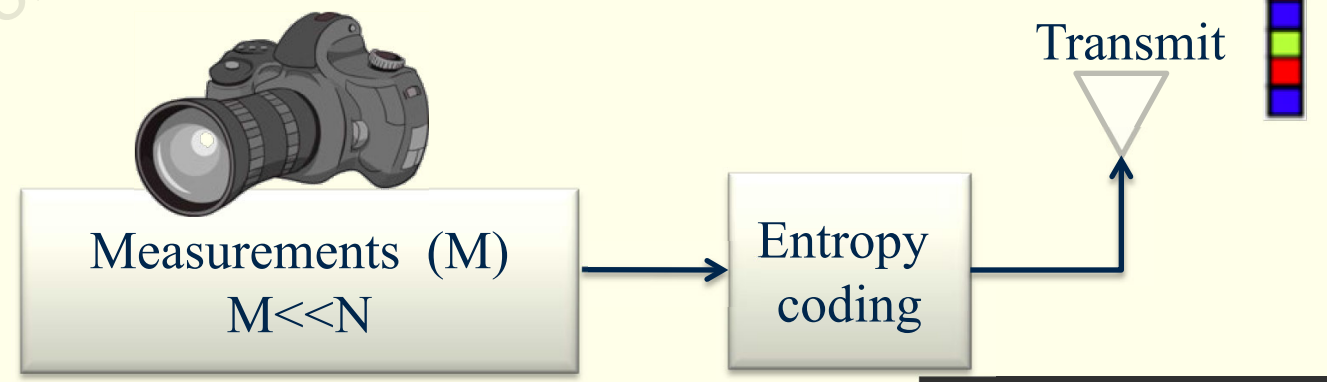
 ORCID: <https://orcid.org/0000-0003-0372-4293>

# Main idea

## Traditional compression techniques



## Compressive sensing (CS)



# Motivation

---

**The most common limitations of compressive sensing (CS) techniques are:**

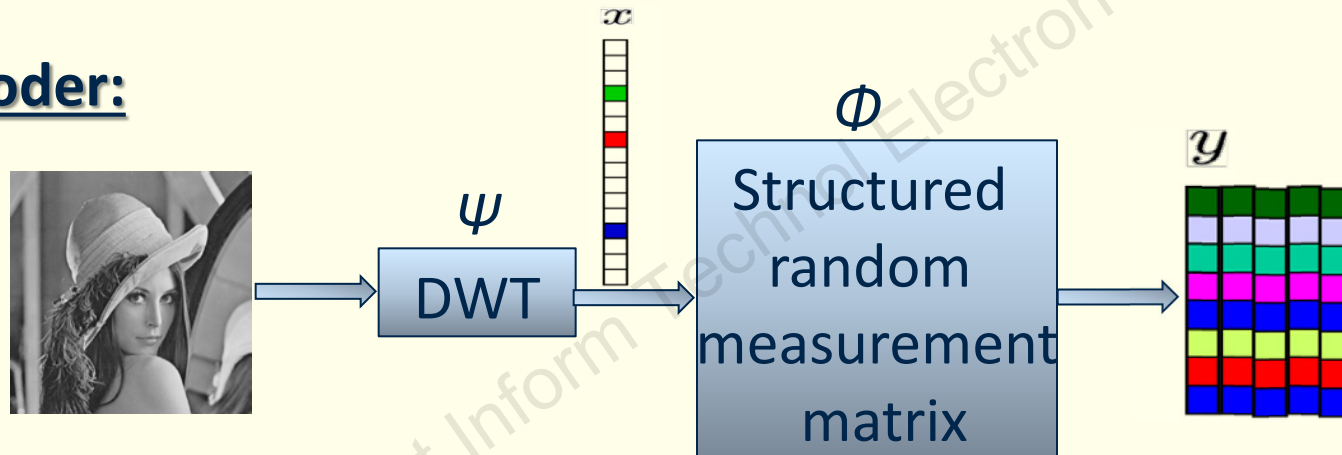
1. lack of the reconstruction quality of reconstructed images;
2. requiring large no of measurements to reconstruct image with acceptable quality;
3. computational complexity is high at decoding side.

