

# Multi-scale analysis of the self-vibration of a liquid crystal elastomer fiber-spring system exposed to constant-gradient light

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## Key words:

Self-vibration; Constant-gradient light; Liquid crystal elastomer; Multi-scale method; Fiber; Spring oscillator

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# System Description

- The system consists of an LCE fiber, a spring, and a mass, where gradient light induces photothermal contraction in the fiber, leading to nonlinear self-oscillation.

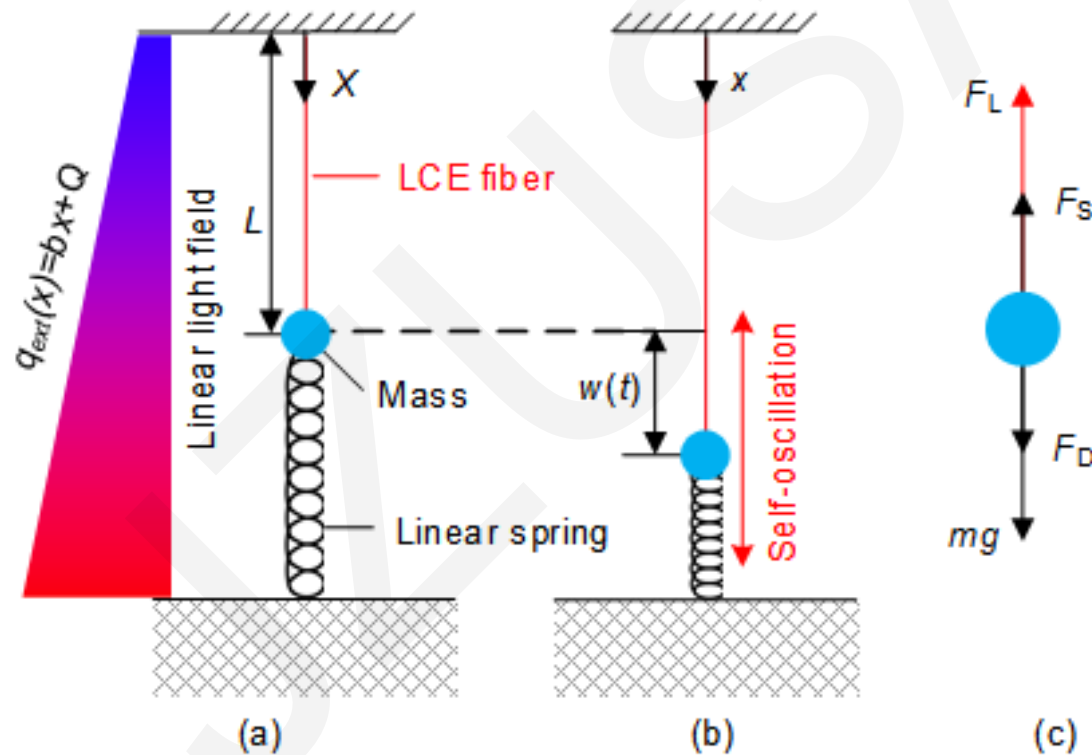
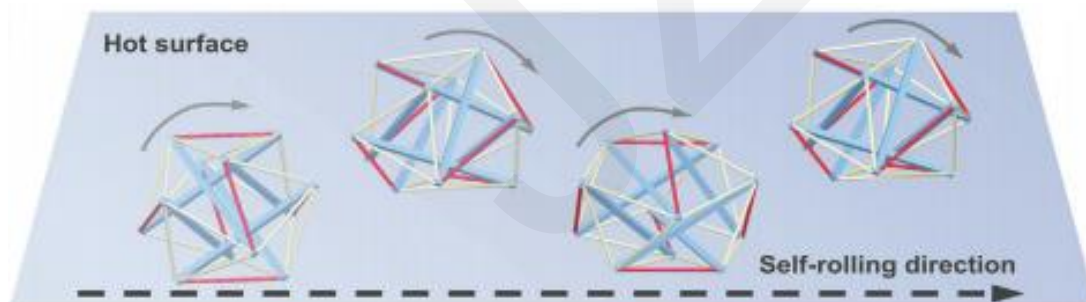


