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# A VHDL application for kinematic equation solutions of multi-degree-of-freedom systems

**Key words:** Multi-degree-of-freedom systems, Kinematics, Co-processor, Serial communication, Six-legged robot

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# Introduction

- As kinematic calculations are complicated, it takes a long time and is difficult to get the desired accurate result with a single processor in real time
- Designed systems are also complicated because they have many parts and cabling
- This paper presents the design and implementation of a hardware that will provide solutions to these problems
- This hardware is designed for a six-legged robot and has been working with servo motors controlled via the serial port
- This hardware has a co-processor for the calculation of kinematic equations and can be used together with the equipment that would reduce the electromechanical mess
- It is intended to be used as a tool which will accelerate the transition from design to application for robots

# Mechanical structure and kinematic equations

Denavit-Hartenberg parameters for three-joint legs

$i$	$\alpha_i$ (°)	$a_i$ (mm)	$d_i$ (mm)	$\beta_i$
1	0	0	0	$\beta_1$
2	90	60	0	$\beta_2$
3	0	80	0	$\beta_3$

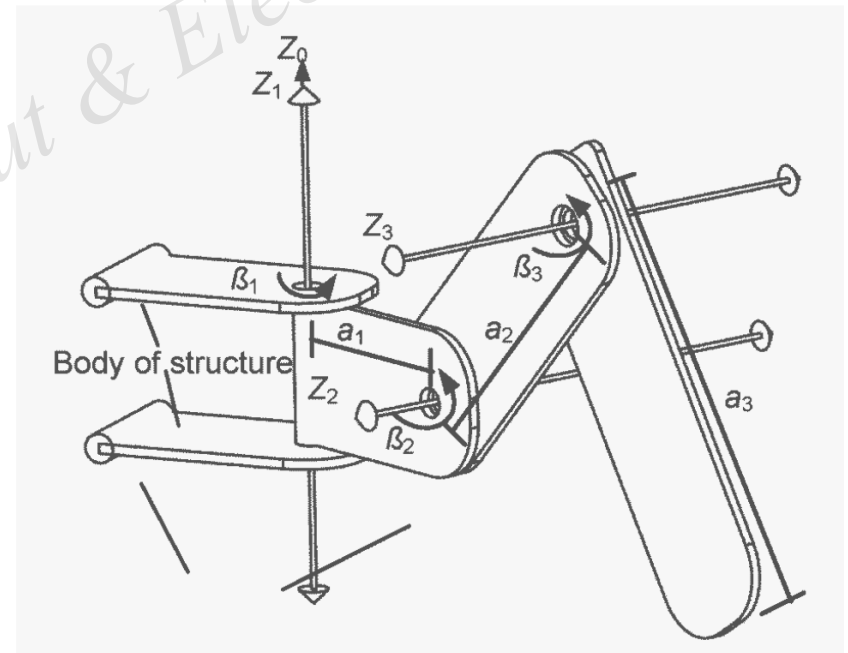
$$T_3^0 = \begin{bmatrix} c_{23} \cdot c_1 & -s_{23} \cdot c_1 & s_1 & c_1 (a_2 \cdot c_2 + a_3 \cdot c_{23}) \\ c_{23} \cdot s_1 & -s_{23} \cdot s_1 & -c_1 & s_1 (a_2 \cdot c_2 + a_3 \cdot c_{23}) \\ s_{23} & c_{23} & 0 & a_3 \cdot s_{23} + a_2 \cdot s_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$P_x = (d_2 + d_3) \cdot s_1 + a_2 \cdot c_1 \cdot c_2 + a_3 \cdot c_1 \cdot (c_2 \cdot c_3 - s_2 \cdot s_3)$$

