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# A dynamic $K$ -nearest neighbor method based on strong access point credibility for indoor positioning

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**Abstract:** High-precision indoor positioning offers valuable information support for various services such as patient monitoring, equipment scheduling management, and laboratory safety. A traditional indoor positioning technology, fingerprint indoor positioning, often employs the  $K$ -nearest neighbor (KNN) algorithm to identify the closest  $K$  reference points (RPs) via the received signal strength (RSS) for location prediction. However, RSS is susceptible to environmental interference, leading to the selection of RPs that are not physically the closest to the user. Moreover, using a fixed  $K$  value is not the optimal strategy. In this work, we propose a novel approach, the dynamic  $K$ -nearest neighbor method based on strong access point (AP) credibility (SAPC-DKNN), for indoor positioning. In SAPC-DKNN, we leverage prior knowledge of RSS path loss and employ the RSS fluctuation area to quantify the significance of different APs. We integrate the similarity of AP sets within the range of strong APs and formulate a weighted distance metric for RSS based on the credibility of strong APs. Additionally, we introduce a dynamic  $K$ -value algorithm based on neighbor density (ND-DKA) for the automatic optimization of the  $K$  value for each test point. Experimental evaluations conducted on three datasets demonstrate that our method significantly reduces the average positioning error by 15.41%–64.74% compared to the state-of-the-art KNN methods.

**Key words:** RSS path loss; Fingerprint indoor positioning; Dynamic  $K$ -nearest neighbor  
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## 1 Introduction

The rapid progress of wireless communication technology has led to increased attention concerning location-based services that rely on positioning technology (Liu H et al., 2007; Gu et al., 2009; Song et al., 2019). These services are ubiquitous in daily life. They are found in places like roads, playgrounds, underground parking lots, shopping malls, laboratories, and classrooms, and play a vital role in supporting travel navigation, scheduling equipment, ensuring laboratory and personnel safety, etc. Although the Global Navigation Satellite System (GNSS) excels in outdoor environments (Hegarty

and Chatre, 2008), its signals are influenced by factors such as geomagnetism, weather, and building obstructions in indoor settings, which cause signal distortion and hinder the provision of accurate and reliable positioning information (Nguyen et al., 2024; Zhao et al., 2024). In the current landscape, effective indoor positioning is attainable through technologies like Wi-Fi (Yang and Shao, 2015; Cha and Lim, 2022), Bluetooth (Liu S et al., 2014; Pu and You, 2018), ZigBee (Dong ZY et al., 2019), radio frequency identification (RFID) (Ni et al., 2003; Chon et al., 2004), and ultra-wideband (UWB) (Yu et al., 2021). Wi-Fi, in particular, stands out due to its low power consumption, high real-time performance, low deployment cost, and robust environmental adaptability, making it popular for wide application in

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indoor positioning and the Internet of Things (Ma J et al., 2008; Salamah et al., 2016; Dong YH et al., 2022). Due to the widespread deployment of Wi-Fi infrastructure in indoor settings, indoor positioning methods based on Wi-Fi are commonly categorized into two types: ranging-based and fingerprint-based (Rusli et al., 2016; Nguyen et al., 2023). In ranging-based methods, the received signal strength (RSS) value is typically employed to compute the distance between the test point (TP) and the access point (AP) using the RSS propagation loss model (Ciu-rana et al., 2007; Dag and Arsan, 2018). However, these methods are susceptible to environmental variations and lead to increased estimation errors due to changing obstacles. In contrast, the fingerprint positioning algorithm does not determine the target location by estimating the distance between the TP and the AP. Instead, it estimates the location by assessing the RSS distance between the TP and the offline-collected database (Xia et al., 2015; Alitalessi et al., 2023). During the offline phase, the fingerprint database is created and stores the received signal strength indicator (RSSI) and the corresponding coordinates of all APs collected at each reference point (RP) using mobile devices. In the online phase of position estimation, the mobile device gathers the user's current location information, and the RP information in the database is used to estimate the location of the target point with the highest probability. The appeal of the fingerprint-based algorithm lies in its capacity to enhance positioning accuracy without incurring additional hardware costs, making it a subject of interest for many scholars (He and Chan, 2016; Ren et al., 2023; Ayinla et al., 2024).

Numerous fingerprint-based indoor positioning methods, including the  $K$ -nearest neighbor (KNN) algorithm (Sadowski et al., 2020; Chen et al., 2022), deep learning (Nabati and Ghorashi, 2023; Arslantas and Okdem, 2024), Bayesian probability method (Madigan et al., 2005), support vector machine (SVM) (Brunato and Battiti, 2005), and clustering (Le et al., 2021; Lin et al., 2023), have been proposed. The KNN method, compared with deep learning and SVM methods, demonstrates acceptable positioning accuracy with a simple structure and low computational complexity. As a result, our research focuses on methods based on KNN. Many improved KNN approaches have been developed to enhance positioning accuracy (Lin et al., 2023). These enhance-

ments involve changes to the RSS distance measurement method and the conversion of the traditional Euclidean distance (ED) to alternative metrics, such as cosine distance and Spearman distance (Peng et al., 2016; Xie et al., 2016). However, these improved methods do not consider the positioning errors caused by features. Subsequently, Zou et al. (2017) proposed the use of the signal trend index as a new weighting scheme for weighted KNN (WKNN), which improved positioning accuracy. Nevertheless, an exponential relationship exists between the RSS and physical distance, and relying solely on RSS similarity cannot accurately reflect the physical distance between the TP and RP (Zhang H et al., 2022). Addressing this, Hu XK et al. (2015) suggested using the Jaccard coefficient to calculate AP set similarity as a weight, effectively mitigating the physical estimation errors caused by RSS instability. However, they overlooked the sequence of AP strength and the relationship between the RSS and physical distance.

In the fingerprint positioning method grounded in KNN, many researchers adopt a uniform  $K$  value across all test samples to derive prediction outcomes directly. For instance, Li et al. (2015) employed a  $K$  value of 2, whereas Hu XK et al. (2015) opted for 3. Discrepancies like these primarily stem from varying network environments. However, such static KNN approaches might overlook opportunities to enhance accuracy through flexible adjustment of the  $K$  value. Thus, several scholars have delved into determining the optimal  $K$  through extensive experimentation. For instance, Ma R et al. (2015) identified the optimal  $K$  as 4, whereas Torres-Sospedra et al. (2015) found it to be 13. Nevertheless, this approach demands substantial human effort, and further enhancements in accuracy are warranted. Studies have revealed that customizing the  $K$  value for individual test samples can lead to enhanced positioning performance (Umair et al., 2014). Consequently, some scholars have established a threshold criterion, incorporating only new neighbors if the distance between the user's RSS vector and the neighbor point's fingerprint falls below the threshold (Hu JS et al., 2018, 2019). Moreover, constraints based on the physical distance are imposed (Costa et al., 2006; Lee et al., 2016). However, determining these thresholds also necessitates extensive experimentation.

Existing enhanced KNN methods (Hoang et al., 2018; Zhang J and Mao, 2022) encounter certain

challenges:

1. The conventional weighted KNN method overlooks the prior knowledge of RSS path loss and the significance of features at the AP level. It relies solely on RSS similarity to measure the physical distance, which is suboptimal. Because RSS weakens over time and distance, the physical distance between the RP and AP determines the noise level of the currently received signal. Signal fluctuation varies for RPs at different locations, and the degree of fluctuation is inconsistent. Stronger signals received by the AP result in less noise. Hence, emphasis should be placed on the order and similarity of strong APs. Consequently, relying solely on RSS similarity during the position estimation stage leads to larger errors.

2. The performance of KNN methods is influenced by the choice of the  $K$  value (Oh and Kim, 2018). When the  $K$  value is small, the positioning result is susceptible to interference from noise points, leading to increased errors. Conversely, when the  $K$  value is large, adjacent points may encompass numerous points of different categories, also contributing to error escalation. Hence, conventional static KNN methods may overlook opportunities for enhancing accuracy by adjusting the  $K$  value. Empirical assignment of  $K$  values fails to adequately address actual requirements across diverse network environments. Manually determining the optimal  $K$  value for individual samples proves challenging and resource-intensive. Moreover, many dynamic KNN (DKNN) approaches entail additional threshold settings, necessitating extensive experimentation for acquisition.

To overcome the challenges mentioned above, we propose a DKNN method based on strong AP credibility for indoor positioning (SAPC-DKNN). This method leverages prior knowledge of RSS path loss, uses the relationship between the physical distance from the RP to AP and the RSS, quantifies the credibility of different RSS values, and integrates the similarity of strong AP levels. Notably, SAPC-DKNN eschews fixed  $K$  values or the design of thresholds for dynamic  $K$  adjustment; instead, it adaptively selects the RP based on the improved RSS distance measurement results and the concept of neighbor density. In contrast to prior studies (Hu XK et al., 2015; Zhang H et al., 2022), SAPC-DKNN directly incorporates prior knowledge of RSS atten-

uation, theoretically quantifies the credibility of different RSS values, and considers two key aspects of the strong AP level: order and similarity. This method exhibits strong robustness and does not require the collection of challenging-to-obtain information such as the user's walking speed, direction, and time. Achieving favorable positioning results across various environments is feasible using only the collected RSS data.

