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Quasi 1D modeling of two-phase flow and deposit formation for urea-selective catalytic reduction systems

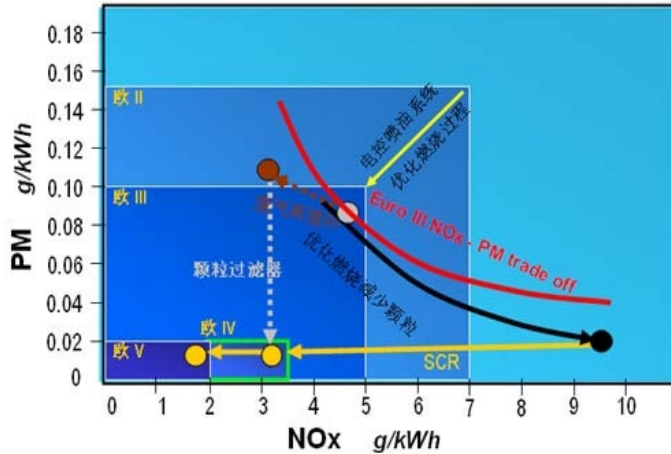
Xu-bo GAN



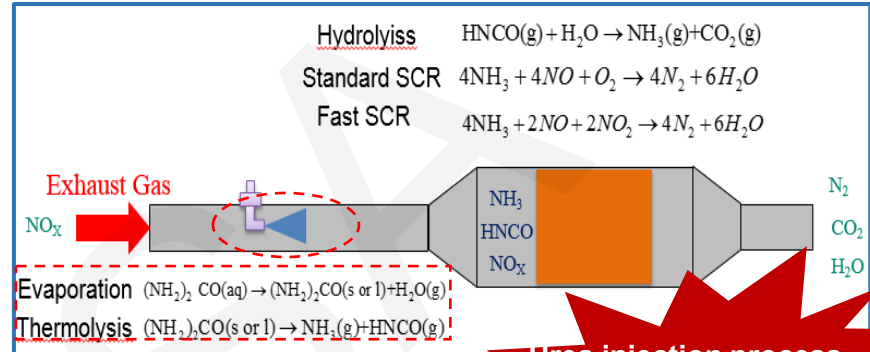
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Introduction



SCR is one of the most promising methods to reduce NOx emission from heavy-duty vehicles



Urea injection process is very important for SCR performance

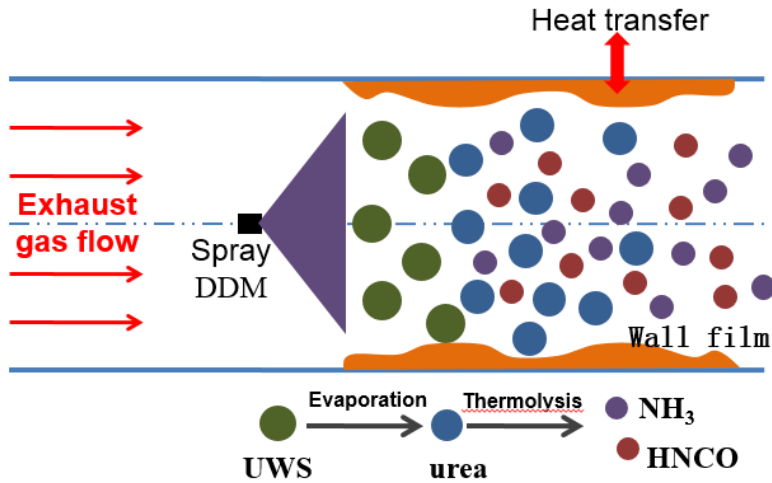
Urea deposits

Injection strategy & ammonia production

The 'Urea deposits' section shows three images of engine components heavily coated with white urea deposits. The 'Injection strategy & ammonia production' section shows two 3D simulation diagrams of a reactor. The left diagram illustrates the injection strategy with a color-coded flow field. The right diagram shows ammonia production with a color-coded flow field.



