

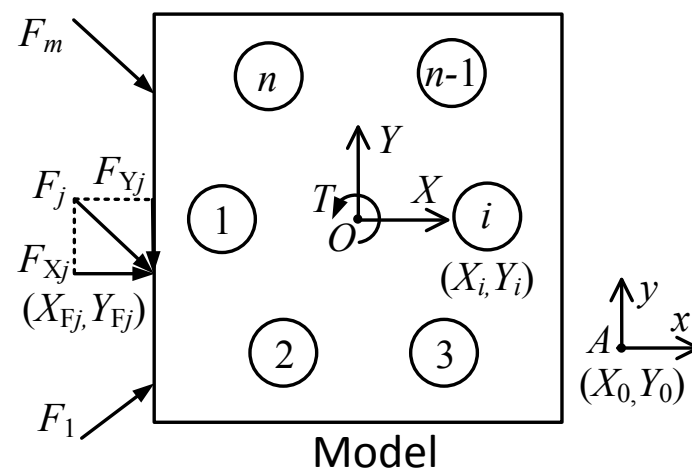
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## Nonlinear analysis of pile groups subjected to combined lateral and torsional loading

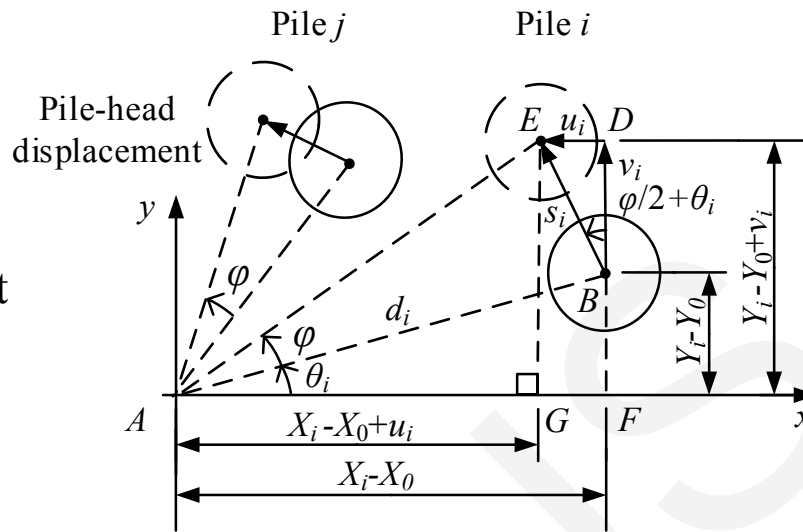
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Key words: Combined lateral and torsional loading, Pile groups, Twist center,  $\rho$ -multiplier, Group effect

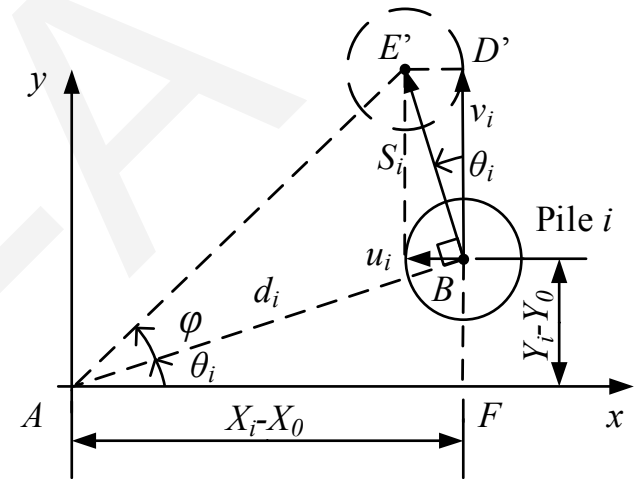


# Method of analysis

Pile-head displacements relation is built in these two situations.