## 2 Related works

The nearest neighbor (NN) algorithm has been widely applied in indoor positioning. Bahl and Padmanabhan (2000) introduced the RADAR system, using wireless local area network (LAN) for indoor positioning and the NN algorithm to determine the coordinates of the target point. Experiments substantiated that this method achieved higher positioning accuracy than the model propagation method under similar conditions. Following this work, Wu et al. (2009) investigated two memoryless positioning techniques, KNN and naive Bayes, and compared them with the trilateration method across various scenarios. Experimental results indicated that KNN is the simplest and most accurate positioning method. However, these methods may not consistently yield the optimal results. Thus, some enhanced KNN algorithms were proposed to improve indoor positioning effectiveness (Chen et al., 2022).

Furthermore, some studies have investigated improved methods for RSS distance measurement. Xie et al. (2016) introduced the use of Spearman distance to refine the KNN algorithm, demonstrating improved positioning performance through simulations. Peng et al. (2016) proposed the Sim-KNN and IW-KNN methods, with the Sim-KNN method incorporating both ED and cosine similarity to gauge fingerprint similarity. There are also weighting methods applied at the RSS value level; for instance, Zou et al. (2017) used the RSS trend index as a new weighting scheme for weighted KNN (WKNN), resulting in enhanced positioning accuracy. Subsequently, some scholars integrated historical information into KNN, leading to a notable improvement in positioning accuracy (Hoang et al., 2018; Zhang H et al., 2022). Although experimental results revealed that these methods surpassed traditional KNN in terms of positioning accuracy, they

fall short of optimal performance because they neglect prior knowledge of RSS attenuation and AP-level information.

Liu SY et al. (2022) observed that adjusting the parameter  $K$  can markedly enhance positioning performance. In comparison to the NN method, varying  $K$  for different TPs can yield a positioning performance improvement of more than 45%. Subsequently, scholars explored algorithmic research on  $K$  value selection in KNN. For instance, Oh and Kim (2018) introduced an adaptive KNN algorithm, adjusting the  $K$  value based on the ED between the target position and the fingerprint database. By considering only RPs within a specific ED range, positioning accuracy was improved by more than 30%. Umair et al. (2014) proposed a DKNN method that sorts the values based on the difference in ED and sets a threshold to derive a dynamic  $K$  value, which proved more accurate than the traditional method. Costa et al. (2006) presented an adaptive approach for establishing thresholds in neighbor selection within sensor networks. However, their consideration was limited to the distance between sensors, and they found that a two-stage selection algorithm for neighboring sensors was inadequate. Consequently, Lee et al. (2016) introduced the DKNN method, which determines the optimal  $K$  value by accounting for changes in topology and distance among NNs.

Although the aforementioned DKNN methods significantly reduce positioning errors, their approaches require the introduction of new manually adjusted parameters, which increases labor cost and optimization difficulty. In this work, we propose a novel improved DKNN indoor positioning method, integrating prior knowledge of RSS attenuation and AP-level information to achieve more accurate prediction.

### 3 Our method

Our method is divided into two parts: (1) strong AP weighted distance measurement method and (2) density-based dynamic  $K$ -value algorithm.

#### 3.1 Strong AP weighted distance measurement method

The path loss model for estimating RSS is characterized using a logarithmic attenuation model

(Latif and Parasuraman, 2022), that is,

$$\text{RSS} = \text{RSS}_0 - 10n \lg d, \quad (1)$$

where  $\text{RSS}_0$  is the RSS at a distance of 1 m from the AP,  $n$  is the path attenuation coefficient, ranging from 2 (free space) to 6 (complex indoor environment) (Latif and Parasuraman, 2022), and  $d$  is the distance from the RP to the AP.

When there are two RPs at the same location but at different times, the RSS from the same AP is denoted as  $\text{RSS}_1$  and  $\text{RSS}_2$ . The RSS change,  $\Delta\text{RSS}$ , is then represented as

$$\Delta\text{RSS} = \text{RSS}_1 - \text{RSS}_2 = 10 \lg(n_1 - n_2), \quad (2)$$

where  $n_1 - n_2$  consistently maintains a specific distribution over time, whereas  $\Delta\text{RSS}$  and  $d$  exhibit a positive correlation (Jin et al., 2015). Consequently, when a particular RP is distant from a specific AP, a smaller RSS corresponds to a larger  $d$  and  $\Delta\text{RSS}$ . These parameters indicate heightened signal fluctuations and increased noise at that location, diminishing the credibility of the RSS signal under the corresponding AP. Additionally, scholars have highlighted that RSS similarity inadequately reflects the proximity of locations (Zhang H et al., 2022). Hence, relying solely on RSS measurements for distance assessment may not accurately depict the physical closeness of two points. This underscores the importance of prioritizing attention on the AP with robust signals.

We introduce a method that employs the RSS fluctuation area as AP credibility to account for the significance of the RSS corresponding to a single AP. If the strongest signal  $\text{RSS}_{\text{stro}}$  at the current RP is identified, the maximum and minimum distances ( $d_{\text{stro}}^{\max}$  and  $d_{\text{stro}}^{\min}$ ) of the RP from the corresponding AP can be determined by Eq. (1):

$$d_{\text{stro}}^{\max} = 10^{\frac{\text{RSS}_0 - \text{RSS}_{\text{stro}}}{10n_{\min}}}, \quad (3)$$

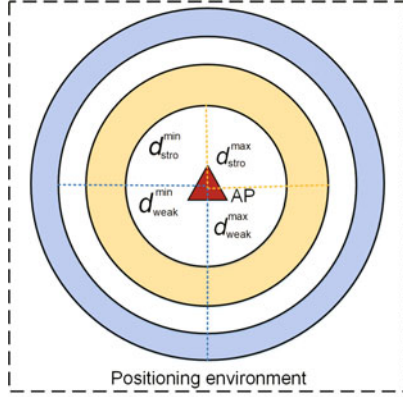
$$d_{\text{stro}}^{\min} = 10^{\frac{\text{RSS}_0 - \text{RSS}_{\text{stro}}}{10n_{\max}}}, \quad (4)$$

where  $\text{RSS}_0$  is a constant value, and we designate the maximum RSS in the database as  $\text{RSS}_0$ .  $n_{\min} = 2$ ,  $n_{\max} = 6$ . By using  $d_{\text{stro}}^{\min}$  and  $d_{\text{stro}}^{\max}$  as radii, the fluctuation space  $S_{\text{stro}}$  of  $\text{RSS}_{\text{stro}}$  can be derived (represented by the area of the yellow circle in Fig. 1):

$$S_{\text{stro}} = \pi((d_{\text{stro}}^{\max})^2 - (d_{\text{stro}}^{\min})^2). \quad (5)$$

As illustrated in Fig. 1 and according to Eqs. (3) and (4), the distance from  $\text{RSS}_{\text{weak}}$  (weaker than

$RSS_{stro}$ ) to the AP can be derived. The area  $S_{weak}$  (in blue) of the ring bounded by it can be determined from Eq. (5). Comparing the areas of the blue and yellow rings ( $S_{weak} > S_{stro}$ ), it is evident that as  $n$  remains constant, larger RSS values correspond to smaller RSS fluctuation spaces for the respective APs, indicating higher credibility of the AP.



