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A framework for analysis of extended fuzzy logic

Key words: Extended fuzzy logic, Fuzzy logic, *f*-Transformation, S-answer, Validity

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Introduction

- Fuzzy logic is a fascinating and dynamic field of study and research.
- What remains widely unrecognized is that, results in fuzzy logic carry a necessary condition of being provably valid.
 Many real world applications do not satisfy this condition.
 The validity term is added to fuzzy logic to meet this condition, which leads to extended fuzzy logic (FLe).

Objective of this study

Studying FLe-based reasoning in mathematical detail

Proving structural isomorphism between the answers and their validities

Proving the representation theorem about problems in *C* and solutions in *f*-*C*

To show that in the presence of imperfect information, the solutions obtained are near the true ones when applying FLe

FLe's basic terminology

- *f*-Transformation: a map of one-to-many.
- Validation principle: *f*-*p* has a high validity index.
- Cointensive assumption: *f*-*C* is close-fitting to its true prototype, *C*.
- **P/I principle:** h(f-C)f = f-h(C).
- *S*-answer: the centroid of the relevant *f*-answer.
- **A-granule:** the smallest granule that contains the *f*-transform of the object.

Major results (I)

Theorem 1 Suppose *Q* is an A-granule, f- $s_i(P)$ the *f*-answer of problem *P*, s_i the *S*-answer, v_{si} a validity measure, *d* a bounded positive quantity, f- $s_i(P)|_{v_{s_i(P)}} = s_i(P)$, i=1, 2 and $||s_1(Q)-s_2(Q)|| < d$. Then $||s_1(P)-s_2(P)|| < f$ -*d*, where *f*-*d* is the *f*-transform of *d* and is bounded and positive.

Major results (II)

Theorem 2 Suppose Q is an A-granule, v a validity measure, f- $s_i(P)$ the f-answer of problem P, s_i the S-answer, $f - s_i(P) \Big|_{V_{s_i(P)}} = s_i(P), S_i$ the solution in the C-space, $F_Q(S_i)$ the functional of S_i with respect to Q such that $F_Q(S_i) = f - s_i(Q) \Big|_{v_{s_i(Q)}} = s_i(Q)$, and $v(||F_Q(S_1) - F_Q(S_2)|| < d) > \delta$, where i=1, 2, and δ , d are positive quantities and are bounded. Then there exists a positive quantity ρ different from δ such that $v(||s_1(P) - s_2(P)|| \le d) \ge \rho$.

Major results (III)

Theorem 3 For a problem P on C through ftransformation, there exists a function s(P) defined in f-C that is the centroid (precisiated) of the f-transform of S(P), where S(P) is the solution of problem P on C and s(P) is the best approximation of S(P) in terms of similarity.