Exact Solution



Approximate Solution

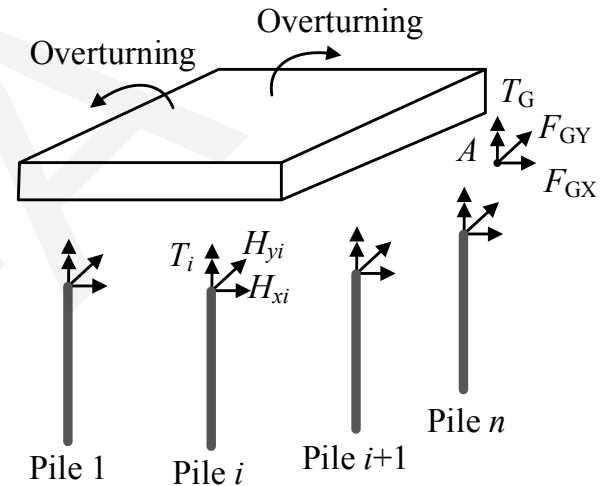
$$\left\{ \begin{array}{l} u_i = \frac{(Y_i - Y_0) \cos(\frac{\varphi}{2}) + (X_i - X_0) \sin(\frac{\varphi}{2})}{(Y_R - Y_0) \cos(\frac{\varphi}{2}) + (X_R - X_0) \sin(\frac{\varphi}{2})} u_R, \\ v_i = \frac{(X_i - X_0) \cos(\frac{\varphi}{2}) - (Y_i - Y_0) \sin(\frac{\varphi}{2})}{(X_R - X_0) \cos(\frac{\varphi}{2}) - (Y_R - Y_0) \sin(\frac{\varphi}{2})} v_R. \end{array} \right.$$

$$\left\{ \begin{array}{l} u_i \doteq \frac{Y_i - Y_0}{X_0 - X_R} v_R, \\ v_i \doteq \frac{X_i - X_0}{X_R - X_0} v_R. \end{array} \right.$$

# Method of analysis

Simplified  
Static  
Equilibrium  
Equation of  
pile cap

$$\left\{ \begin{aligned} \frac{v_R}{X_0 - X_R} \sum_{i=1}^n K_{Hi} (Y_i - Y_0) &= F_{GX}, \\ \frac{v_R}{X_0 - X_R} \sum_{i=1}^n K_{Hi} (X_0 - X_i) &= F_{GY}, \\ \frac{v_R}{X_0 - X_R} \sum_{i=1}^n \{K_{Hi} [(X_0 - X_i)^2 + (Y_i - Y_0)^2] + K_{Ti}\} \\ &= \sum_{j=1}^m [F_{Yj} (X_{Fj} - X_0) - F_{Xj} (Y_{Fj} - Y_0)] + T. \end{aligned} \right.$$



Solution

$$\left\{ \begin{aligned} X_0 &= \frac{b}{a} - \frac{F_{GY} (ag + ah + ad - b^2 - c^2)}{acF_{GX} - abF_{GY} + a^2q - a^2r + a^2T}, \\ Y_0 &= \frac{c}{a} + \frac{F_{GX} (ag + ah + ad - b^2 - c^2)}{acF_{GX} - abF_{GY} + a^2q - a^2r + a^2T}, \\ v_R &= \frac{F_{GY}}{a} \\ &\quad - \frac{(b - aX_R)(cF_{GX} - bF_{GY} + aq - ar + aT)}{a^2g + a^2h + a^2d - ab^2 - ac^2}, \end{aligned} \right.$$

$$\begin{aligned} a &= \sum_{i=1}^n K_{Hi}, & g &= \sum_{i=1}^n K_{Hi} X_i^2, \\ b &= \sum_{i=1}^n K_{Hi} X_i, & h &= \sum_{i=1}^n K_{Hi} Y_i^2, \\ c &= \sum_{i=1}^n K_{Hi} Y_i, & q &= \sum_{j=1}^m F_{Yj} X_{Fj}, \\ d &= \sum_{i=1}^n K_{Ti}, & r &= \sum_{j=1}^m F_{Xj} Y_{Fj}. \end{aligned}$$

# Method of analysis

Generalized  $p$ -multiplier of pile  $i$   
(Kong et al., 2019)

Reduction factors of the leading  
pile and trailing pile,  $\beta_l$  and  $\beta_t$ ,