Modeling Method



- Liquid phase model
(droplet motion, evaporation, thermolysis)

$$\frac{dm_d}{dt} = -\pi D_d \rho_{g,mix} \Gamma_{ref} Sh \ln(1 + B_M) \times (T_\infty / 673) \quad \frac{du_d}{dt} = \frac{3}{4} \frac{\rho_g C_d}{\rho_d D_d} |u_g - u_d| (u_g - u_d)$$

$$\frac{dT_d}{dt} = \frac{(-dm_d / dt) c_{p,vap} (T_g - T_d) / B_T - L_{vap}}{m_d c_{p,d}} \quad \frac{dm_d}{dt} = -m_d A e^{(-E_a / RT_d)}$$

- Spray wall interaction

$$s_d = \left| \int u_r dt \right| \geq d_c$$

$$K = \frac{(\rho D)_d^{0.75} u_d^{1.25}}{\sigma_d^{0.5} \mu_d^{0.25}} \quad T^* = \frac{T_w}{T_{sat}}$$

- Gas flow

$$\frac{\partial \rho_g}{\partial t} + \frac{\partial \rho_g u_g}{\partial x} = 0 \quad \frac{\partial \rho_g H_g}{\partial t} + \frac{\partial \rho_g u_g H_g}{\partial x} = \alpha_{gw} (T_w - T_g) a_{geo} + S_{ggs}$$

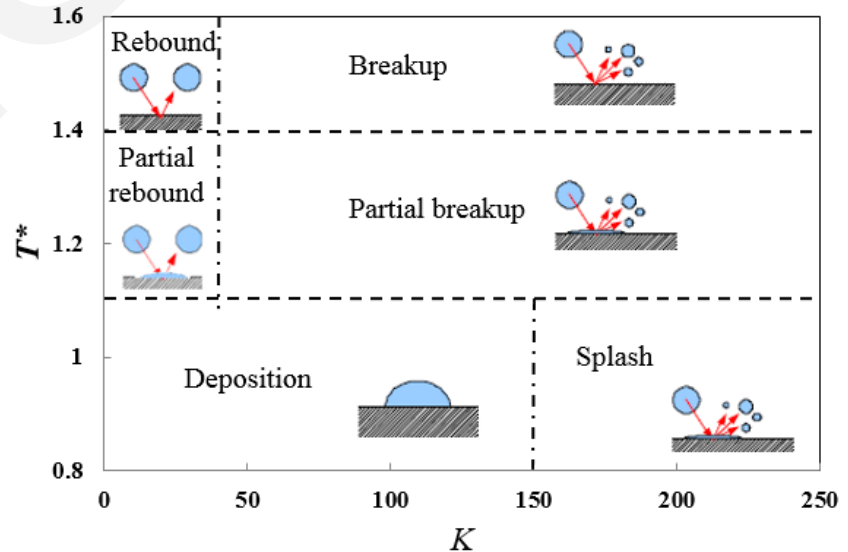
$$\frac{dP_g}{dx} = -K_d u_g \quad \frac{\partial \rho_g w_{i,g}}{\partial t} + \frac{\partial \rho_g u_g w_{i,g}}{\partial x} = S_{species}$$

- Heat transfer of pipe wall

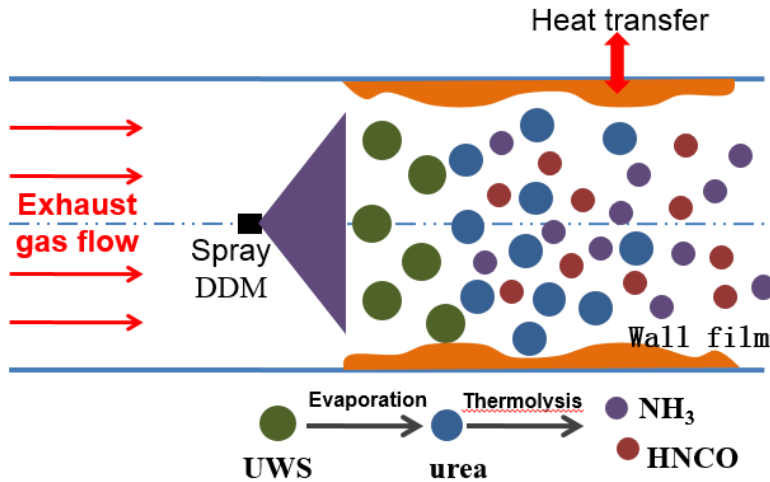
$$\frac{\partial}{\partial t} (T_w \rho_{l,w} c_{p,l,w}) = \frac{\partial}{\partial z} (\lambda_{l,w} \frac{\partial T_w}{\partial z}) + \frac{1}{r} \frac{\partial}{\partial r} (r \lambda_{l,w} \frac{\partial T_w}{\partial r}) + S_{wd} + S_{wf}$$