**Fig. 1** RSS fluctuation range under strong and weak APs.  $d_{stro}^{min}$  and  $d_{stro}^{max}$  (yellow dotted lines) are the radii of the inner and outer circles of the yellow ring, representing the minimum and maximum distances from the RP of the strong signal ( $RSS_{stro}$ ) to the AP, respectively.  $d_{weak}^{min}$  and  $d_{weak}^{max}$  (blue dotted lines) are the radii of the inner and outer circles of the blue ring, representing the minimum and maximum distances from the RP of the weak signal ( $RSS_{weak}$ ) to the AP, respectively. AP: access point; RP: reference point; RSS: received signal strength. References to color refer to the online version of this figure

The traditional KNN method frequently uses the ED of the RSS to ascertain the physical proximity between two points. Nevertheless, it is acknowledged that RSS similarity alone may not completely convey the physical distance (Zhang H et al., 2022). In response to this limitation, certain researchers have suggested employing the Jaccard coefficient to assess the difference in AP sets for estimating the physical location (Hu XK et al., 2015). Motivated by this insight, we assemble a set comprising corresponding APs with the strongest signal and subsequently perform set similarity calculations between the points to be measured and RPs. Diverging from previous work (Hu XK et al., 2015), which exclusively considered APs with signals, our approach incorporates the order of RSS signal strength. Given the RSSs for a TP and RP, along with their AP IDs, we sort the RSSs. This sorting process arranges the RSSs from strong to weak, accompanied by their corresponding

AP (ID) sequences denoted as  $\mathbf{L}_{tp}$  and  $\mathbf{L}_{rp}$ :

$$\mathbf{L}_{tp} = \begin{bmatrix} RSS_1^{tp} & RSS_2^{tp} & \cdots & RSS_M^{tp} \\ AP_1^{tp} & AP_2^{tp} & \cdots & AP_M^{tp} \end{bmatrix}, \quad (6)$$

$$\mathbf{L}_{rp} = \begin{bmatrix} RSS_1^{rp} & RSS_2^{rp} & \cdots & RSS_M^{rp} \\ AP_1^{rp} & AP_2^{rp} & \cdots & AP_M^{rp} \end{bmatrix}, \quad (7)$$

where  $M$  is the number of APs. We take the first  $N_t$  APs in  $\mathbf{L}_{tp}$  to form a set, perform similarity matching with the first  $N_r$  strong APs in  $\mathbf{L}_{rp}$ , and obtain the AP set similarity vector  $\alpha$ :

$$\alpha = [\alpha_1, \alpha_2, \cdots, \alpha_{N_r}], \quad (8)$$

$$\alpha_i = \begin{cases} 1, & AP_i^{rp} \in \{AP_{start}^{tp}, \cdots, AP_{end}^{tp}\}, \\ 0.0001, & AP_i^{rp} \notin \{AP_{start}^{tp}, \cdots, AP_{end}^{tp}\}, \end{cases} \quad (9)$$

$$start = \begin{cases} i - \lfloor (N_t - 1)/2 \rfloor, & i \neq 1, \\ 1, & i = 1, \end{cases} \quad (10)$$

$$end = i + \lfloor (N_t - 1)/2 \rfloor, \quad (11)$$

where  $i \in \{1, 2, \cdots, N_r\}$ , and  $N_t$  and  $N_r$  denote the size of the RSS fault tolerance space and the scope of focusing on strong APs, respectively.  $N_r$  is acquired from the database and  $N_t = 3$  is a fixed coefficient, which will be further discussed in subsequent sections.

At this time, the RSS fluctuation space  $S_i$  corresponding to the first  $N_r$  strong APs can be obtained using Eq. (5), and after normalization, the RSS credibility vector is formed:

$$\lambda = [\lambda_1, \lambda_2, \cdots, \lambda_{N_r}], \quad (12)$$

$$\lambda_i = \frac{\exp(-S_i)}{\sum_{i=1}^{N_r} \exp(-S_i)}. \quad (13)$$

We update the weighted ED (Zhang H et al., 2022) of the RSS between the current TP ( $\mathbf{L}_{tp}$ ) and RP ( $\mathbf{L}_{rp}$ ) to be measured as

$$D_{SAPC} = \frac{1}{\lambda \alpha^T} \sqrt{\sum_{m=1}^M \omega_m (RSS_m^{tp} - RSS_m^{rp})^2}, \quad (14)$$

$$\omega_m = \frac{W_m^{rp} W_m^{tp}}{\sum_{m=1}^M W_m^{rp} W_m^{tp}}, \quad (15)$$

$$W_m^{rp} = (1/RSS_m^{rp})^2, \quad (16)$$

$$W_m^{tp} = (1/RSS_m^{tp})^2. \quad (17)$$

Ultimately, the preliminary positioning result  $L_{\text{inIP}}^K$  is obtained by identifying the weighted coordinates  $L_k$  corresponding to the  $K$  minimum ED  $D_{\text{SAPC}}^k$ :

$$L_{\text{inIP}}^K = \sum_{k=1}^K \frac{1}{D_{\text{SAPC}}^k} L_k \bigg/ \sum_{k=1}^K \frac{1}{D_{\text{SAPC}}^k}, \quad (18)$$

in which “inIP” refers to the initial position.

### 3.2 Dynamic $K$ -value algorithm based on neighbor density

In the original KNN positioning method, determining the optimal  $K$  value emerges as a pivotal challenge. Ni et al. (2003) addressed this by selecting the  $K$  value through experimentation. They explored various  $K$  values, specifically  $K = 2, 3, 4, 5$ , to assess position estimation errors. The results indicated that, on average, the optimal effect was observed at  $K = 4$ . However, obtaining this empirical value demands considerable effort and may lack generalizability to other datasets. Additionally, prior studies have demonstrated that adjusting parameter  $K$  for different TPs holds potential for improving localization performance (Umair et al., 2014; Lee et al., 2016; Oh and Kim, 2018). Therefore, for each individual TP across diverse datasets, it is essential and effective to determine the optimal  $K$  value for predicting each sample. Lee et al. (2016) proposed to adjust the optimal  $K$  value based on the topology and distance changes of its NNs. Drawing inspiration from this approach, we introduce a density-based  $K$ -value selection algorithm, named ND-DKA (Dynamic  $K$ -value Algorithm based on Neighbor Density). In contrast to the method by Lee et al. (2016), ND-DKA does not require an experiential threshold setting. Instead, we prioritize the proximity of neighbors to the TP and the density of neighbors during NN selection. ND-DKA employs two criteria for evaluating  $K$  values: (1) If the selected  $K$  RPs are near the predicted position, and (2) the  $K$  RPs are close to each other, then  $K$  is deemed optimal.

**3.2.1 Proximity of the neighbor to TP:** quantify the proximity of  $K$  RPs to their weighted geometric centers

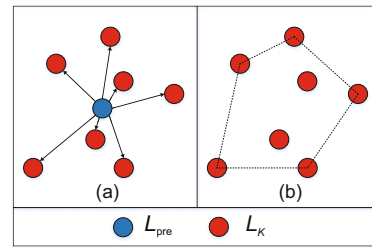
If the  $K$  RPs  $L_K = \{L_1(x_1, y_1), L_2(x_2, y_2), \dots, L_K(x_K, y_K)\}$  are known, the preliminary predicted position  $L_{\text{inIP}}^K(x_{\text{pre}}^K, y_{\text{pre}}^K)$  is obtained. As illustrated in Fig. 2a, to quantify the proximity between

$L_K$  and  $L_{\text{pre}}$ , the initial step involves calculating the physical distance between  $L_{\text{pre}}$  and  $L_K$ :

$$\text{dis}_k = \sqrt{(x_{\text{pre}}^K - x_k)^2 + (y_{\text{pre}}^K - y_k)^2}. \quad (19)$$

From this, we can obtain the closeness of  $K$  RPs to the predicted position, that is,

$$\beta_K = \frac{1}{K} \sum_{k=1}^K \left( \text{dis}_k - \frac{1}{K} \sum_{k=1}^K \text{dis}_k \right)^2. \quad (20)$$



**Fig. 2 Example diagram of the ND-DKA calculation approach: (a) distance distribution relative to the predicted point  $L_{\text{pre}}$  of  $K$  RPs; (b) convex hull of the  $K$  selected RPs**

**3.2.2 Density of neighbors:** quantify the proximity of  $K$  RPs to each other

As depicted in Fig. 2b,  $K$  RPs can encompass a minimal area, known as the convex hull area. This area reflects the density of RP distribution. An increase in the  $K$  value may result in the expansion of the convex hull area of RPs and potentially fail to meet the evaluation standards. Therefore, we use the unit convex hull area as an indicator of whether RPs are close or far apart. Initially, the Graham scan algorithm is employed to calculate the convex hull of the point set  $L_K$ , followed by the determination of the convex hull area  $h_K$ . The algorithm flow is outlined in Algorithm 1.