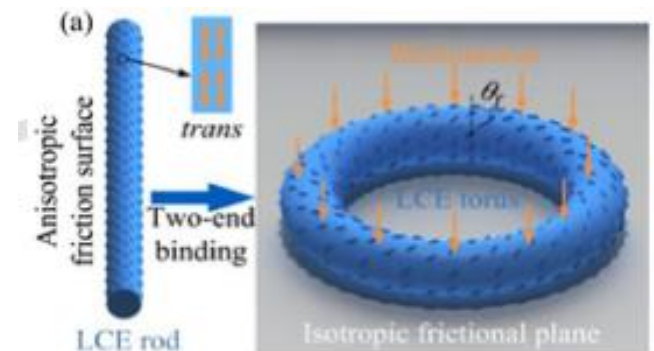
Fig. 1 System exposed to spatially-constant gradient light. (a) reference state; (b) current state; (c) force analysis

# Innovation Highlights

- Proposes an analytical modeling framework for self-vibrating systems based on the multi-scale method.
- Simulates and analyzes an LCE fiber-spring system under gradient light stimulation, revealing two motion regimes: static and self-vibrating.
- Systematically investigates how seven key parameters influence motion state, amplitude, and frequency, using the Hurwitz criterion.
- Confirms high consistency between analytical solutions and Runge-Kutta numerical results, significantly improving computational efficiency.



Nat. Mater. 23, 1728–1735 (2024).



Int. J. Mech. Sci. 281, 109584 (2024).

# Motion Regimes & Mechanism

## ■ Static and self-vibrating regimes

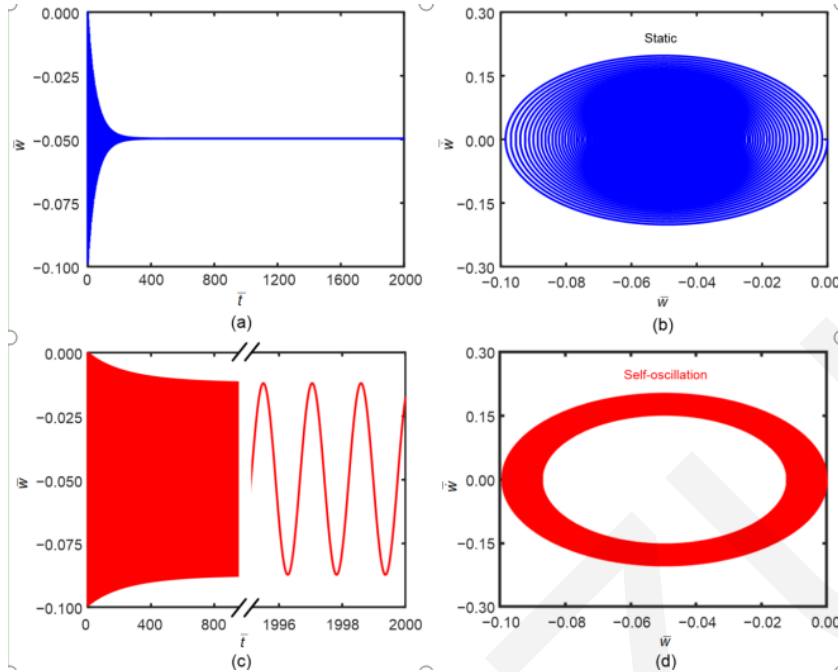


Fig. 2 Two motion regimes of the system.

