

# Pullout capacity of small ground anchor: a least square support vector machine approach

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# Details of LSSVM

Training vector:

$$x = [D_{eq}, L, q_c, f_s, IT] \quad y = [Q]$$

$$D = \left\{ \left( \mathbf{x}^1, \mathbf{y}^1 \right), \dots, \left( \mathbf{x}^l, \mathbf{y}^l \right) \right\}$$

The data has been taken from the work of Shahin and Jaksa, (2006).

According to LSSVM:  $y(x) = w^T \varphi(x) + b$

Where the nonlinear mapping  $\varphi(\cdot)$  maps the input data into a higher dimensional feature space,  $w$  = an adjustable weight vector and  $b$  = scalar threshold.

# Optimization problem

$$\text{Minimize: } \frac{1}{2} w^T w + \gamma \frac{1}{2} \sum_{k=1}^N e_k^2$$

$$\text{Subjected to: } y(x) = w^T \varphi(x_k) + b + e_k, k=1, \dots, N$$

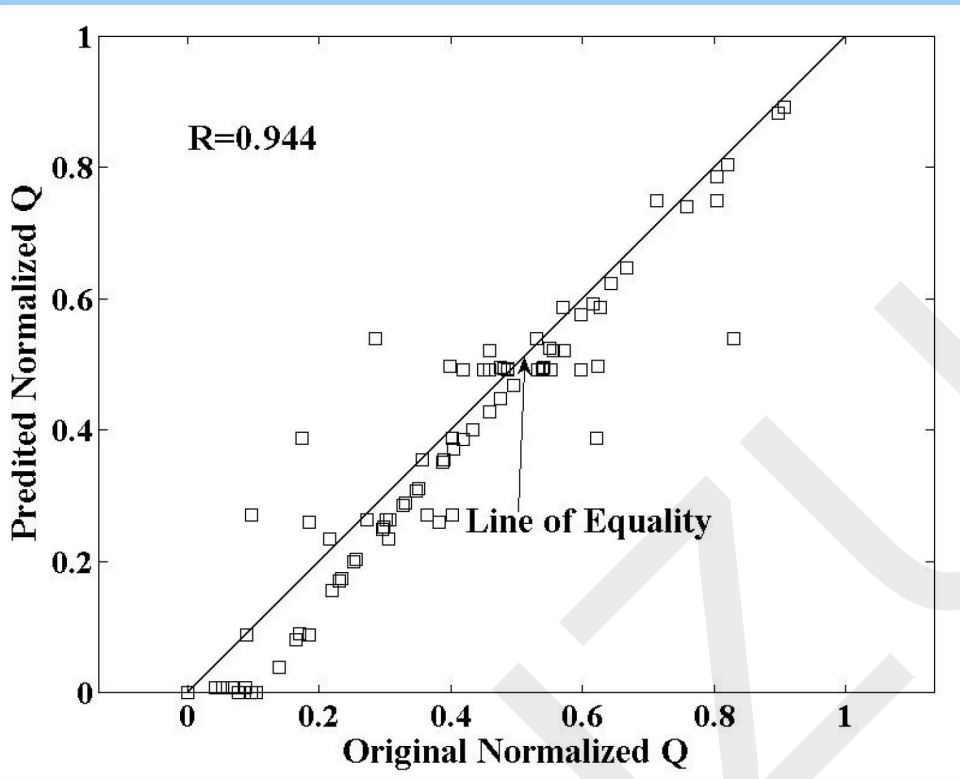
Where  $\gamma$  is the regularization parameter, determining the trade-off between the fitting error minimization and smoothness and  $e_k$  is error variable.