The ultimate criterion for evaluating the  $K$  value is the fusion of both methods, forming an assessment sequence  $U$  across various  $K$  values:

$$U = \{u_{K_{\min}}, u_{K_{\min}+1}, \dots, u_{K_{\max}}\}, \quad (21)$$

and for any  $i \in \{K_{\min}, K_{\min} + 1, \dots, K_{\max}\}$ ,

$$u_i = \frac{\beta_i}{\sum_{i=K_{\min}}^{K_{\max}} \beta_i} + \frac{h_i}{\sum_{i=K_{\min}}^{K_{\max}} h_i}, \quad (22)$$

where  $\beta_i$  is the closeness of  $i$  RPs to the predicted position,  $h_i$  is the unit convex hull area enclosed by

**Algorithm 1** Convex hull area

**Require:** initial selection of the first  $K$  RP sets  $L_K = \{L_1(x_1, y_1), L_2(x_2, y_2), \dots, L_K(x_K, y_K)\}$  determined by Eq. (14).  
**Ensure:** convex hull area  $h_K$ .  
 // Select the starting point  
 1: Select the coordinates with the smallest  $y$  coordinate (if there are multiple points with the smallest  $y$  coordinate, select the leftmost one) as  $P_1$   
 // Polar angle sorting  
 2: Calculate the polar angle  $A_i$  of each point  $P_i$  (except  $P_1$ ) relative to  $P_1$ , and sort the remaining points in ascending order of polar angle:  

$$A_i = \text{atan2}(y_i - y_1, x_i - x_1)$$
 // Initialize the stack  
 3: Put  $P_1$  and  $P_2$  into the empty stack  $S$  in sequence  
 // Scan and build convex hull  
 4: **For**  $j = 3$ :  $\text{length}(L_K)$   
 5: Calculate the cross product  $B_j = (x_{P_2} - x_{P_1})(y_{P_j} - y_{P_1}) - (y_{P_2} - y_{P_1})(x_{P_j} - x_{P_1})$   
 6: **While**  $B_j < 0$  and the number of elements in stack  $S > 1$   
 7: Pop the top element of the stack  
 8: **End While**  
 9: Push point  $P_j$  onto stack  $S$   
 10: **End For**  
 11: Enter  $S = \{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\}$  to calculate the convex hull area:  

$$h_K = \frac{1}{2} \left| \sum_{j=1}^n (x_j y_{j+1} - x_{j+1} y_j) \right| / K, \quad n \leq K$$
 12: **return**  $h_K$

$i$  RPs, and  $K_{\min} = 3$  and  $K_{\max} = 30$  are empirical values.

Ultimately, the  $K$  value corresponding to the minimum value in  $U$  is chosen as the optimal  $K$  value, and its predicted position serves as the final positioning outcome:

$$L_{\text{finP}} = L_{\text{inIP}}^K(x_{\text{pre}}^K, y_{\text{pre}}^K)_{\min(U)}. \quad (23)$$

## 4 Experiments

### 4.1 Dataset description

We chose four benchmark Wi-Fi fingerprint datasets, namely Tampere (Lohan et al., 2017), UJI-IndoorLoc (Torres-Sospedra et al., 2014), Geotec-Database (Torres-Sospedra et al., 2016), and

SODIndoorLoc (Bi et al., 2022), to assess the efficacy of our method. Prior to conducting the experiments, the dataset underwent preprocessing, retaining only the necessary data for the experiment. The retained data include signal strength and real-world coordinates (longitude and latitude) of the APs at all RPs.

1. Tampere: The dataset was gathered from a four-story university building situated in Tampere, Finland, spanning the period from January to August 2017. It encompasses 687 training fingerprints and 3951 test or estimated fingerprints. The collection was conducted in a crowd-sourced manner, involving 21 distinct devices and users. Coordinates were meticulously recorded in three dimensions, with each sample comprising 992 AP signals.

2. UJIIndoorLoc: The dataset was released by Jaume I University in Spain and encompasses multiple adjacent buildings and floors. Table 1 presents the relevant dataset information. Each record in this dataset includes RSS data from 520 APs (WAP001–WAP520), along with details such as building ID (BUILDINGID), collection device ID (PHONEID), and longitude and latitude (LONGITUDE and LATITUDE) indicating its location.

3. GeotecDatabase: The dataset was gathered and released by the GEOTEC Laboratory. As depicted in Table 2, each data record includes RSS data from 97 APs (WAP1–WAP97), along with details such as longitude and latitude.

4. SODIndoorLoc: The dataset was collected in the vicinity of the south and east sides of floors within corridors, offices, and conference rooms. Considered as a complement to UJIIndoorLoc, they share a consistent format. The stored data are labeled by building numbers, namely CETC331, HCXY, and SYL, with the respective APs containing 53, 347, and 363 RSSs.

### 4.2 Performance of SAPC-DKNN

To evaluate the efficacy of our method in a real-world localization setting, we partition the

**Table 1** UJIIndoorLoc dataset (some examples)

WAP001	WAP002	...	WAP519	WAP520	LONGITUDE	LATITUDE	BUILDINGID	PHONEID
100	100	...	100	100	-7541.2643	4 864 920.778	1	23
100	100	...	100	100	-7536.6212	4 864 934.225	1	23
...	...	...	...	...	...	...	...	...
100	100	...	100	100	-7536.1658	4 864 897.859	1	10

**Table 2 GeotecDatabase dataset (some examples)**

WAP1	WAP2	...	WAP96	WAP97	LONGITUDE	LATITUDE	TIMESTAMP
100	100	...	-57	-53	-8220.546 590	4 865 048.064	1450452282
100	100	...	-55	-56	-8220.546 590	4 865 048.064	1450452285
...	...	...	...	...	...	...	...
100	100	...	-72	-58	-8226.447 664	4 865 062.628	1450786990

experiments into two distinct phases:

1. Explore the positioning effect of SAPC-DKNN in a 3D environment. We select the Tampere dataset for 3D indoor positioning prediction and juxtaposed SAPC-DKNN against the latest methods. The experimental outcomes are delineated in Table 3. To underscore impartiality, the baseline method results in Table 3 are exclusively sourced from the original text. Notably, amid the majority of deep learning-based approaches, ours exhibits superior performance. Notably, compared to the optimal deep learning-based method GrowNetLoc, SAPC-DKNN yields a 47% increase in positioning accuracy. This method integrates two distinct networks, a gradient boosting neural network (GrowNet) and a long short-term memory (LSTM) network, effectively navigating complex environments for 3D positioning. Nonetheless, under limited data circumstances, it may not yield anticipated outcomes. Moreover, compared with the KNN-based method, RWKNN achieves optimal positioning accuracy at 6.53 m, surpassing deep learning-based alternatives. Incorporating indoor movement constraints, it employs search rectangles and trajectory constraints to mitigate spatial ambiguity. In contrast, our proposed approach still outperforms it by 37%, underscoring the efficacy of AP credibility-based methods in mit-

igating positioning errors arising from RSS instability. In addition, among fingerprint-based positioning methods, the KNN method can achieve acceptable positioning accuracy with a simple structure and low computational complexity.

2. Explore the 2D positioning effect of SAPC-DKNN under the walking trajectory of a single person. As aforementioned, we have confirmed that, compared with deep learning-based methods, the KNN method can achieve better positioning accuracy with a simple structure and lower complexity. We compare the results of SAPC-DKNN on three datasets with KNN (Sadowski et al., 2020), WKNN (Zhang J and Mao, 2022), STI-WKNN (Zou et al., 2017), Spearman-KNN (Xie et al., 2016), SIM-KNN (Peng et al., 2016), and SRL-KNN (Hoang et al., 2018). To verify the performance of our method in a 2D environment, we use actual positioning application habits and divide them according to different users on three public datasets to verify the effect of online indoor positioning in a simulated real environment. The experimental results are shown in Table 4. To ensure fair results, each method uses the optimal  $K$  value. Specifically, for UJIIndoorLoc, we categorize walking trajectories based on building names and user device IDs. Three random trajectories per building (denoted as B for BUILDINGID and P for PHONEID, with B0-P0 representing the trajectory where BUILDINGID and PHONEID are both 0) are selected for prediction. This allows us to assess positioning performance in both single-user and multi-user contexts. Across these six test tracks, SAPC-DKNN demonstrates superior performance compared to the six other advanced methods, including a significant performance gap. On B0-P4, we achieve the highest accuracy positioning error of 4.18 m, marking a 61.90% improvement over the least accurate baseline method and a 27.43% enhancement compared to the best-performing SRL-KNN method. Subsequently, B0-P0 exhibits a positioning error of 5.66 m. Notably, B0-P4 and B0-P0

**Table 3 Performance of SAPC-DKNN on Tampere for 3D positioning**

Method	Reference	Loss (m)
CNN	Arslantas and Okdem (2024)	8.13
SALLoc	Ayinla et al. (2024)	9.52
eAaT+	Nguyen et al. (2024)	8.14
GrowNetLoc	Zhao et al. (2024)	7.82
EA-CNN	Alitalessi et al. (2023)	9.52
bAaT	Nguyen et al. (2023)	8.53
GMM+WKNN	Lin et al. (2023)	11.17
Vanilla LSTM	Dong YH et al. (2022)	8.66
HADNN	Cha and Lim (2022)	9.05
RWKNN	Chen et al. (2022)	6.53
CNNLoc	Song et al. (2019)	10.88
SAPC-DKNN	This paper	<b>4.14</b>