**In this paper, limitations of the sparsity adaptive matching pursuit CS technique will be addressed to improve its reconstruction efficiency.**

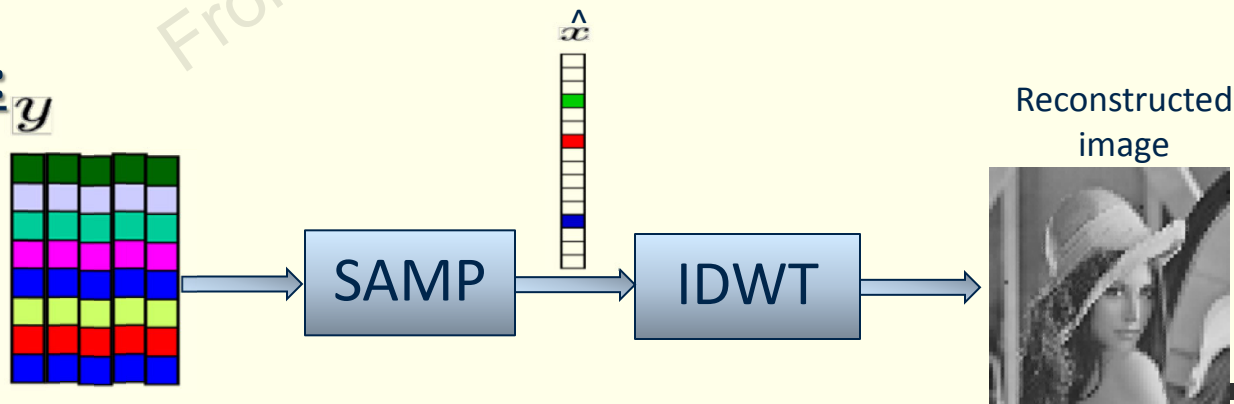
---

# Conventional CS-SAMP technique

## Encoder:



## Decoder:



# Conventional CS-SAMP technique

## Advantage

- Reconstructs signals without prior information of sparsity
- Robust to noise compared to the other greedy algorithms
- faster than linear programming methods

