



# Discrete element method study of hysteretic behavior and deformation characteristics of rockfill material under cyclic loading

## Keywords:

Granular material, Discrete element method (DEM), Plastic deformation, Cyclic loading, Hysteretic behavior

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# Research background and objective



## Primary concerns

The hysteretic behavior and accompanied strain accumulation

## Most study concerns

Dynamic responses of geomaterials and liquefaction of sandy soils

## Rare study cases

Deformation characteristics of geomaterials under low-frequency cyclic loading (such as reservoir storage and discharge)

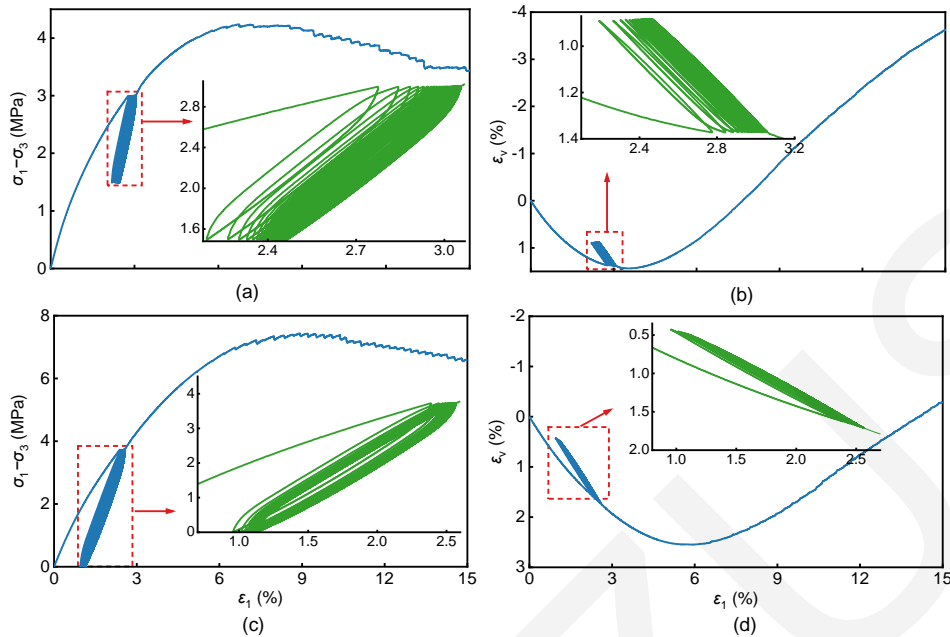
## Research objective

- deformation characteristics of rockfill material under cyclic loading
- hysteretic behavior from a macro and microscale perspective



Rockfill dam

# DEM cyclic loading tests



**Table 1 Simulation groups design**

Loading condition	Value
Confining pressure, $P$ (MPa)	0.5, 1.0, 1.5, 2.0
Stress level, $S_L$	0.25, 0.5, 0.7, 0.9
Amplitude of cyclic loading, $U_a$	0.25, 0.5, 0.75, 1.0
Number of cycles, $N$	50

Fig. 1 Evolution of shear stresses (a and c) and volumetric strains (b and d) for crushable granular materials under different cyclic loading conditions: (a and b)  $P=1.0$  MPa,  $S_L=0.7$ , and  $U_a=0.5$ ; (c and d)  $P=2.0$  MPa,  $S_L=0.5$ , and  $U_a=1.0$

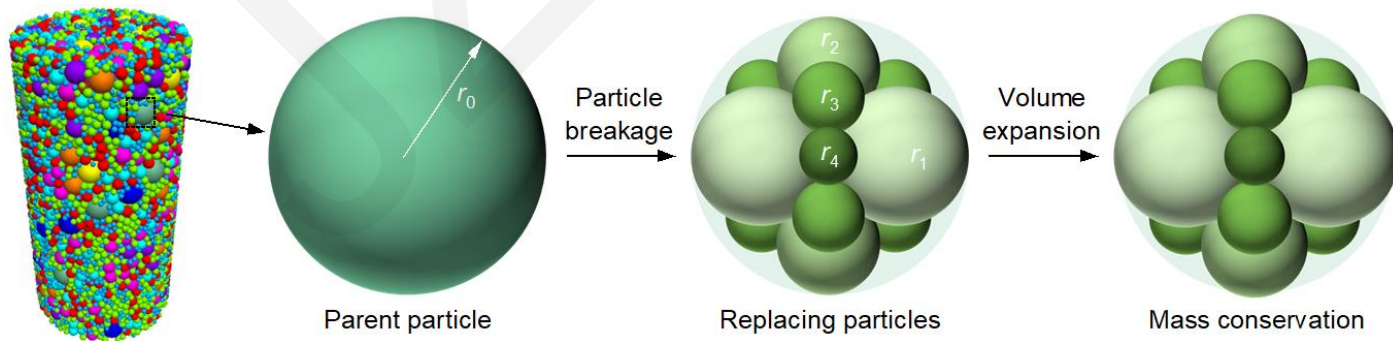


Fig. 2 Illustration of particle breakage modeling using fragment replacement method