The best result is in bold

**Table 4 Average positioning error for different methods**

Trajectory	Average positioning error (m)						
	SAPC-DKNN ( $K \in [3, 30]$ )	KNN ( $K = 5$ )	WKNN ( $K = 5$ )	STI-WKNN ( $K = 5$ )	Spearman-KNN ( $K = 5$ )	SIM-KNN ( $K = 5$ )	SRL-KNN ( $K = 3$ )
B0-P0	<b>5.66±3.61</b>	9.46±6.23	9.52±6.26	8.70±5.88	16.05±10.95	9.52±6.26	8.26±5.11
B0-P4	<b>4.18±3.92</b>	6.87±5.11	6.84±5.08	6.73±4.59	10.97±9.10	6.84±5.08	5.76±4.45
B0-P21	<b>6.20±5.89</b>	13.02±11.12	13.00±11.11	13.62±11.10	13.46±9.22	13.00±11.11	15.29±11.55
B1-P4	<b>6.90±4.27</b>	10.67±7.22	11.33±7.95	10.72±8.82	16.65±10.75	11.33±7.95	10.15±6.84
B1-P12	<b>8.01±6.58</b>	12.38±9.15	12.37±9.12	12.16±9.60	12.83±9.48	12.37±9.12	16.49±20.20
B1-P13	<b>7.70±7.22</b>	11.11±8.82	11.04±8.88	10.51±9.37	12.55±10.36	11.04±8.88	11.34±10.27
Val-1	<b>4.56±2.20</b>	5.87±2.69	5.87±2.72	5.87±2.87	5.39±2.32	5.87±2.73	5.57±2.64
Val-2	<b>4.68±1.97</b>	5.73±2.70	5.73±2.70	5.76±2.80	5.87±3.07	5.72±2.75	5.74±2.77
Val-3	<b>4.52±1.90</b>	6.43±3.02	6.45±3.02	6.27±2.96	7.31±3.44	6.44±3.03	6.14±2.89
Val-All	<b>4.59±2.08</b>	6.02±2.94	6.03±2.93	6.04±2.91	6.47±3.22	6.04±2.94	5.92±2.79
Testing-CETC331	<b>2.96±2.63</b>	4.75±4.31	4.75±4.31	4.66±4.03	4.87±4.05	4.79±4.33	4.72±4.07
Testing-HCXY-All	<b>2.20±1.93</b>	3.15±2.99	3.01±2.79	2.84±2.58	4.35±4.17	3.00±2.80	2.98±2.82
Testing-SYL-All	<b>3.68±5.01</b>	5.19±5.27	5.18±5.27	4.78±5.25	5.18±5.30	5.08±5.30	5.02±5.30

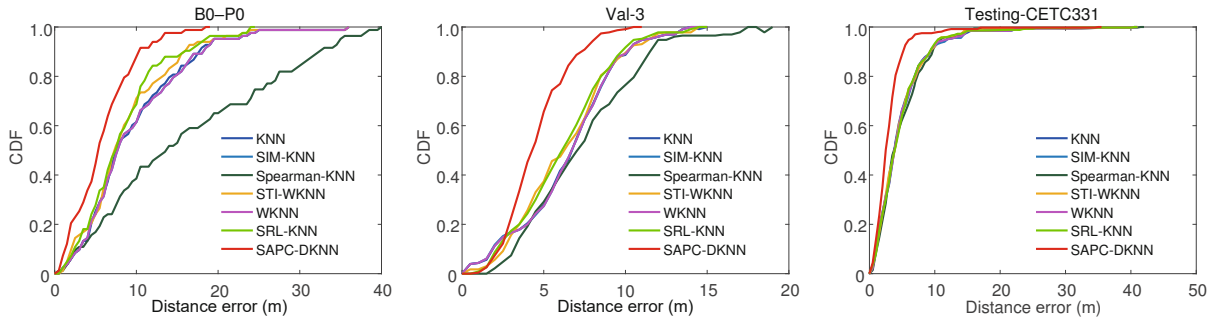
The best results are in bold

represent short and long trajectories, respectively, underscoring the consistent stability of SAPC-DKNN across trajectory lengths. Across the B0 and B1 trajectories, the positioning accuracy gap consistently ranges between 1 and 2 m, affirming SAPC-DKNN's robust performance in both single-user and multi-user scenarios. Furthermore, our observations highlight Spearman-KNN as the least effective method across most trajectories. This discrepancy arises, in part, because Spearman-KNN neglects the ranking effect of APs when calculating fingerprint similarity. Instead, it solely considers overall data, potentially resulting in identical fingerprints being associated with different locations. It is crucial to note that our method successfully addresses this challenge and maintains the highest accuracy by leveraging prior knowledge of RSS attenuation performance and exploiting AP sequence information.

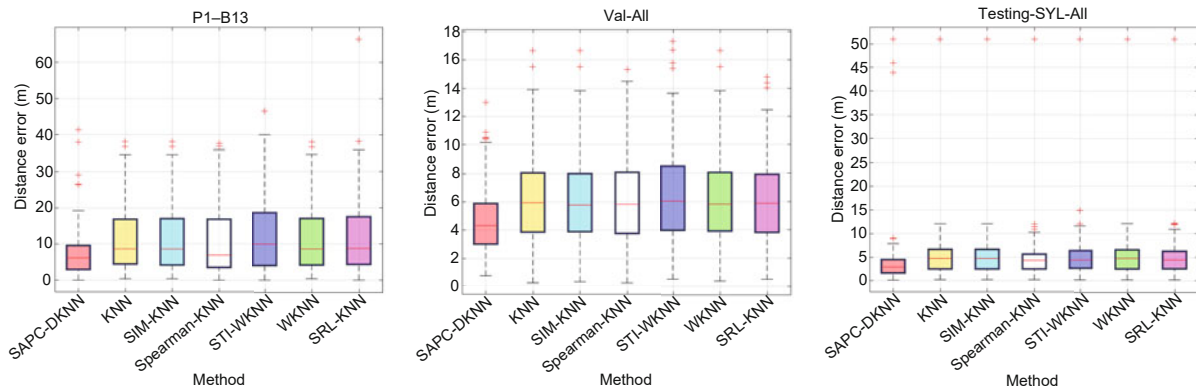
The GeotecDatabase test set exhibits temporal continuity, with a few instances featuring significant time intervals, notably 4238 s and 17 290 s. We attribute these intervals to inconsistencies in the data collection process, and use them as time nodes to segment the test set into three distinct walking trajectories: Val-1, Val-2, and Val-3. These trajectories, along with the entire test set, are independently subjected to predictions to showcase the real-time positioning efficacy in scenarios involving both continuous walking and intermittent user positioning in authentic environments. Similar to the observed performance on UJIIndoorLoc, SAPC-DKNN demonstrates positioning differences of  $< 0.1$  m on Val-1, Val-2, and Val-3, all aligning closely with the re-

sults of Val-All. This substantiates the capacity of SAPC-DKNN to excel in both continuous walking and discontinuous positioning settings.

On SODIndoorLoc, we conduct experimental verification using all unprocessed test sets (Testing-CETC331, Testing-HCXY-All, and Testing-SYL-All) across three environments. SRL-KNN, incorporating principles of human walking, ranks third in Testing-SYL-All. However, it neglects the impact of RSS fluctuations, leading to biased positioning outcomes. KNN, representing traditional fingerprint positioning methods, exhibits a positioning accuracy 29.70% lower than SAPC-DKNN on Val-3 and 37.68% lower on Testing-CETC331. Although WKNN, SIM-KNN, and STI-WKNN aim to enhance KNN by considering weights and fingerprint distances, their performance improvements across the three datasets are relatively modest, and their generalization performance is average. This suggests that employing different strategies such as assigning weights at distinct RP locations and adopting varied fingerprint calculation methods may not be highly effective for datasets with varying trajectory lengths and environmental backgrounds. Figs. 3 and 4 present comparisons of distance error cumulative distribution function curves and error box plots for seven positioning methods across three datasets, respectively. In Fig. 3, it is evident that SAPC-DKNN consistently exhibits leftward-shifted error curves on all three datasets, with the maximum error consistently smaller than those of the six other methods. Specifically, on B0-P0, SAPC-DKNN accounts for more than 80% within the 10-m positioning error



**Fig. 3** Comparison of the cumulative distribution function (CDF) among seven methods of indoor positioning (References to color refer to the online version of this figure)



**Fig. 4** Comparison of distance errors among seven methods of indoor positioning

range, surpassing SRL-KNN at approximately 60%, and outperforming the remaining methods. Notably, on Val-3 and Testing-CETC331, the SAPC-DKNN curve stands distinct from the six comparison methods, underscoring its superior performance. Fig. 4 illustrates that SAPC-DKNN achieves the lowest positioning errors at the median, maximum, minimum, and upper quartile. In summary, SAPC-DKNN leverages prior knowledge of the RSS decay model, quantifies AP importance, and mitigates RSS uncertainty, resulting in consistently superior accuracy across multiple datasets. These findings affirm the model's good generalization performance and stability.