## Disadvantage

- Still suffer from the lack of reconstruction quality

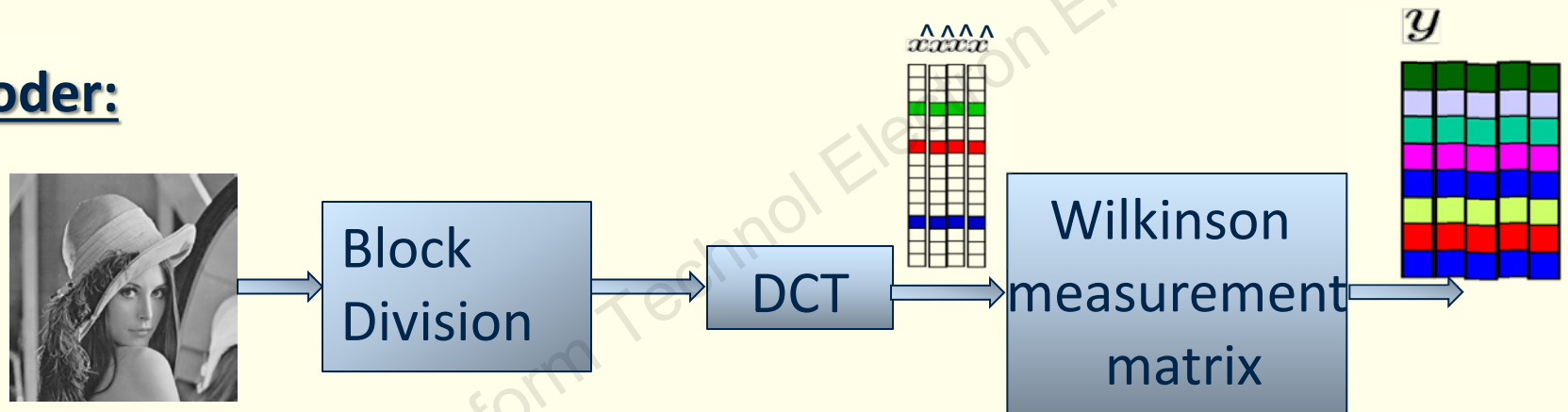
**WHY?**

**Because of choosing  
an improper measurement  
matrix**

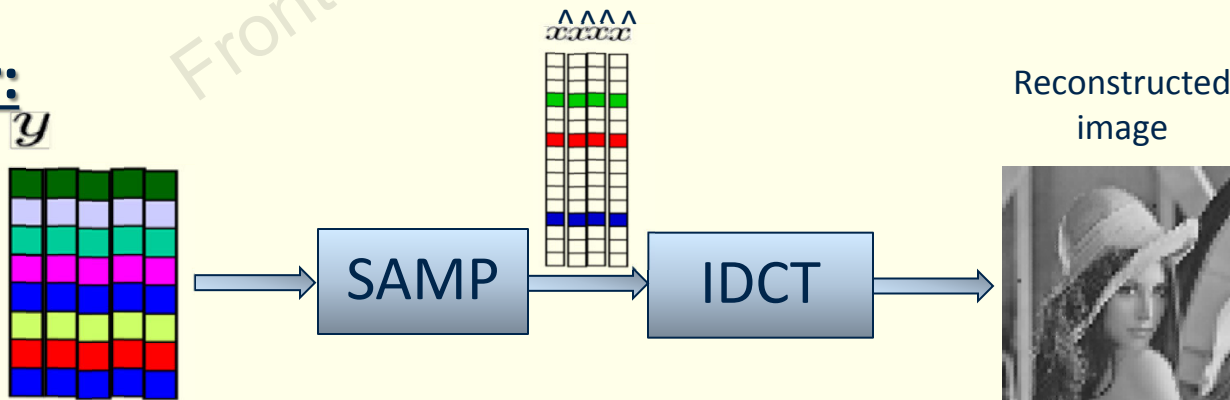
# Method

## Proposed BCS-SAMP Technique

### Encoder:



### Decoder:



# Wilkinson Matrix

8x8 Wilkinson matrix

$\frac{n-1}{2}$	1	0	0	0	0	0	0	0
1	$\frac{n-2}{2}$	1	0	0	0	0	0	0
0	1	$\frac{n-3}{2}$	1	0	0	0	0	0
0	0	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	0
$\vdots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\vdots$
0	0	0	$\ddots$	$\ddots$	$\ddots$	$\ddots$	$\ddots$	0
0	0	0	0	0	1	$\frac{n-3}{2}$	1	0
0	0	0	0	0	0	1	$\frac{n-2}{2}$	1
0	0	0	0	0	0	0	1	$\frac{n-1}{2}$

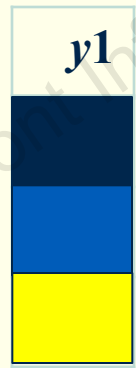
Re-orthogonal of 3x8 Wilkinson matrix

-0.78	0.58	-0.21	-0.05	0	0	0	0
-0.57	0.53	0.57	0.25	0	0	0	0
-0.23	0.54	-0.44	-0.68	0	0	0	0