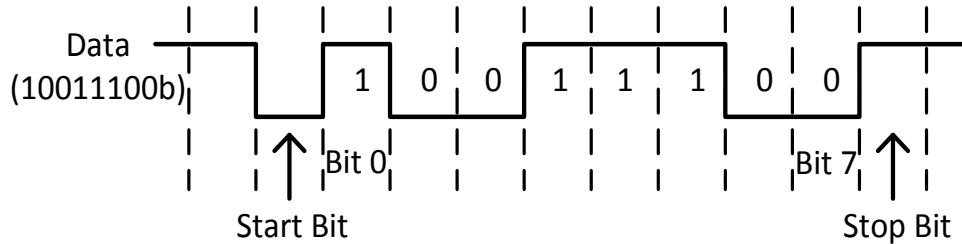
$$P_y = -(d_2 + d_3) \cdot c_1 + a_2 \cdot s_1 \cdot c_2 + a_3 \cdot s_1 \cdot (c_2 \cdot c_3 - s_2 \cdot s_3)$$

$$P_z = a_3 \cdot s_{23} + a_2 \cdot s_2$$

$$\beta_N = \arctan \left( \frac{s_i}{c_i} \right)$$



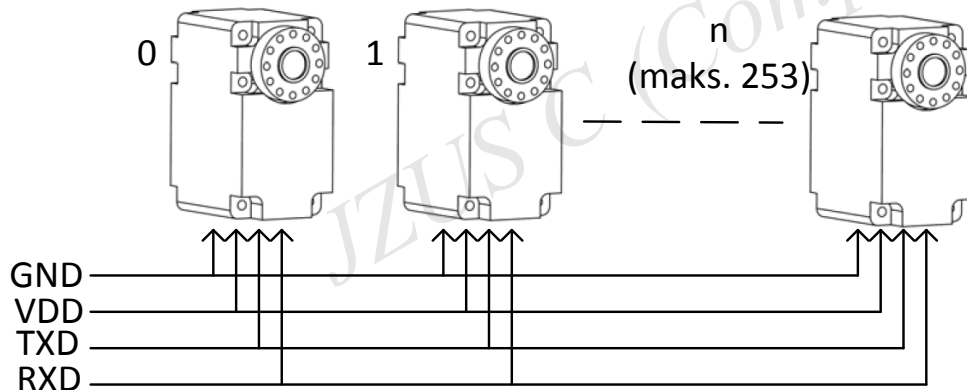
# Motors controlled via serial port



**Data transmission signal**

## Pin descriptions of motor connector

Pin number	Name	Description
1	GND	Electrical ground connection
2	VDD	Supply voltage
3	TXD	Transmitting line
4	RXD	Receiving line