### 4.3 Research on parameters

Following the sorting of APs for both the point to be measured and the RP, SAPC-DKNN chooses the RSS corresponding to  $N_t$  and  $N_r$  APs for distance measurement. The selection of  $N_t$  and  $N_r$  significantly influences the ultimate positioning accuracy. Specifically, the value of  $N_t$  determines the extent of the RSS fault tolerance space, while  $N_r$  dictates the scope of focus on strong APs. Optimal values for  $N_t$  and  $N_r$  contribute to the optimization of positioning

accuracy.

We assume that the value of  $N_r$  might be associated with the distribution of RSS sizes within the fingerprint database. The chosen  $N_r$  should fulfill the requirement of having a sufficient number of strong APs to cover all RPs in the fingerprint database. This selection serves to prevent excessive weak APs extracted from RPs, thereby averting inaccurate matching results during the process of matching RPs with points to be measured. To identify the suitable  $N_r$  for various datasets, we visualize the RSS distribution within the fingerprint database across three datasets. By arranging the RSS values corresponding to each RP in ascending order, we generate an RSS heatmap. As depicted in Fig. 5, distinct  $N_r$  values can be selected based on the RSS distribution within the fingerprint database across various datasets. For instance, on the UJIIndoorLoc dataset, the total count of strong APs is approximately 10 ( $N_r \approx 10$ ), whereas on GeotecDatabase, it amounts to approximately 12 ( $N_r \approx 12$ ). Across different environments within the SODIndoorLoc dataset, the distribution of strong AP counts remains relatively consistent, at approximately 15 ( $N_r \approx 15$ ).

To corroborate our assumptions regarding the

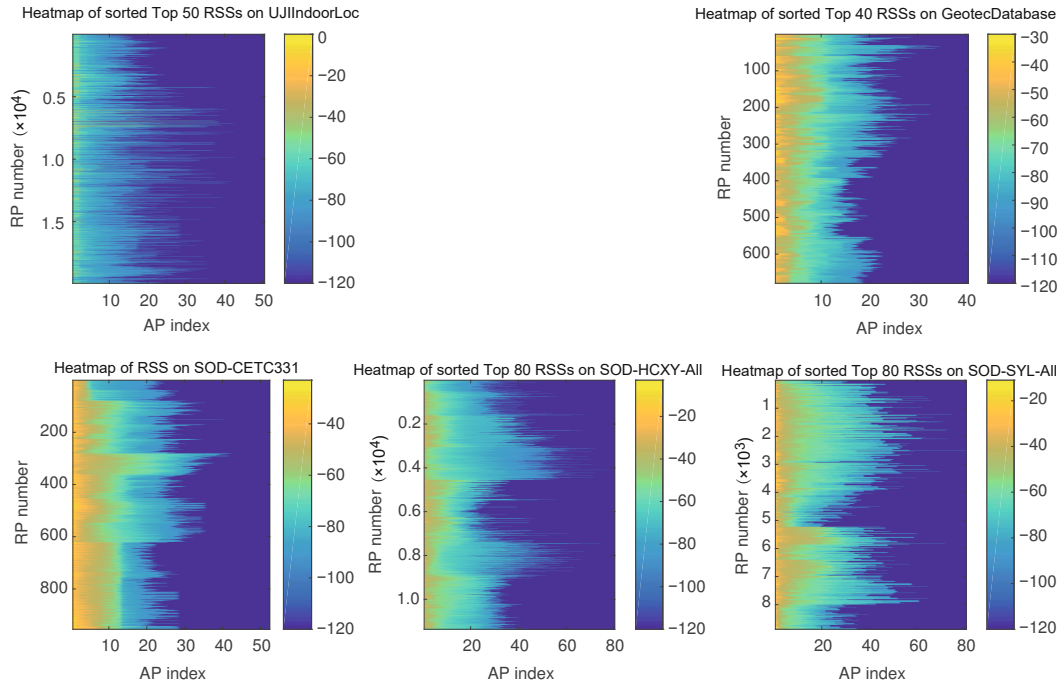


Fig. 5 RSS distribution heatmap on three datasets (RP: reference point; RSS: received signal strength)

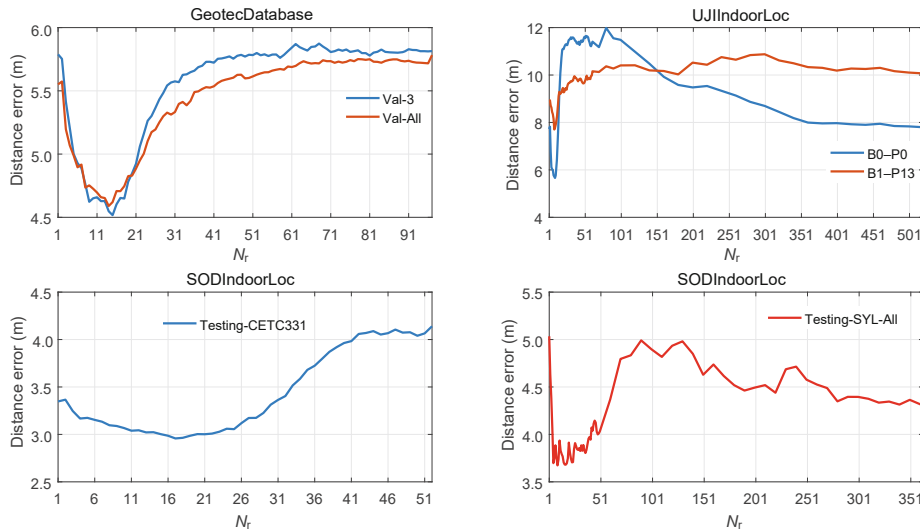


Fig. 6 Distance errors against  $N_r$  (References to color refer to the online version of this figure)

value of  $N_r$  and to determine the appropriate selection of  $N_t$ , we randomly select two test sets for experiments across three types of datasets. The results depicted in Figs. 6 and 7 reveal insights. In Fig. 6, with  $N_t$  fixed at three, the curves across the six test sets exhibit varying trends. Different datasets exhibit distinct peak values. Notably, on Val-3 and Val-All, there is a conspicuous minimum error, cor-

responding to  $N_r$  values of 15 and 14, respectively. When  $N_r \approx 12$ , a minor error persists, consistent with our hypothesis. Intriguingly, on both the UJI-IndoorLoc and SODIndoorLoc datasets, the error trend tends to plateau. However, when  $N_r \approx 10$  and  $N_r \approx 15$ , improved values are obtained. When  $N_r$  reaches its maximum value, it represents the total number of APs. At this point, both strong and

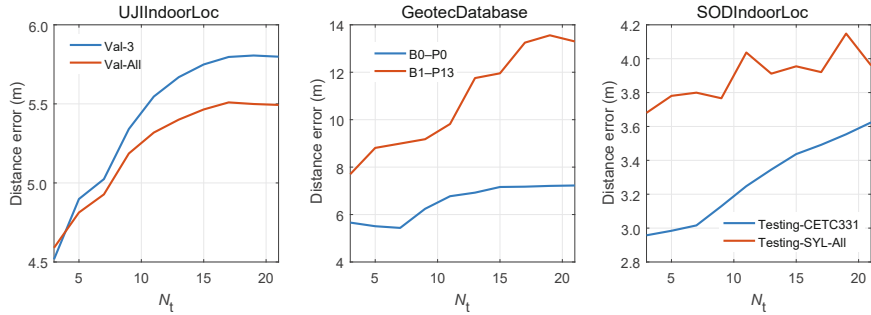


Fig. 7 Distance errors against  $N_t$  (References to color refer to the online version of this figure)

weak APs are included in the algorithm. As shown in Fig. 6, as  $N_r$  approaches the total number of APs, the prediction error initially increases, reaches a peak, and then gradually converges. This indicates that incorporating more weak RSS signals when calculating the weights reduces positioning performance. The reason is that the noise in weak RSS signals is significantly larger than the effective signal, causing the useful information to be overwhelmed by noise. Moreover, noise removal is challenging due to its complexity. Consequently, selecting too many weak RSS signals is not an optimal strategy. Hence, our assumption regarding  $N_r$  is affirmed. By analyzing the RSS distribution within the fingerprint database, we can determine the number of RPs covered by the majority of strong APs, representing the appropriate  $N_r$ . The results in Fig. 7 are based on the experimental outcomes of Fig. 6. Following the determination of  $N_r$ , errors exhibit an upward trend across the six test sets. When  $N_t$  is set to 3, minimum errors are observed for Val-3, Val-All, B1-P13, and Testing-CETC331. Although this trend is not consistent for B0-P0 and Testing-SYL-All, the error variation is not substantial compared to that when  $N_t$  is set to 3. Consequently, based on our comprehensive experiments, we adopt  $N_t = 3$  as the overall model design.