# Hysteretic behavior from a microscale perspective

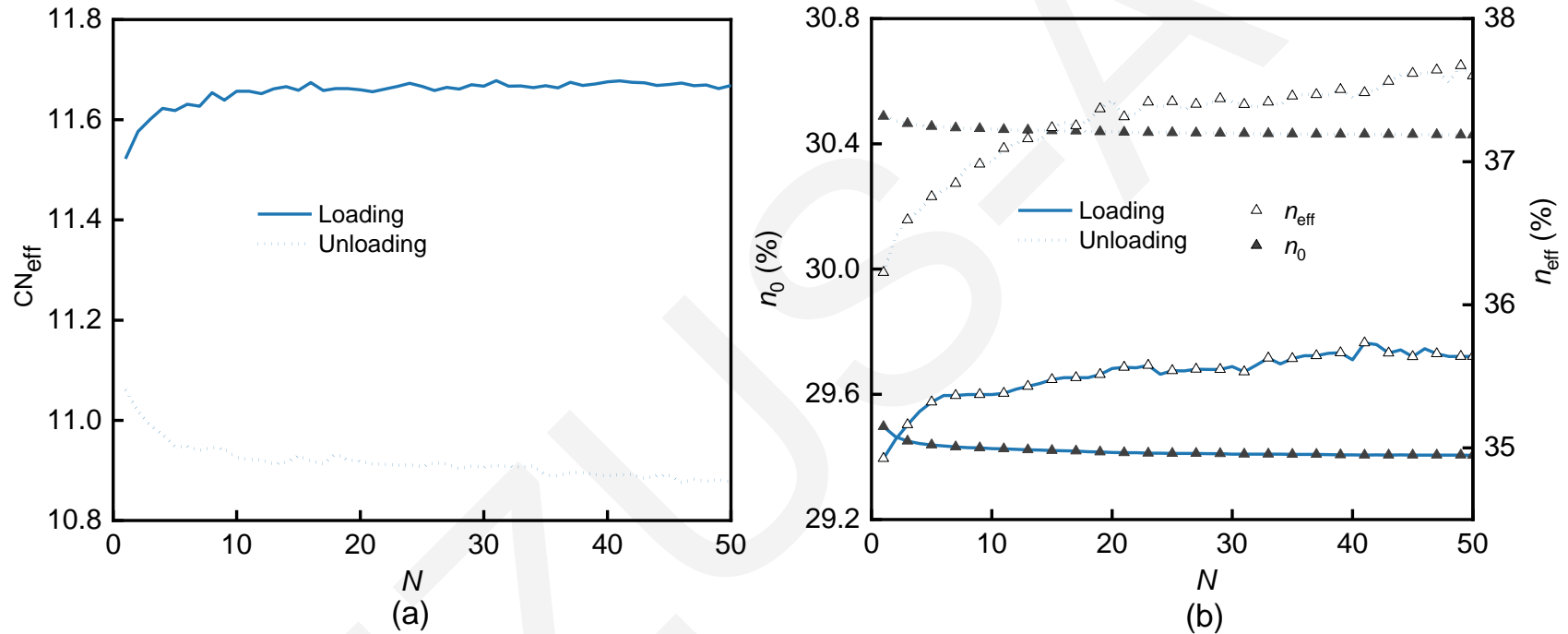


Fig. 3 Coordination number (a) and porosity evolution (b) of the specimen under different numbers of cycles  $N$  ( $P=1.5$  MPa,  $SL=0.7$ ,  $U_a=1.0$ )

- According to the evolution of effective coordination number, the number of effective particles changing into rattlers is more than that of rattlers turning into effective particles, which probably produces the residual strain
- The change rate of porosity reduces after a certain number of cycles, suggesting the volumetric deformation become less and the hysteresis loops coincide