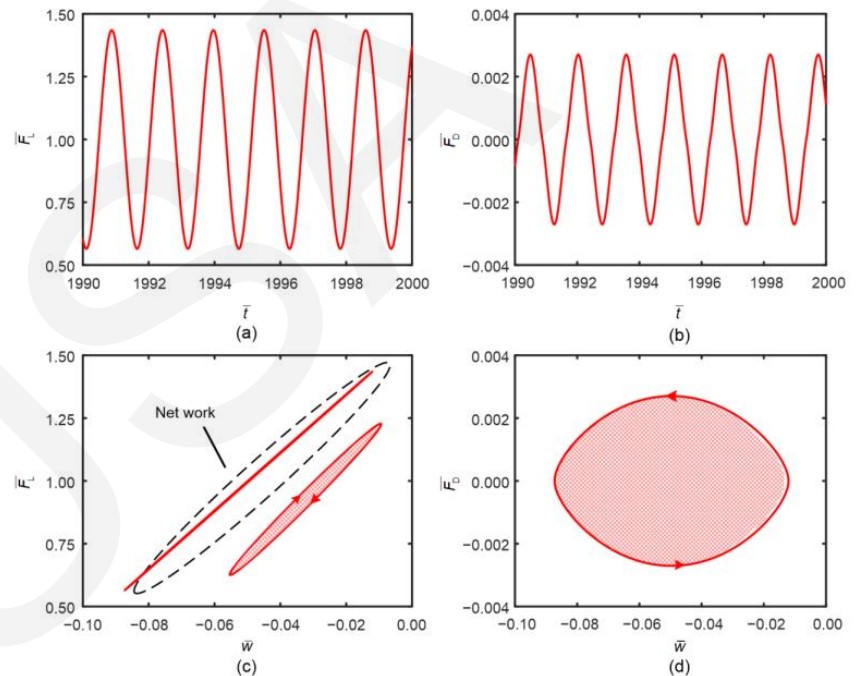
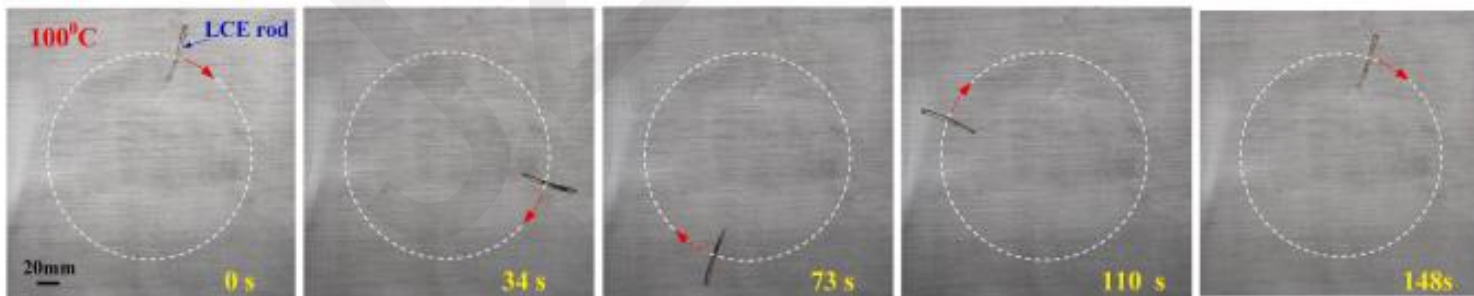
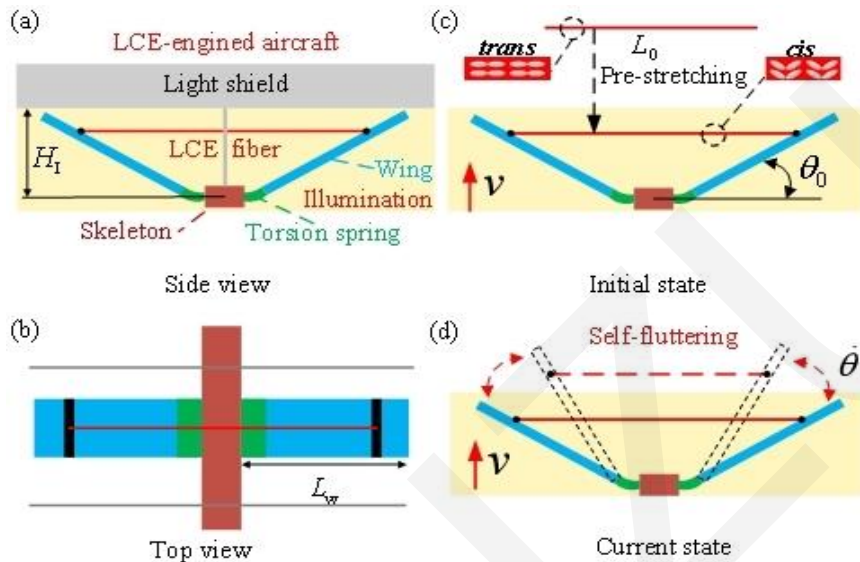