In general, selecting a small  $N_t$  limits the space for AP ranking changes induced by RSS fluctuations and overly relies on the magnitude of the RSS value. Conversely, a large  $N_t$  increases the RSS fault tolerance space, potentially screening out APs with greater physical distance. This is not conducive to enhancing positioning accuracy. Similar considerations apply to the value of  $N_r$ . A narrow focus on strong APs limits the stability of the judgment basis, whereas an overly broad focus

introduces weaker APs and interferes with RSS credibility calculations and diminishing positioning accuracy. In real-world application scenarios, the value of  $N_r$  may vary across different environments, but it can be determined from the RSS distribution within the fingerprint database. Regarding the value of  $N_t$ , experimental findings across three distinct datasets suggest that  $N_t = 3$  can be directly applied to real-world scenarios. This confirmation underscores the continued effectiveness of SAPC-DKNN in practical applications.

#### 4.4 RSS credibility discussion

In our method, AP credibility is depicted by the RSS fluctuation area, which contributes to the optimal positioning accuracy. The credibility of each strong AP hinges on its respective RSS value and serves as a key aspect of our proposed approach. However, considering the potential for enhanced accuracy, could we derive improved results by overlooking specific RSS values and instead employing straightforward arithmetic or geometric relationships to assess the strength of the first  $N_r$  APs? To explore this, we introduce two alternative methods for quantifying AP credibility:

1. Arithmetic method. The arithmetic method establishes the credibility of various strong and weak APs as a vector linked to the AP order and  $N_r$ . In other words, it transforms Eq. (13) as follows:

$$\lambda_i = (N_r - i + 1)/N_r. \quad (24)$$

2. Equal-ratio method. Similar to the arithmetic method, the equal-ratio method converts the credibility between strong and weak APs into an equal-ratio relationship, transforming Eq. (13) as follows:

$$\lambda_i = 1/(N_r)^i. \quad (25)$$

We conduct experimental verification by randomly selecting two test sets from each of the three datasets, and the results are presented in Table 5. Across the six test sets, the positioning accuracy of the arithmetic method is inferior to that of our proposed method, and the equal-ratio method exhibits lower accuracy than the arithmetic method. Our method demonstrates lower mean location errors across all tests (Table 5), though with marginally higher standard deviations on B1–P12, Val-1, and Val-All. This discrepancy arises because the equal difference or proportional relationship is independent of the RSS value corresponding to the AP but is solely linked to the strength order and  $N_r$ . Compared with our method, the arithmetic method diminishes the credibility gap between the strongest  $N_r$  APs. If the  $i^{\text{th}}$  AP, following the strength ranking, significantly differs in strength from the  $(i + 1)^{\text{th}}$  AP, the arithmetic method fails to reflect such a gap. This fixed weighting method smooths signal differences and reduces positioning standard deviations, but distorts AP reliability. The equal-ratio method encounters a similar issue, because it cannot dynamically quantify differences between APs with distinct strengths. In contrast, SAPC-DKNN dynamically quantifies AP credibility based on the strength of its corresponding RSS, which is closely tied to the strength of APs. We visualize the deviation between the actual position and the predicted position using the three quantization methods on the B0–P0 test set. As illustrated in Fig. 8, the green line represents the physical distance between the actual and predicted positions and serves as a metric for prediction accuracy. In Fig. 8, from right to left, the area cov-

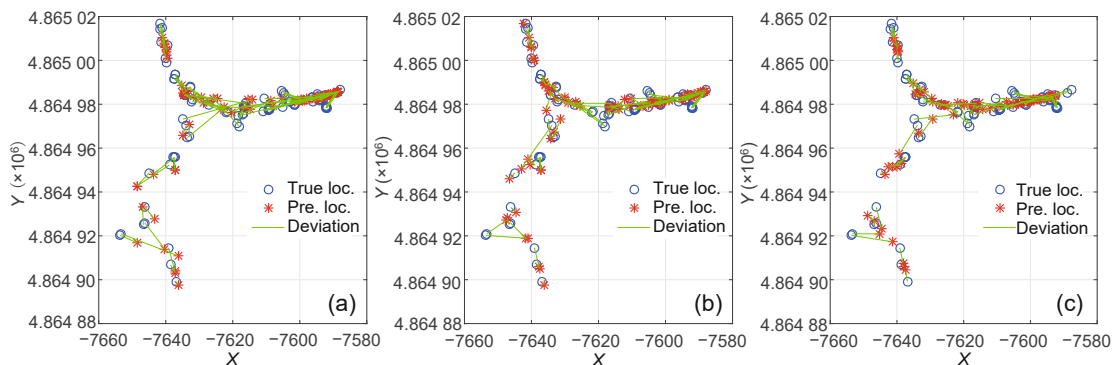
ered by the green lines widens and deepens, affirming the superior positioning accuracy of our method. Furthermore, Fig. 9 depicts the actual and predicted trajectories of the B0–P4 test set. When the blue and red lines overlap, the optimal prediction accuracy is achieved. Notably, Fig. 9a reveals numerous non-overlapping trajectories in the upper part, indicating a suboptimal prediction effect. In contrast, Fig. 9b exhibits fewer non-overlapping trajectories, confirming that the equal-ratio method is inferior to the arithmetic method. In the lower part of Fig. 9c, the predicted trajectory almost perfectly aligns with the actual trajectory, a feature absent in both the arithmetic and equal-ratio methods. Critically, the persistent positioning error reduction (Fig. 8) and trajectory alignment fidelity (Fig. 9c) substantiate that mean error optimization dominates the performance metric hierarchy.

#### 4.5 Effectiveness of AP set similarity

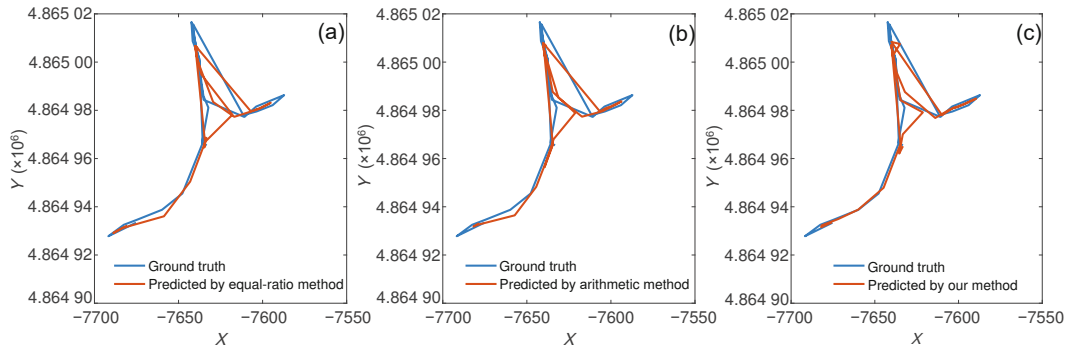
AP set similarity delineates the likeness between the strong APs of the TP and RP, serving as an effective measure of their overall similarity. To assess the effectiveness of our proposed AP set similarity method, we exclude this method on three datasets. This transformation simplifies AP set similarity to

$$\alpha = [1, 1, \dots, 1]_{N_r}. \quad (26)$$

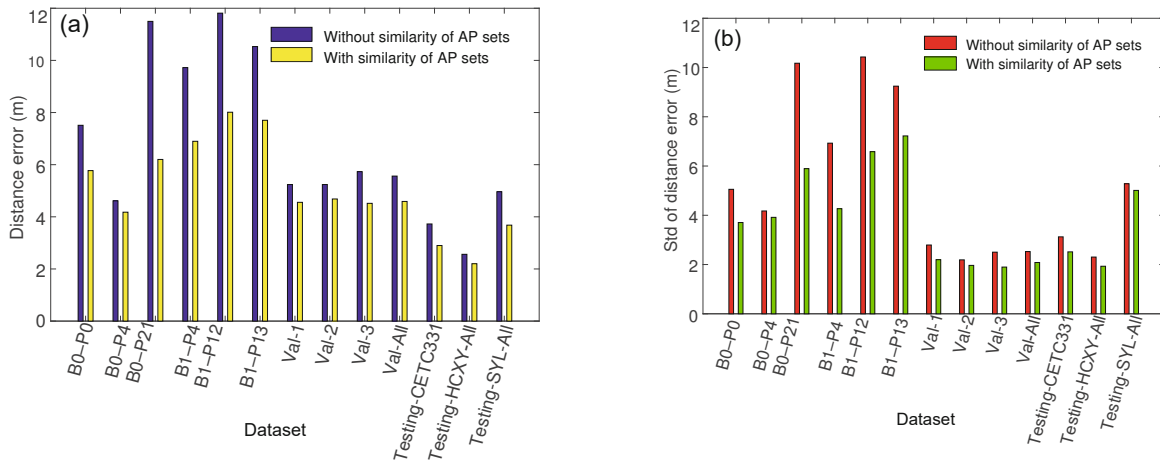
Fig. 10 compares the results between using and not using AP set similarity. As depicted in Fig. 10a, across three distinct datasets, the AP set similarity method consistently outperforms the method without AP set similarity. Across diverse datasets, our