$$\frac{\partial T_w}{\partial z} = 0 \quad @ \quad z = 0 \quad \frac{\partial T_w}{\partial r} = -\frac{\alpha_{gw}}{\lambda_{l,w}} (T_g - T_w) \quad @ \quad r = r_{gw}$$

$$\frac{\partial T_w}{\partial z} = 0 \quad @ \quad z = L_{pipe} \quad \frac{\partial T_w}{\partial r} = -\frac{\alpha_{wa}}{\lambda_{l,w}} (T_w - T_{amb}) \quad @ \quad r = r_{wa}$$



Wall film model



• Wall film thermolysis

	Reactions
R1	urea → NH ₄ ⁺ + NCO ⁻
R2	NH ₄ ⁺ → NH ₃ (g) + H ⁺
R3	NCO ⁻ + H ⁺ → HNCO(g)
R4	urea + NCO ⁻ + H ⁺ → biuret
R5	biuret → urea + NCO ⁻ + H ⁺
R6	biuret + NCO ⁻ + H ⁺ → CYA + NH ₃ (g)
R7	CYA → 3NCO ⁻ + 3H ⁺
R8	CYA + NCO ⁻ + H ⁺ → ammelide + CO ₂
R9	ammelide → 2NCO ⁻ + 2H ⁺ + HCN(g) + NH(g)

• Wall film thickness

$$\delta_i = \frac{V_{f,i}}{a_i}$$

• Wall film motion

$$F = (u_g - u_f) \delta f_i$$

• Wall film evaporation

$$\frac{dm_f}{dt} = -a_f Y_w \rho_g h_m \ln(1 + B_m) \beta \left(\frac{T_w}{T_{sat}} \right)^2$$

• Continuity equation

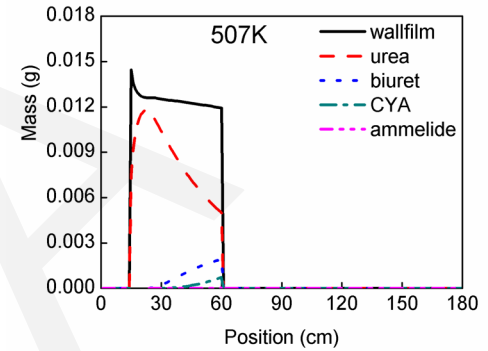
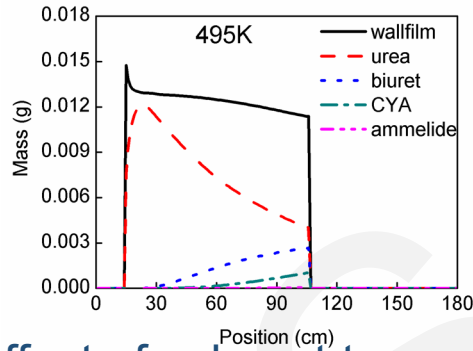
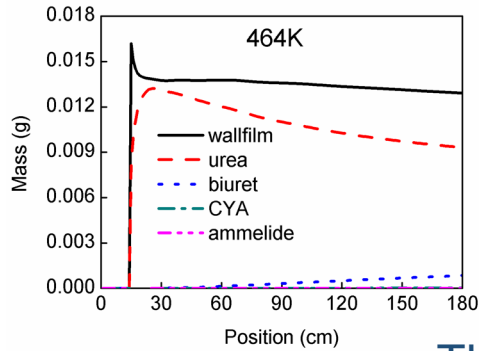
$$\frac{\partial A_s}{\partial t} + \frac{\partial A_s u_f}{\partial x} = \frac{S_m Y_u}{M \theta} \quad \text{Active surface}$$

$$\frac{\partial m_f}{\partial t} + \frac{\partial m_f u_f}{\partial x} = S_m + S_{th} + S_{eva} \quad \text{Film mass}$$