M  
Re-orthogonal  
measurements

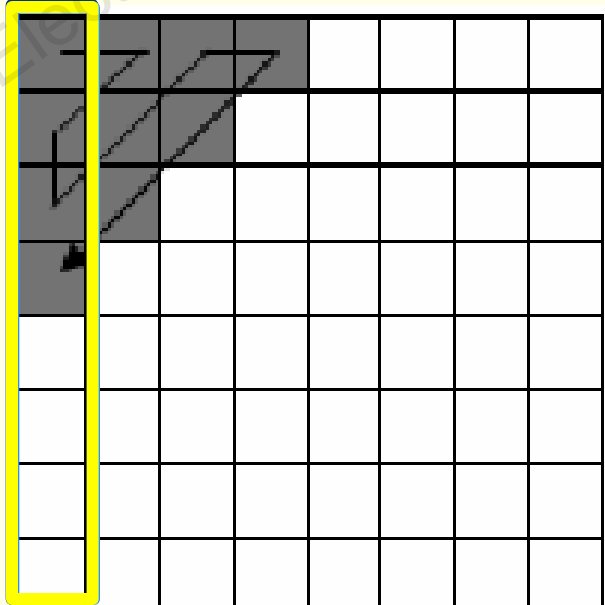
### Re-orthogonal of 3x8 Wilkinson matrix

-0.78	0.58	-0.21	-0.05	0	0	0	0
-0.57	0.53	0.57	0.25	0	0	0	0