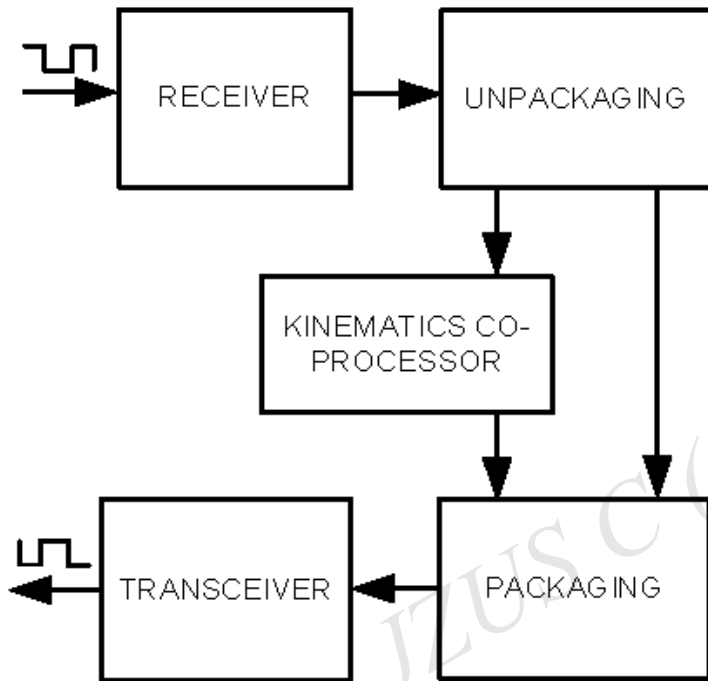


**Motor connections**

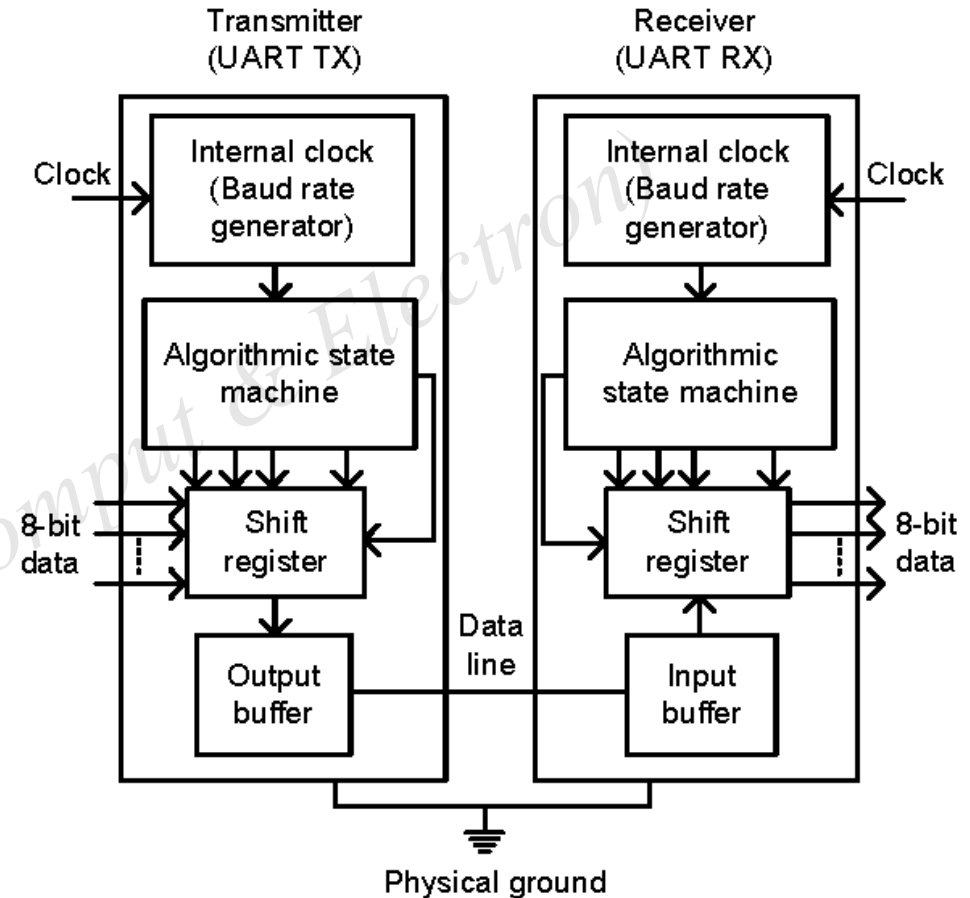
## Details of communication packet

	Header	Pack size	pID	CMD	Check Sum1	Check Sum2	Data [n]
Value	0xFF 0xFF	7-223	0-0xFE	1-9	-	-	-
Length (byte)	2	1	1	1	1	1	Maks. 216