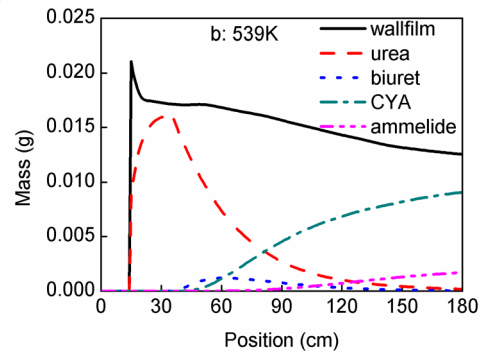
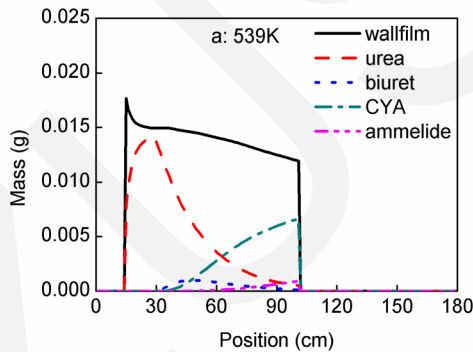
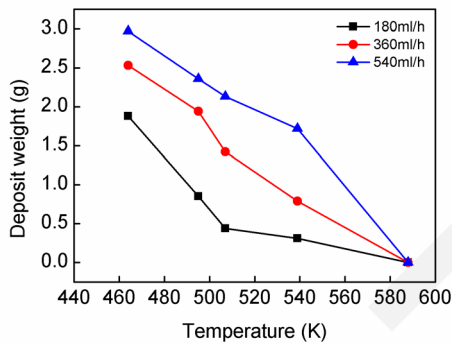
$$\frac{\partial m_i}{\partial t} + \frac{\partial m_i u}{\partial x} = S_i \quad \text{Species mass}$$

A new one dimensional wall film model simplified from a three dimensional model is proposed. The model assumes that the wall film distributes evenly on the inner surface of the pipe mesh

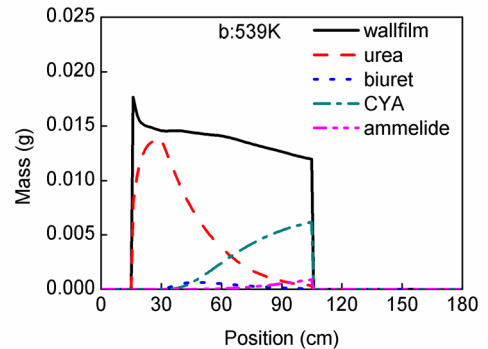
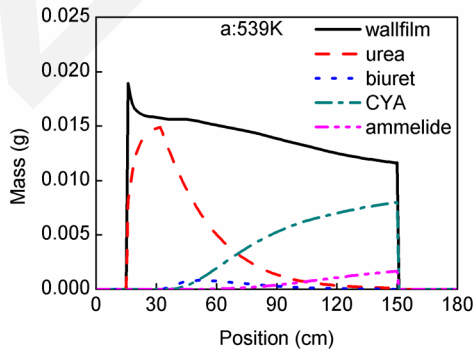
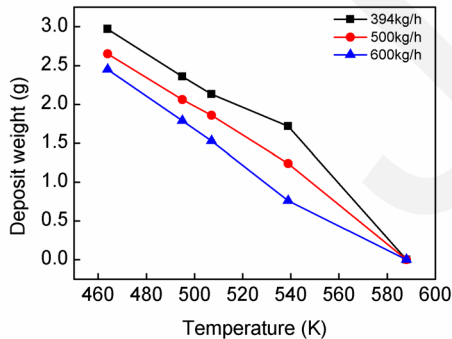
Results and discussion



The effect of exhaust temperature



The effect of UWS injection rate



The effect of exhaust mass flow

Conclusions

- ❑ A simplified one dimensional model of gas-liquid two phase flow is presented. The developed model can calculate not only the generation of the reducing agent but also the formation of deposits in the exhaust pipe.
- ❑ A combination of Birkhold's direct decomposition model and Ebrahimian's kinetic model was implemented, and a new one dimensional wall film model was developed. The position, weight and components of deposits can be simulated.
- ❑ Simulation results showed that: (1) A decrease in exhaust temperature will increase the wall film region and weight of deposits. (2) Deposit components are highly dependent on temperature: when the temperature is low, most deposits are urea, but when the temperature rises, by-products such as biuret and CYA begin to form. (3) The UWS injection rate can affect the total mass of wall film and expand the film region, but it has little influence on deposit components. (4) An increase in exhaust mass flow can decrease the total weight of deposit and the film region on the pipe wall because of the promotion of the mass and heat transfer process both in the droplets and wall film.