-0.23	0.54	-0.44	-0.68	0	0	0	0



This will help SAMP to find the right column easily

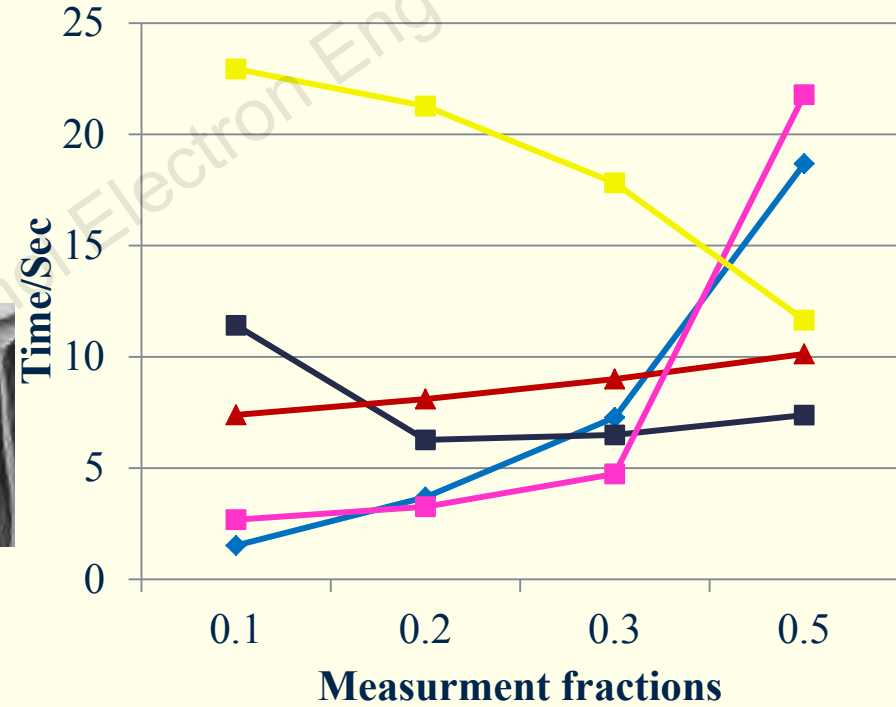
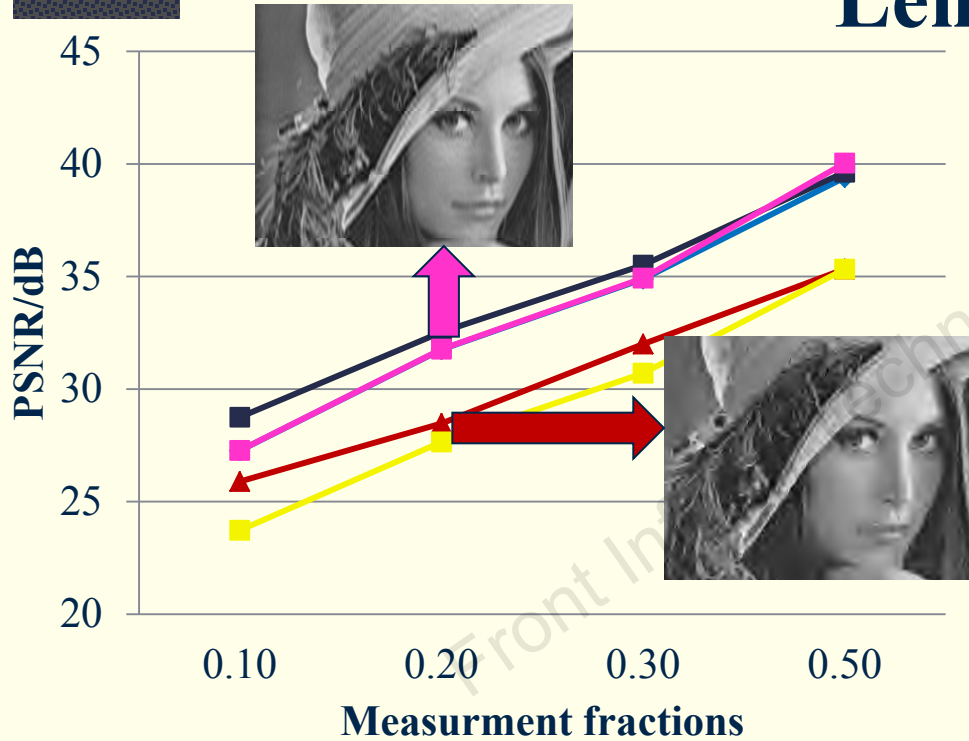
### DCT coefficients of image