# Recommended structure of chip

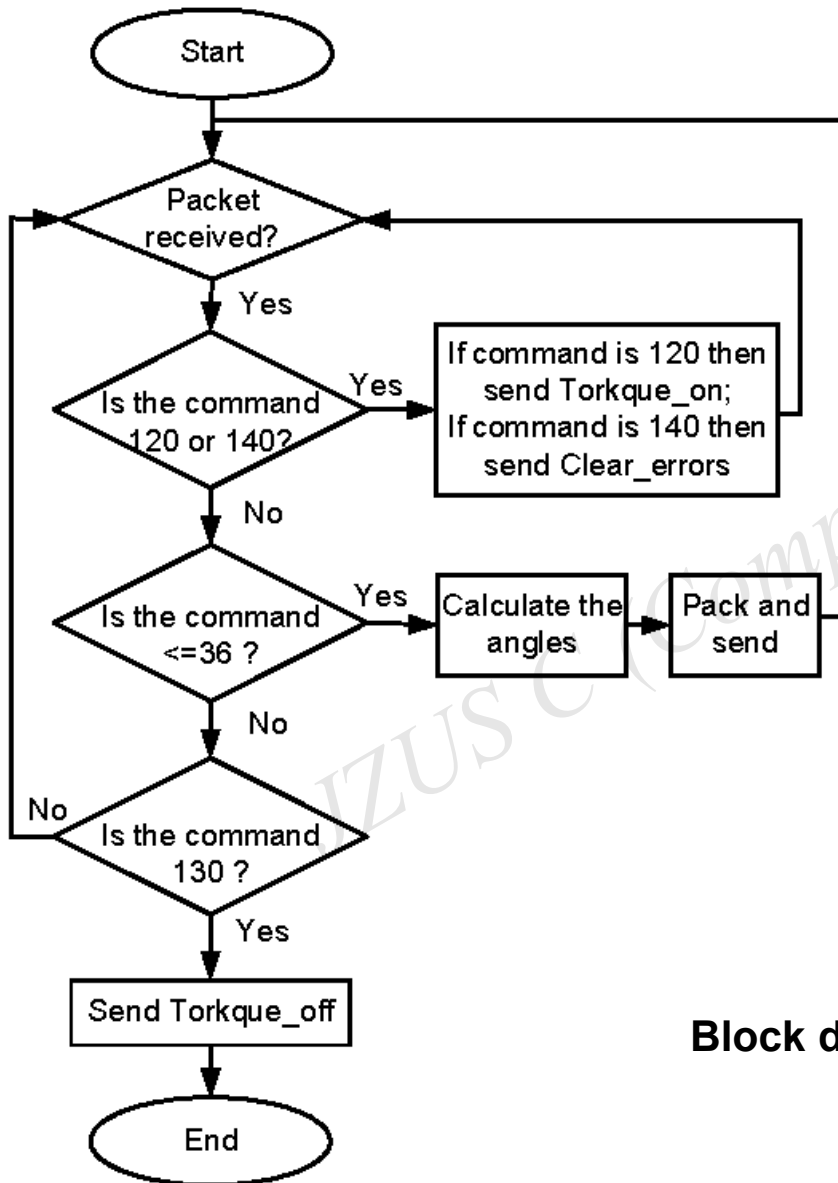


**Block diagram of design**



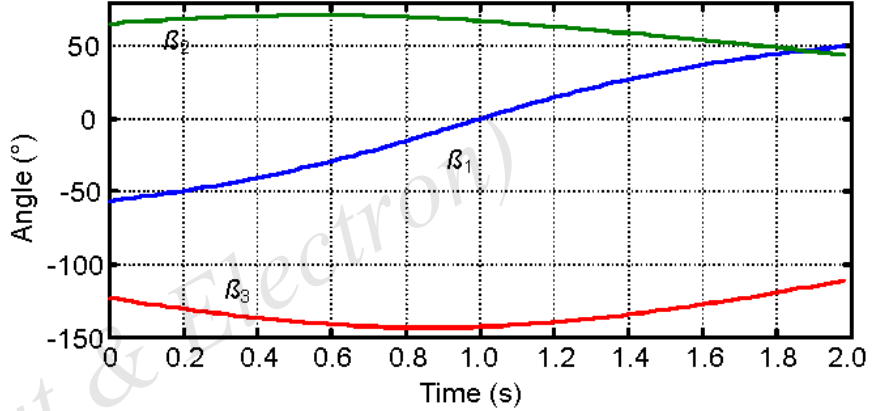
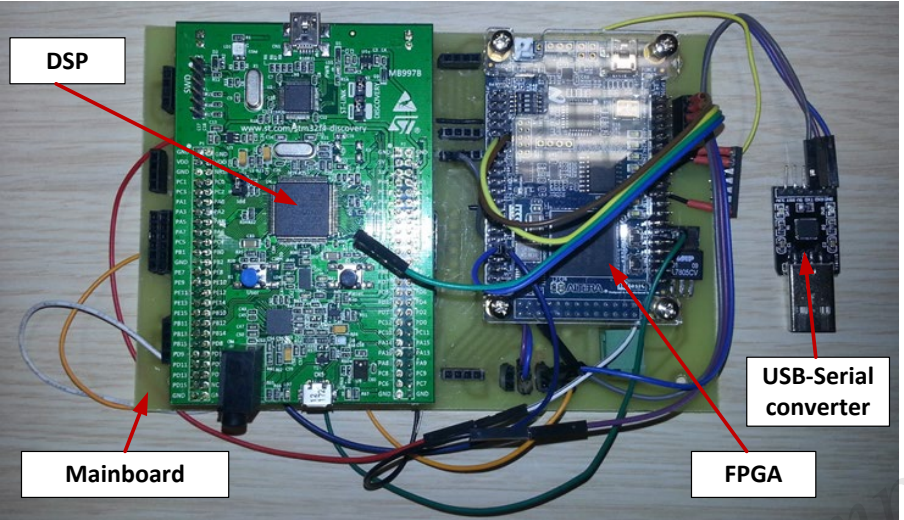
**Block diagram of transmitter and receiver**