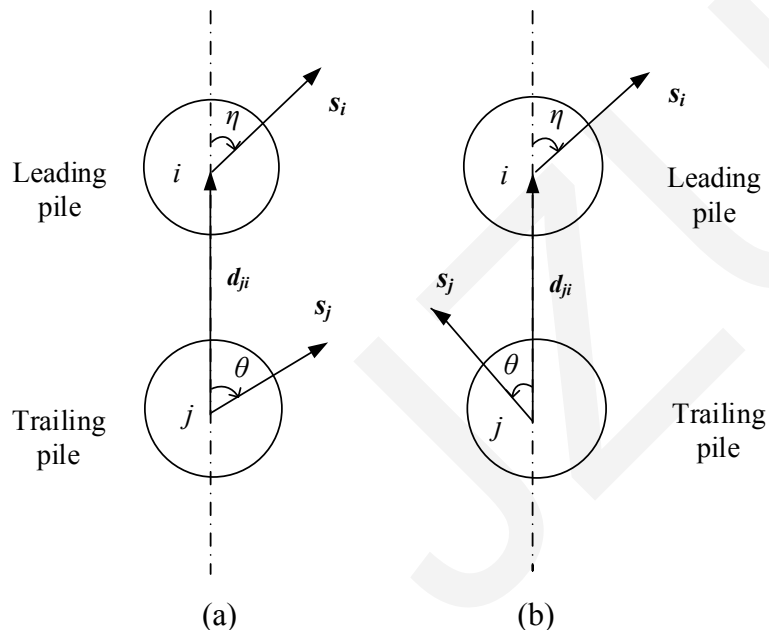


Fig. 4 Two motion states of a double-pile group  
subjected to combined lateral and torsional loading

$$f_{mi} = \beta_{1i} \beta_{2i} \dots \beta_{ji} \dots \beta_{ni} \quad (j \neq i),$$

$$\beta_l = \begin{cases} b_l - \frac{b_l - a_l}{|\theta_c|} \sqrt{\theta_c^2 - \theta^2} & (0 > \theta \geq \theta_c \text{ or } \theta_c \geq \theta \geq 0), \\ 1 & (0 > \theta_c \geq \theta \geq -90^\circ \text{ or } 90^\circ \geq \theta \geq \theta_c > 0) \end{cases}$$

$$\beta_t = \begin{cases} b_t - \frac{b_t - a_t}{|\theta_c|} \sqrt{\theta_c^2 - \theta^2} & (0 > \theta \geq \theta_c \text{ or } \theta_c \geq \theta \geq 0), \\ 1 & (0 > \theta_c \geq \theta \geq -90^\circ \text{ or } 90^\circ \geq \theta \geq \theta_c > 0) \end{cases}$$

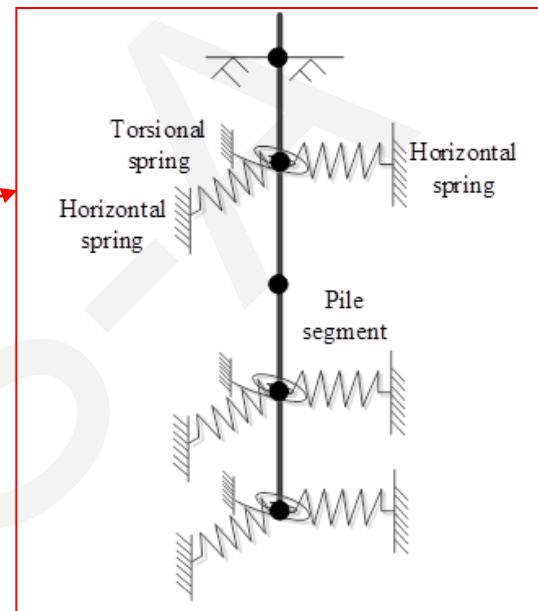
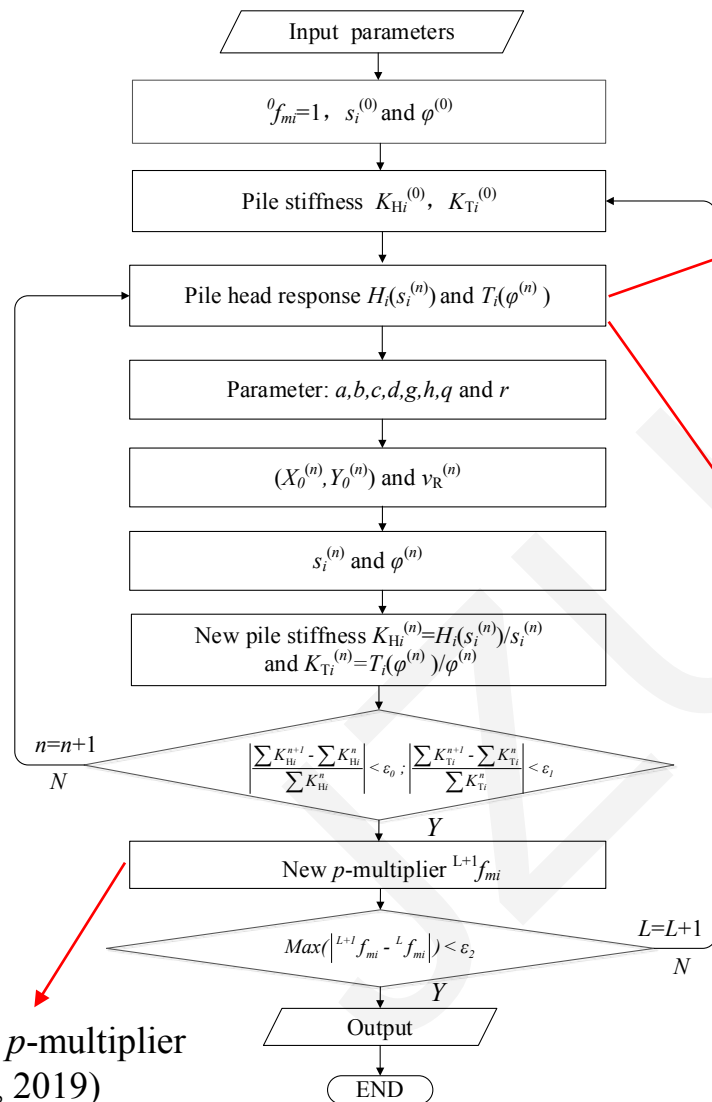
More detail refers to:

Kong LG, Fan JY, Liu JW, Chen YM,  
2019. Group effect in piles under  
eccentric lateral loading in sand.

*Journal of Zhejiang University-  
SCIENCE A*, 20(4): 243-257.

<https://doi.org/10.1631/jzus.a1800617>

# Flow chart of ELPGROUP



The deflection-torsion coupling effect:

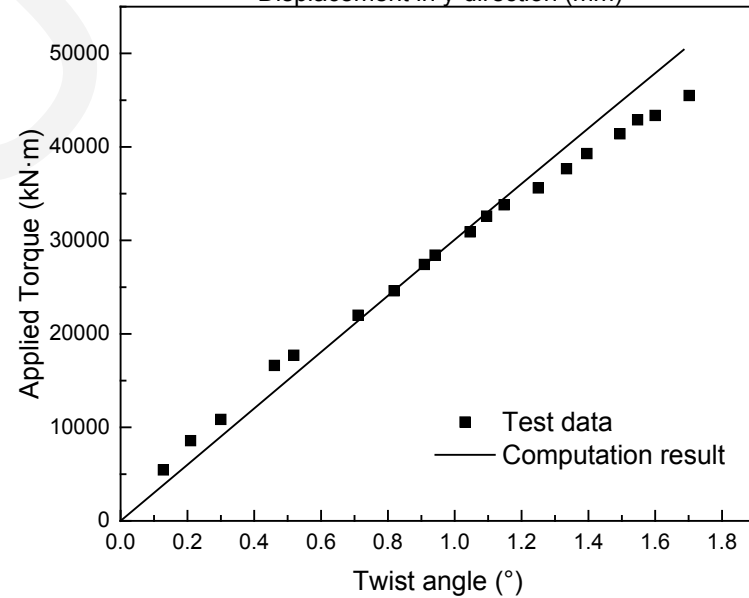
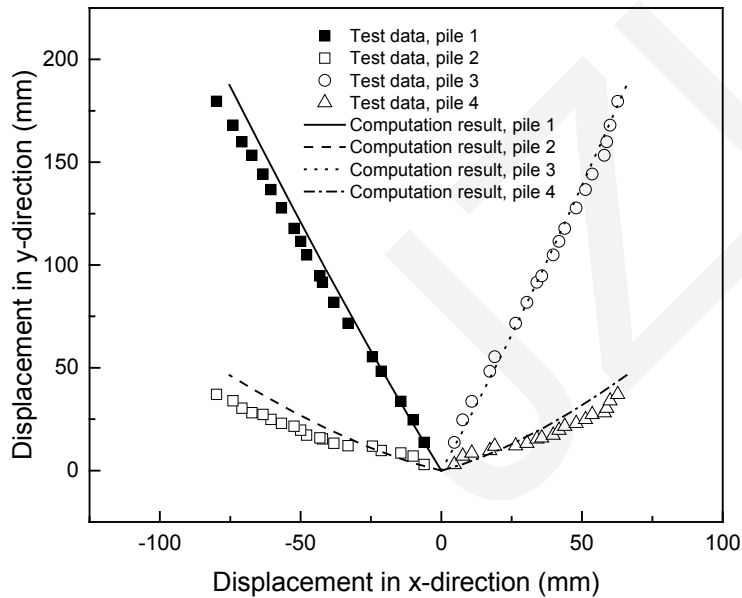
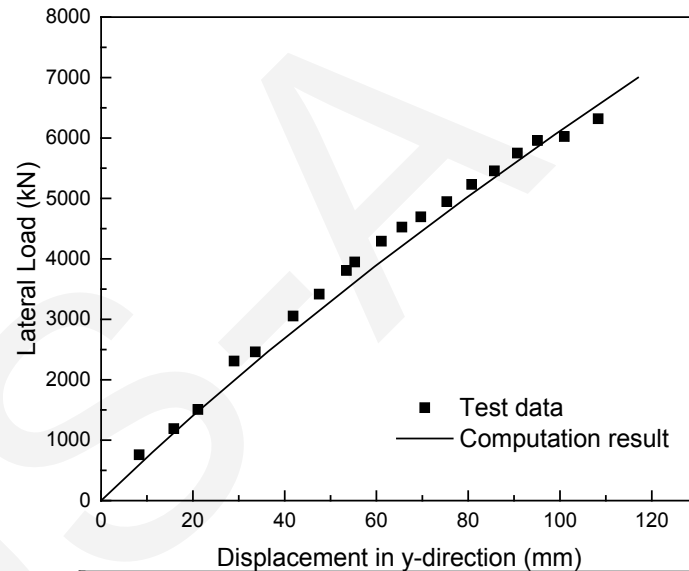
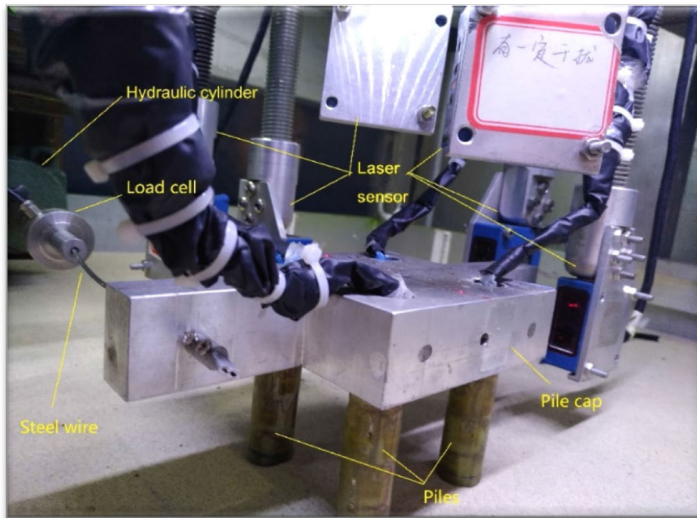
$$\alpha_{TH} = 1 + \left( \frac{\beta_{TH}}{p_a D} \right) p,$$

Kong LG, Zhang LM, 2008a. Experimental study of interaction and coupling effects in pile groups subjected to torsion. *Canadian Geotechnical Journal*, 45(7): 1006-1017.

<https://doi.org/10.1139/t08-038>

Generalized  $p$ -multiplier  
(Kong et al., 2019)

# Test and Prediction Results



# Summary

1. A simple and computationally efficient approach has been developed for analyzing the nonlinear response of pile groups under combined lateral and torsional loading.
2. The pile-cap motion of a pile group subjected to combined lateral and torsional loading is a combination of horizontal and torsional movements, and can be seen as a plane rigid-body motion.
3. An explicit pile-head displacement relationship of the grouped piles and static equilibrium equations of the pile cap were derived according to the concept of instantaneous center in a plane rigid-body motion.
4. The generalized  $p$ -multiplier proposed by Kong et al. (2019) is used in this approach to account for the horizontal interaction among the individual piles, which has a dominant effect on the response of the pile groups.
5. The coupling effect of the lateral resistance and torsional resistance of each pile was quantified using an empirical factor  $\beta$ .
6. An approximate equilibrium equation of the pile cap was derived to improve the computational efficiency in iteration.