- High coefficient=VIP
- Low coefficient=approximately zero

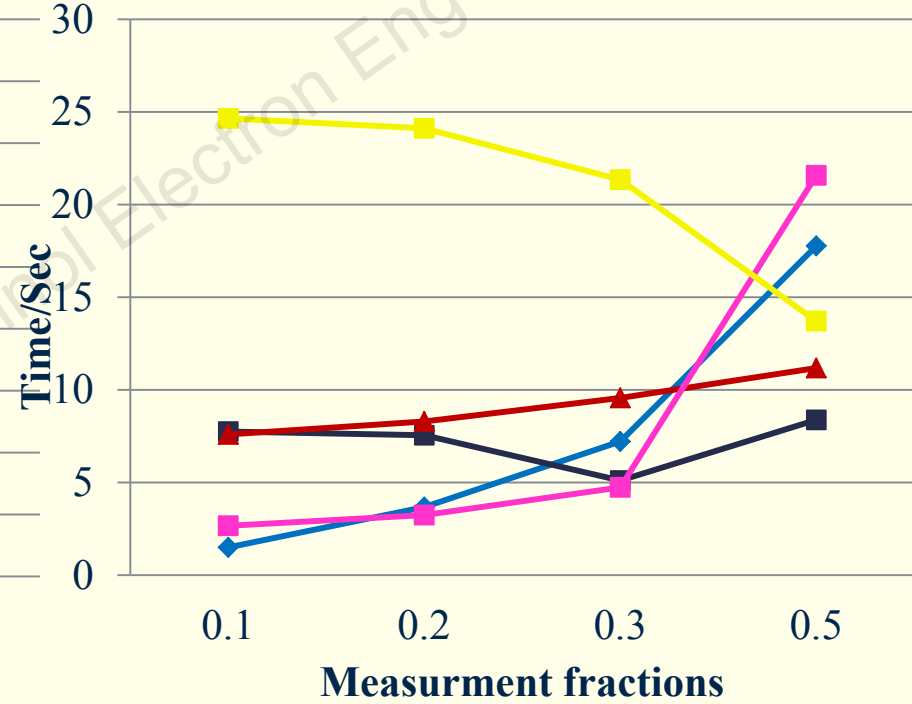
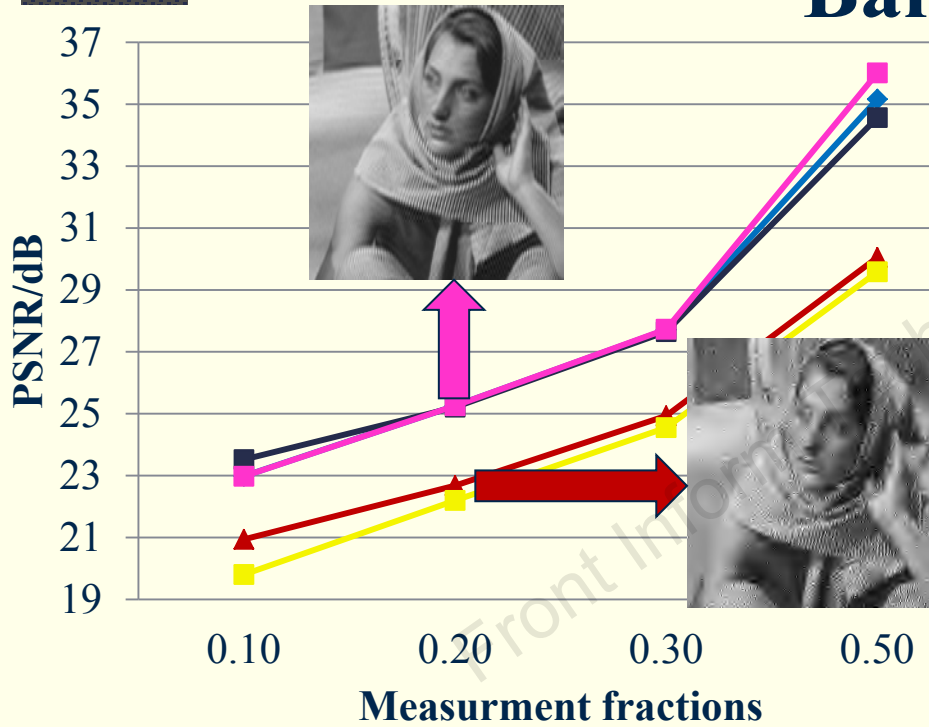
# Results