Fig. 3 Mechanism of self-vibration.



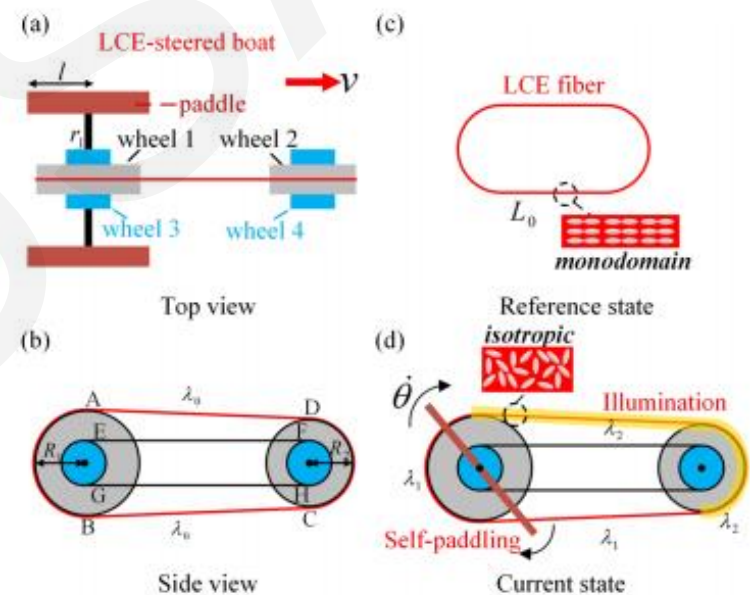
# Conclusions

- This study develops an analytical multi-scale approach to describe the self-vibration behavior of an LCE fiber-spring system under gradient light stimulation, offering a computationally efficient alternative to conventional numerical methods, and clarifies how system parameters modulate vibration regimes, amplitude, and frequency, with results validated against numerical simulations.



**Fig. 4 LCE-based self-fluttering system.**

Haiyang Wu, et al., 2024. Light-fueled self-fluttering aircraft with a liquid crystal elastomer-based engine. *Communications in Nonlinear Science and Numerical Simulation*, 132:107942.