# Recommended structure of chip

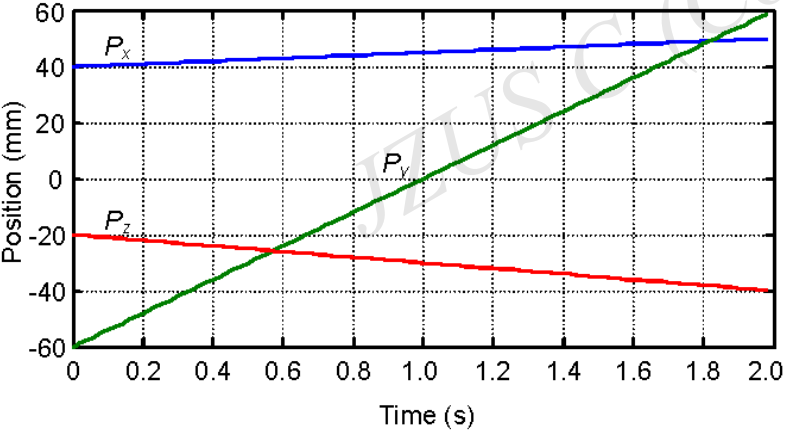


Block diagram of process

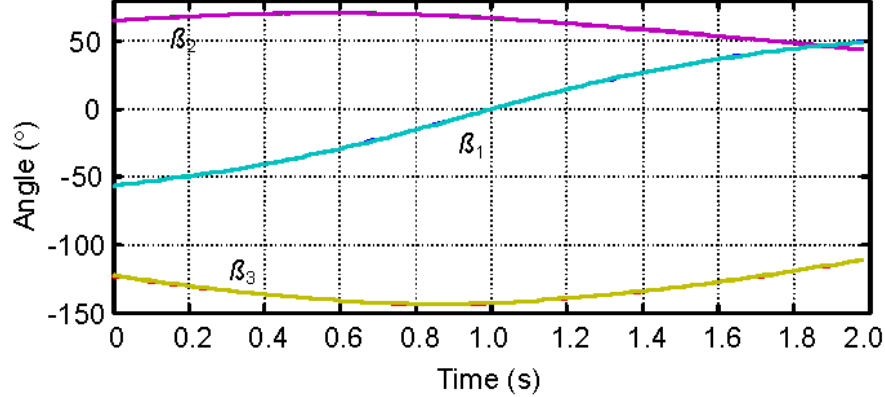
# Hardware test



Changes in joint angles



X, Y, Z positions of the foot



Comparison of the performed design's output signals with simulation

# Conclusions

- The designed hardware has a serial port and also a co-processor to perform kinematic calculations
- The application was performed on FPGA to meet the needs of real-time operation
- The designed hardware calculates the required joint angles to reach the foot positions received from the serial port. Then it sends the angles to the servo motors via the serial port
- Hardware has been developed for a hexapod robot. However, it can be used easily for another robot by changing the kinematic equations solved by the co-processor
- Using this hardware, the transition will be faster from design to implementation in experimental or commercial studies and the load on the main processor will be reduced