# Evolution of resilient modulus

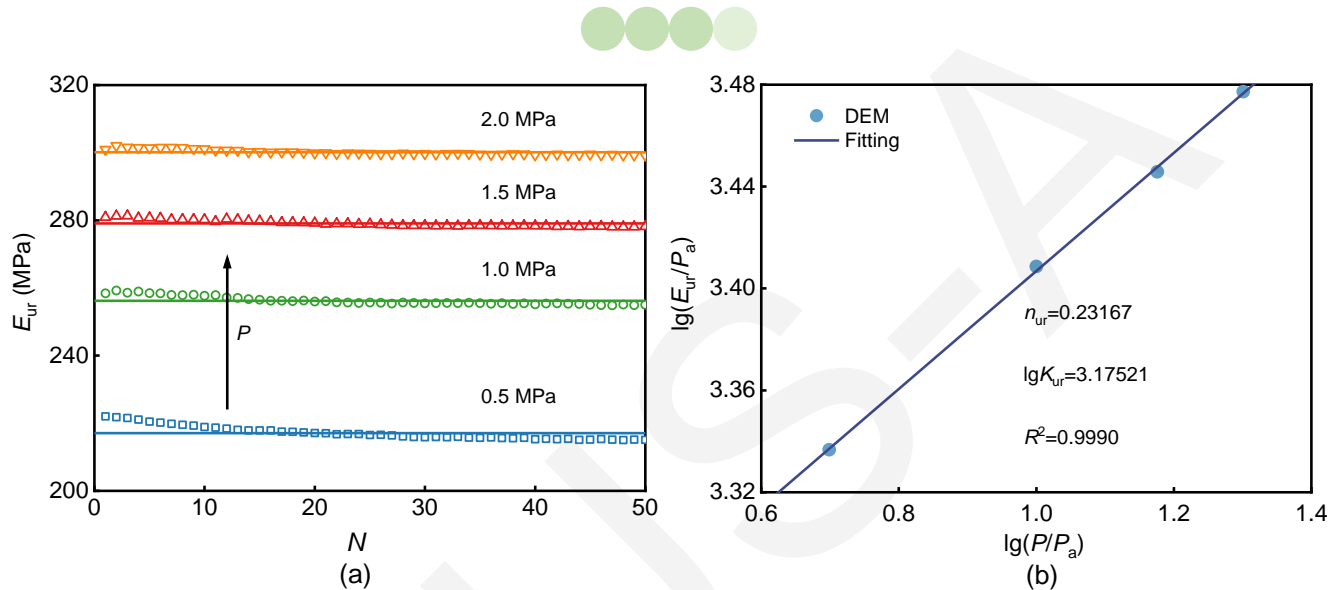


Fig. 4 Evolution of resilient modulus under different confining pressures ( $S_L=0.7$ ,  $U_a=0.5$ ): (a)  $E_{ur}$  evolve with  $N$ ; (b)  $E_{ur}$  evolve with  $P$

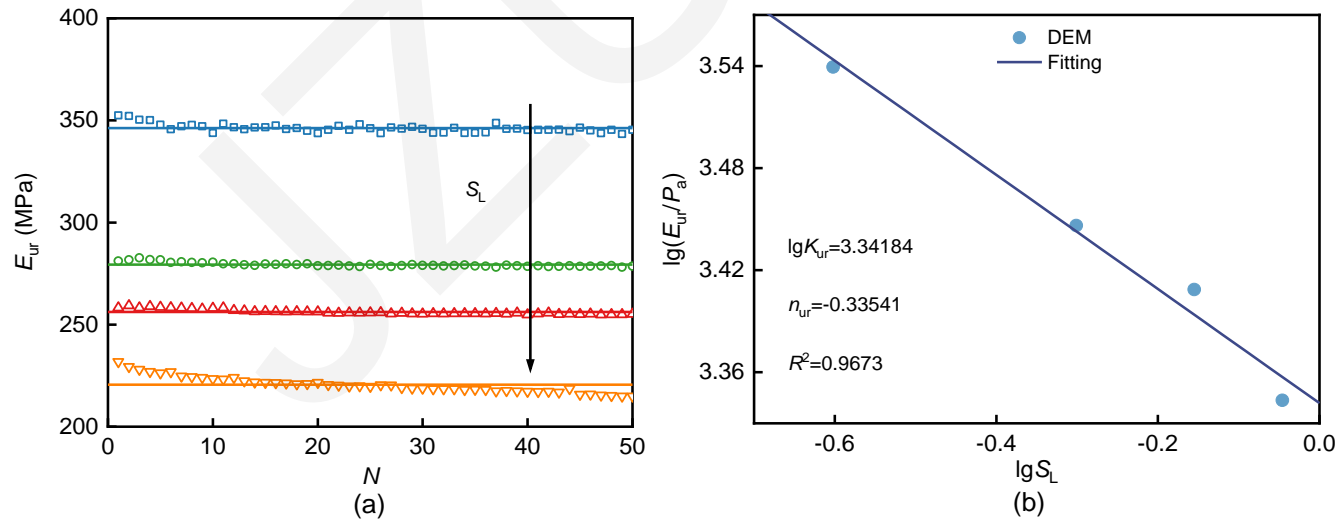


Fig. 5 Evolution of resilient modulus under different stress levels ( $P=1.0$  MPa,  $U_a=0.5$ ): (a)  $E_{ur}$  evolve with  $N$ ; (b)  $E_{ur}$  evolve with  $S_L$