## Lenna



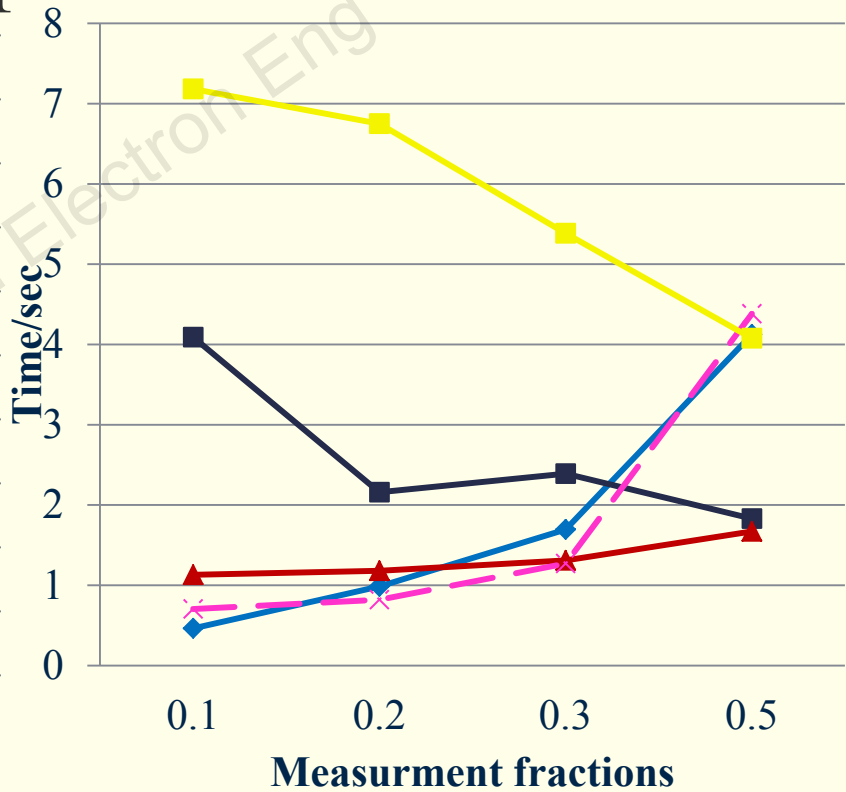
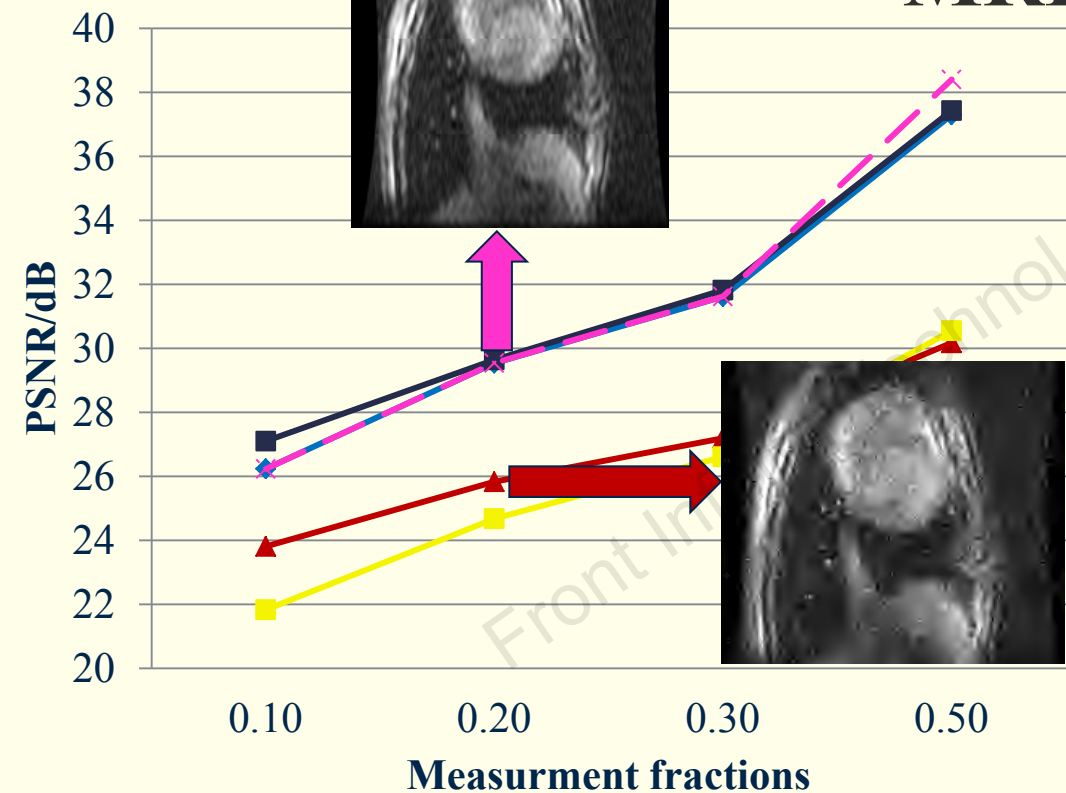
- BCS-OMP
- SAMP
- GPSR
- BCS-SPL
- Proposed 3 BCS-SAMP

# Barbara



- BCS-OMP
- SAMP
- GPSR
- BCS-SPL
- Proposed 3 BCS-SAMP

# MRI



- BCS-OMP
- SAMP
- GPSR
- BCS-SPL
- Proposed 3 BCS-SAMP

# Conclusion

---

It can be concluded from our work that

1. The good choice of measurement matrix play a vital role in the performance of the BCS-SAMP techniques.
  2. The use of Wilkinson measurement matrix improve reconstruction quality, increased the compression ratio and reduced the computational time of these greedy algorithm.
  3. The performance of the greedy algorithms as BCS-SAMP become comparable to the performance of the iterative techniques as BCS-SPL in terms of quality with less computational time.
-