The resulting equation from LSSVM model for Q prediction:

$$Q = y(x) = \sum_{k=1}^N \alpha_k K(x, x_k) + b$$

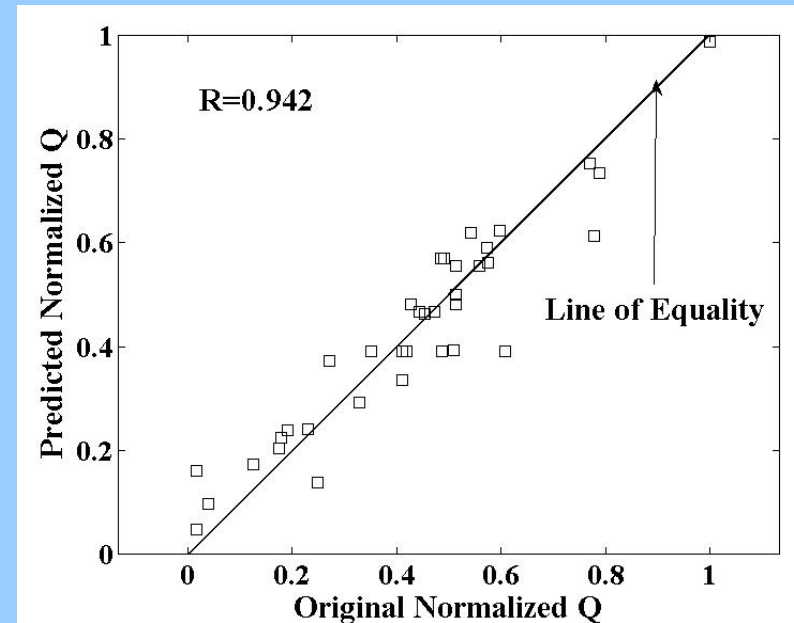
Where  $K(x_i, x)$  is a kernel function, and  $\alpha_i$  Lagrange multipliers