# Evolution of resilient modulus

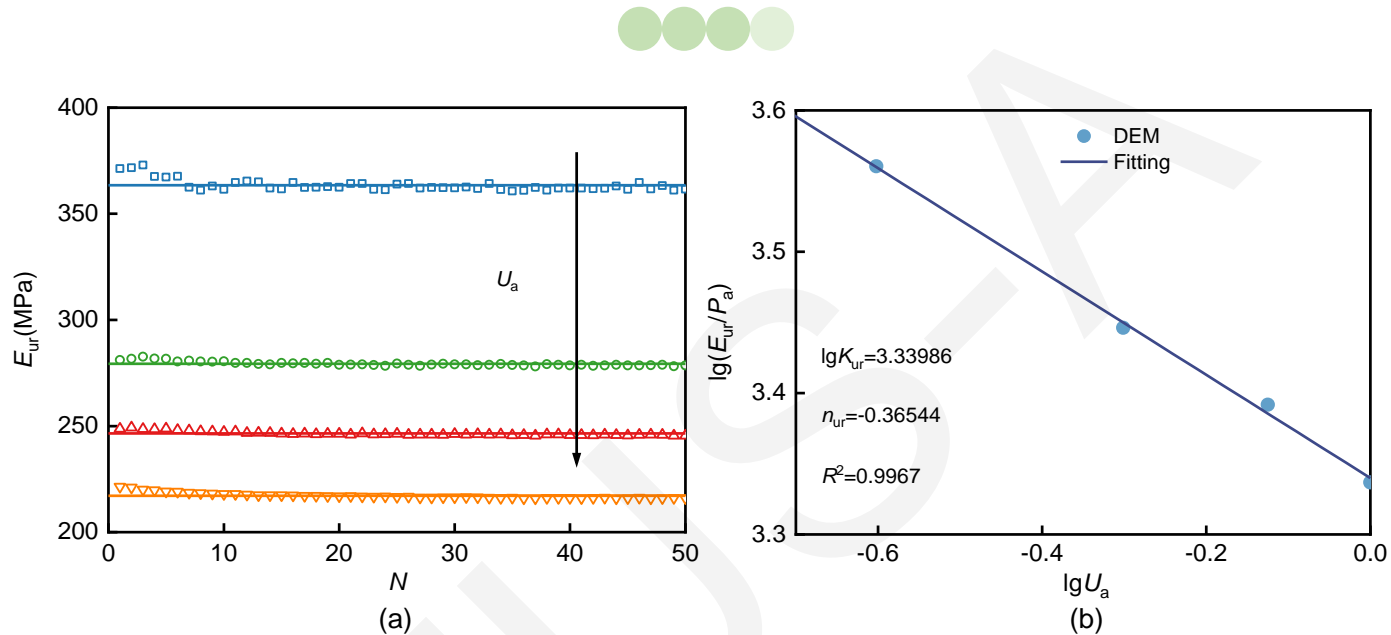


Fig. 6 Evolution of resilient modulus under different amplitudes of cyclic loadings ( $P=1.0$  MPa,  $S_L=0.5$ ): (a)  $E_{ur}$  evolve with  $N$ ; (b)  $E_{ur}$  evolve with  $U_a$

Considering the effects of confining pressure, stress level, and the amplitude of unloading, a reasonable evolution function of resilient modulus is proposed:

$$E_{ur} = \alpha_1 P_a \left( \frac{P}{P_a} \right)^{\alpha_2} S_L^{\alpha_3} U_a^{\alpha_4},$$

where  $P_a$  is the atmospheric pressure;  $\alpha_1$ ,  $\alpha_2$ ,  $\alpha_3$ , and  $\alpha_4$  are fitting parameters

# Conclusions



- **The hysteretic behavior of cyclic loading is analyzed from a microscale view**

Rattlers accumulated during each cyclic loading can cause the generation of a residual strain

The slowing down change in porosity during cyclic loading results in coincidence after a large number of cycles

- **The deformation characteristics under different cyclic loading conditions are discussed**

A function considering the effect of confining pressure, stress level, and the amplitude of unloading is proposed to describe the resilient modulus

## Prospectives

Programming and  
Verifying proposed  
resilient modulus

Investigating  
evolution of particle  
size distribution

Studying the effect  
of particle shapes  
under cyclic loading