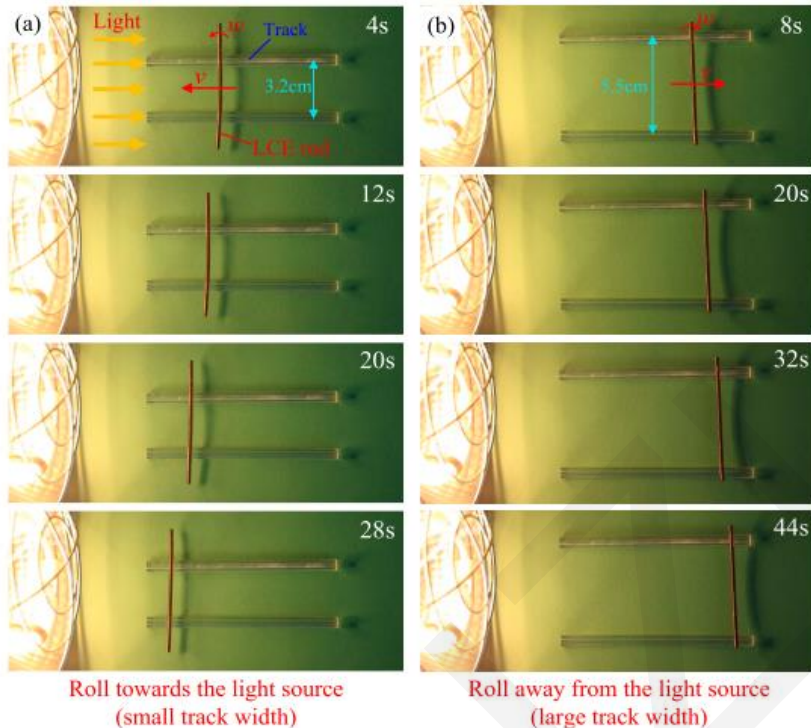


**Fig. 5 LCE-based self-paddling system.**

Haiyang Wu, et al., 2024. Modeling of a light-fueled self-paddling boat with a liquid crystal elastomer-based motor. *Physical Review E*, 109:044705.

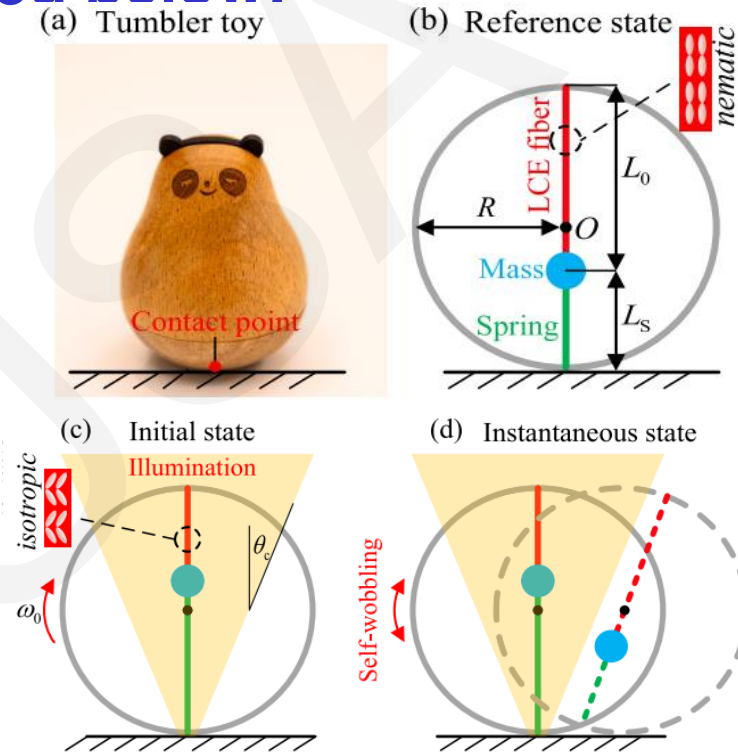
# Related Work

- Some other publications by the authors related to this research field are listed below:



**Fig. 6 Bidirectional self-rolling of the LCE rod under steady illumination.**

Haiyang Wu, et al., 2025. Mechanics of light-fueled bidirectional self-rolling in a liquid crystal elastomer rod on a track. *Chaos, Solitons & Fractals*, 191:115901



**Fig. 7 Schematic of LCE-steered self-wobbling tumbler.**

Haiyang Wu, et al., 2025. Modeling of a light-fueled liquid crystal elastomer-steered self-wobbling tumbler. *Chaos, Solitons & Fractals*, 191:115941.