# Performance of LSSVM



Training Data=83

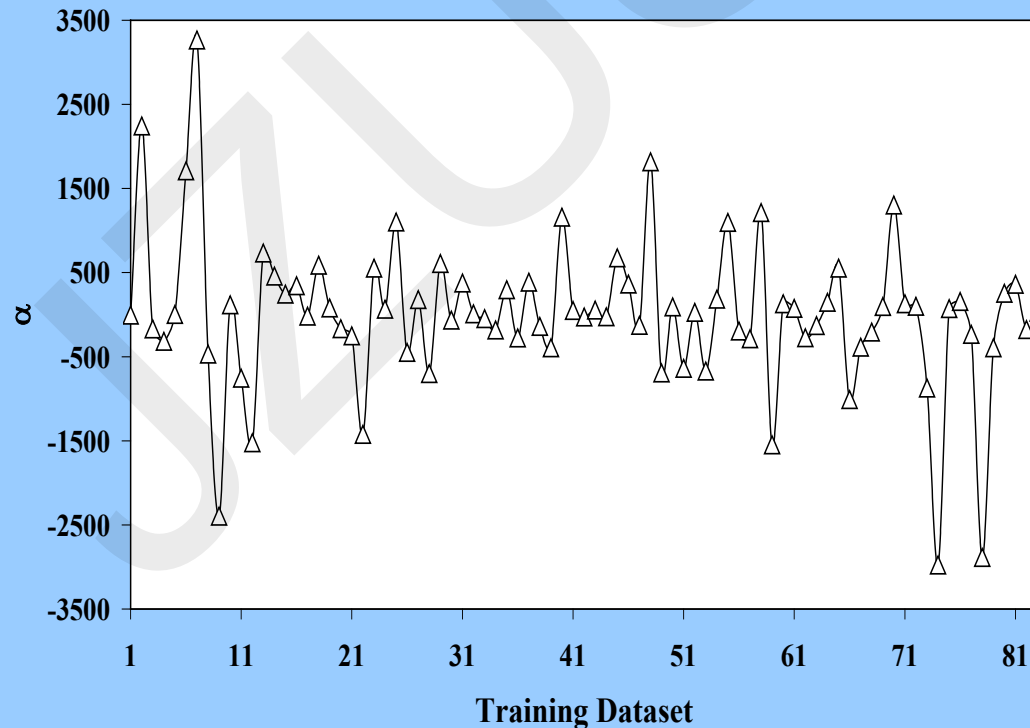
Testing Data=36



# Equation for Prediction of Q

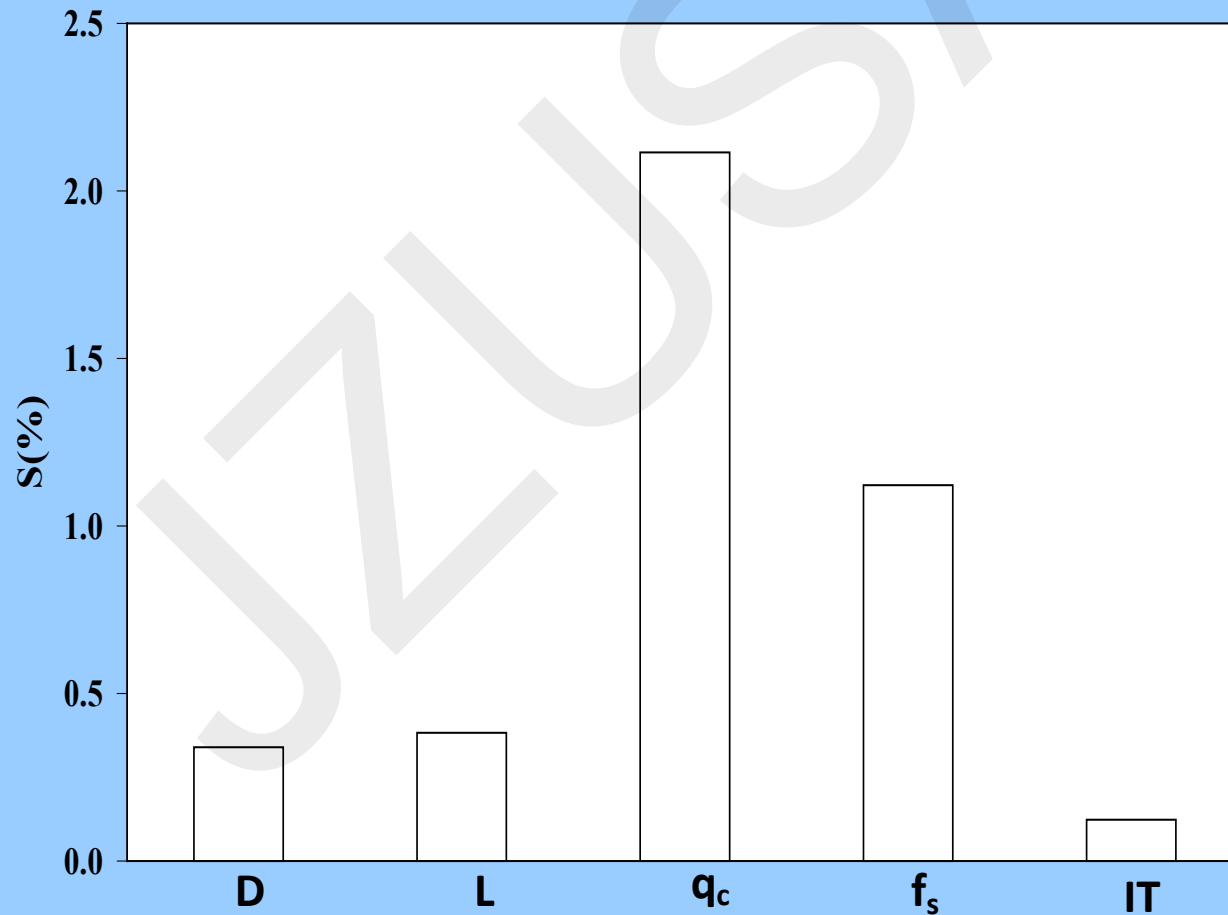
Geotechnical engineers can use the following equation for prediction of Q

$$Q = \sum_{k=1}^{83} \alpha_k \exp \left\{ -\frac{(x_i - x)(x_i - x)^T}{98} \right\} - 3.8239$$



# Sensitivity analysis

$$S(\%) = \frac{1}{N} \sum_{j=1}^N \left( \frac{\% \text{ change in output}}{\% \text{ change in input}} \right)_j \times 100$$



# Conclusion

- The developed LSSVM gives better performance than the ANN
- User can use the developed equation for practical purpose
- Sensitivity analysis indicates that  $q_c$  is the most significant input parameter for predicting  $Q$  of small ground anchor.