

Zhengquan YAN, Xiaofang PAN, Qing ZHANG, Zengqiang CHEN, 2021. Finite-time formation control for first-order multi-agent systems with region constraints. *Frontiers of Information Technology & Electronic Engineering*, 22(1):134-140. <https://doi.org/10.1631/FITEE.2000177>

# Finite-time formation control for first-order multi-agent systems with region constraints

**Key words:** Finite-time formation; Multi-agent system; Asymptotic convergence; Set constraint; Lyapunov theorem

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# Motivation

1. In practical applications, we need to consider some constraints and timeliness, such as the need to implement a formation into a specific area within a specific time.
2. We design a controller which controls all the agents to enter the desired region and to track a desired shape in finite time.
3. For the desired region, the previous studies often obtain a leader-following formation controller. In contrast, our algorithm does not depend on the leader. It has good robustness.

# Main idea

1. A novel control algorithm is proposed using local information and interaction.
2. If the communication graph is undirected and connected and the desired framework is rigid, it is proved that the controller can be used to solve the formation problem with a target area.

# Method

Based on the rigorous undirected network topology, it is shown that all the agents would enter the global desired area and reach formation in finite time.

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# Major results

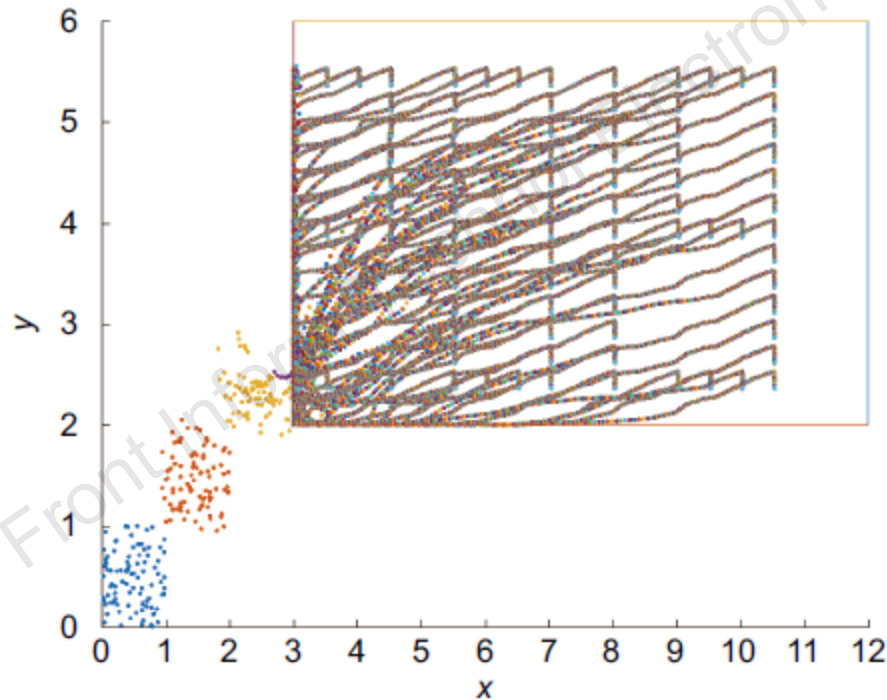
1. Under Assumptions 1 and 2, if  $\beta > N$ , for the first-order MAS (1) with algorithm (5), all the agents can realize the asymptotic convergence of the formation shape in finite time and  $\mathbf{x}_i(t) \in \Omega$  in finite time.

$$\dot{\mathbf{x}}_i(t) = \mathbf{u}_i(t), \quad (1)$$

$$\begin{aligned} \mathbf{u}_i(t) = & - \sum_{j \in N_i} a_{ij} \text{sgn}(\mathbf{x}_i(t) - \mathbf{x}_j(t) - \gamma_{ij}^*) \\ & - \beta \text{sgn}(\mathbf{x}_i(t) - P_{\Omega}(\mathbf{x}_i(t))). \end{aligned} \quad (5)$$

# Major results (Cont'd)

## 2. Simulation process of a 92-agent target formation shape



**Fig. 4** Simulation process of a 92-agent target formation shape

# Major results (Cont'd)

## 3. Final configuration of 92 agents

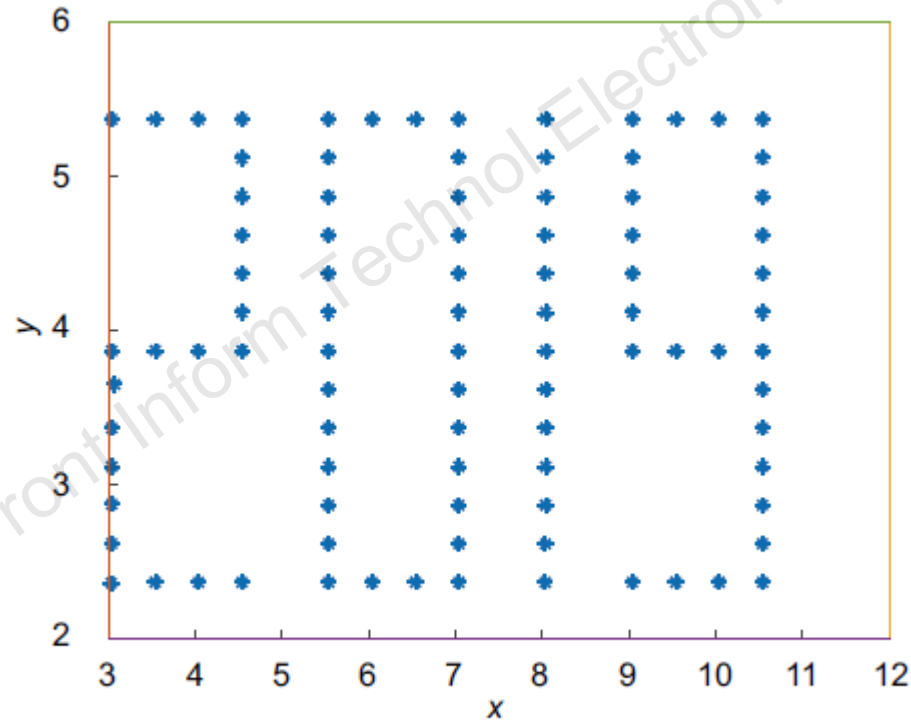


Fig. 5 Final configuration of 92 agents

# Conclusions

1. A formation controller has been proposed by the convex set and local information among the agents.
2. Based on the rigorous undirected network topology, it is shown that all the agents would enter the global desired area and reach formation in finite time.
3. The results have been illustrated by simulation.



Zhengquan YANG received his BS degree in mathematics from the Institute of mathematics, Qufu Normal University, Qufu, China, in 2003, and his PhD in Operational Research and Control Theory from Nankai University, Tianjin, China, in 2009. He is working at the Civil Aviation University of China. His main research interests include synchronization of complex networks and flocking of multi-agents.



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