**Fig. 8** Performance of different quantitative AP credibility methods on B0–P0. (a), (b), and (c) show the results of using the equal-ratio method, arithmetic method, and our method, respectively. References to color refer to the online version of this figure



**Fig. 9** Performance of different quantitative AP credibility methods on B0-P4. (a), (b), and (c) show the results of using the equal-ratio method, arithmetic method, and our method, respectively. References to color refer to the online version of this figure



**Fig. 10** Comparison of distance errors with and without using similarity of AP sets: (a) average positioning error results; (b) standard deviation results

proposed AP set similarity method consistently attains superior positioning accuracy, affirming the method's effectiveness and robustness. Additionally, in the standard deviation results presented in Fig. 10b, the method that does not use AP set similarity consistently exhibits a higher standard deviation compared to the method incorporating it. This suggests that the AP set similarity method can maintain a specific positioning prediction error range, preventing extremely biased prediction results. In contrast, the method without AP set similarity reaches a prediction standard deviation of 10 m, indicating its ineffectiveness in handling samples that are challenging to predict accurately. This underscores the effectiveness of our proposed AP set similarity, which processes AP sorted results based on RSS size rather than directly handling RSS values, thereby eliminating issues arising from small fluctuations in RSS and errors in similarity calculation.

#### 4.6 Ablation experiments

The rationale derived from the RSS decay model demonstrates that RSS similarity inadequately reflects the proximity of locations, with the stability of strong APs surpassing that of weak APs. Building on this insight, we leverage prior knowledge of the RSS decay law to quantify the credibility of strong APs, leading to the development of a novel method for measuring the RSS distance that incorporates the weighting of strong APs. Simultaneously, achieving the optimal target for KNN prediction with a static  $K$  value is challenging. To address this, we introduce a dynamic  $K$ -value algorithm based on neighbor density, ND-DKA.

To assess the efficacy of the combined strong AP weighted RSS distance measurement method with ND-DKA, we conduct experiments by randomly selecting two test sets across three types of

**Table 5 Comparison of different methods for quantifying AP credibility**

Method	Average positioning error (m)					
	B0-P21	B1-P12	Val-1	Val-All	Testing-CETC331	Testing-SYL-All
Equal-ratio method	8.79±8.54	9.51±8.06	5.41±2.46	5.39±2.33	3.48±3.22	4.59±5.18
Arithmetic method	7.37±6.34	8.77±5.62	4.72±1.99	4.78±1.81	3.11±2.64	4.01±5.08
Ours	<b>6.20±5.89</b>	<b>8.01±6.58</b>	<b>4.56±2.20</b>	<b>4.59±2.08</b>	<b>2.96±2.63</b>	<b>3.68±5.01</b>

The best results are in bold

**Table 6 Ablation results of SAPC-DKNN**

Method	Average positioning error (m)					
	B0-P0	B1-P13	Val-3	Val-All	Testing-CETC331	Testing-SYL-All
no-Weight+no-Kdynamic	8.09±5.60	10.83±9.40	6.00±2.96	5.74±2.88	3.99±3.58	5.00±5.19
no-Weight+Kdynamic	7.47±5.03	10.60±9.23	5.68±2.32	5.53±2.56	3.75±3.12	4.92±5.23
Weight+no-Kdynamic	6.32±4.20	8.25±7.44	4.83±2.60	4.85±2.63	3.18±3.04	4.85±5.18
Weight+Kdynamic (ours)	<b>5.66±3.61</b>	<b>7.70±7.22</b>	<b>4.52±1.90</b>	<b>4.59±2.08</b>	<b>2.96±2.63</b>	<b>3.68±5.01</b>

The best results are in bold

datasets. The results are detailed in Table 6, where “no-Weight” denotes the RSS ED without strong AP weighting, that is, the transformation of Eq. (14) into Eq. (27), and “no-Kdynamic” signifies the result without the ND-DKA method.

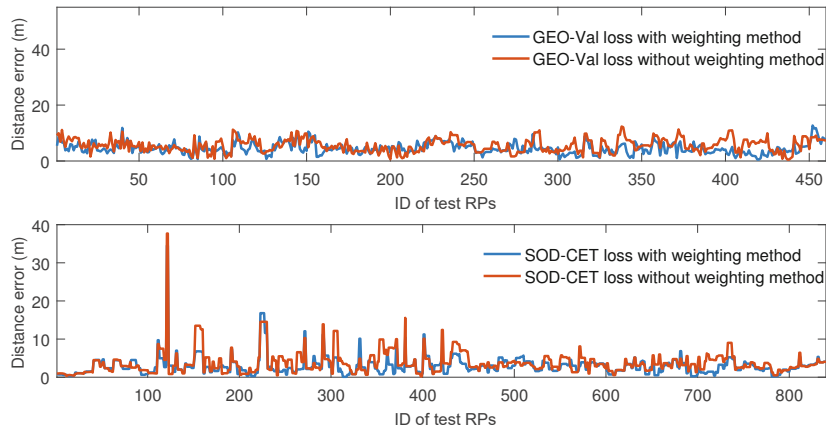
$$D = \sqrt{\sum_{m=1}^M \omega_m (\text{RSS}_m^{\text{tp}} - \text{RSS}_m^{\text{rp}})^2}. \quad (27)$$

Table 6 reveals that “Weight+Kdynamic” consistently performs optimally across the six test sets. Specifically, on B0-P0, “Weight+Kdynamic” outperforms “no-Weight+Kdynamic” by 24.23%. Similarly, without the ND-DKA method, “Weight+no-Kdynamic” surpasses “no-Weight+no-Kdynamic” by 21.88%, demonstrating an effective enhancement in positioning accuracy. This affirms the effectiveness of the strong AP weighting method in KNN. When applying the strong AP weighting method, “Weight+Kdynamic” exhibits a 6.67% improvement on B1-P13 and a 24.12% improvement on Testing-SYL-All compared to “Weight+no-Kdynamic.” Notably, when the strong AP weighting method is not employed, the results consistently favor the ND-DKA method, with “no-Weight+Kdynamic” consistently outperforming “no-Weight+no-Kdynamic.” This underscores the superiority of the method using ND-DKA. Experimental results across various datasets indicate the relative robustness of our ND-DKA method, showcasing its capacity to automatically optimize and enhance positioning prediction accuracy. Overall,

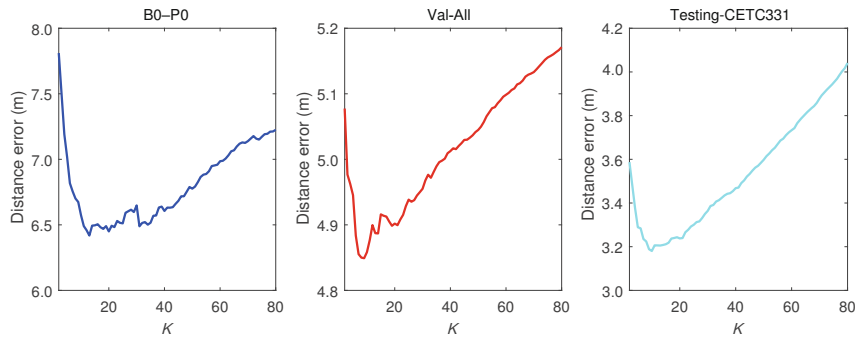
“Weight+Kdynamic” demonstrates improvements of 24.67%, 20.03%, and 25.81% on Val-3, Val-All, and Testing-CETC331, respectively, compared to “no-Weight+no-Kdynamic.” This verification indicates that our method consistently achieves stable and accurate positioning results under both continuous walking and non-continuous environments. It further affirms the efficacy of the strong AP weighted RSS distance measurement method combined with ND-DKA in significantly improving the prediction effectiveness of indoor positioning.

Additionally, Fig. 11 illustrates the sample error trend on GeotecDatabase and SODIndoorLoc when employing and not employing AP weighting. The prediction error curve using the AP weighting method is consistently below the red line, and on the SODIndoorLoc test set, prediction errors are evident in the red line, which is attributed to RSS instability. In contrast, the use of the AP weighting method results in sample errors confined within a specific range, exhibiting minimum fluctuations. This underscores the capability of the weighting method to mitigate inaccuracies in similarity calculation stemming from abnormal RSS fluctuations, thereby maintaining a consistently robust prediction effect.

To further investigate the effectiveness of ND-DKA, we conduct experiments with three selected test sets. Fig. 12 illustrates the prediction results under different  $K$  values when ND-DKA is not applied. Fig. 13 illustrates the distribution of automatically selected  $K$  values when using ND-DKA. The  $K$ -value range in ND-DKA is set between 3 and 30.



**Fig. 11** Comparison of distance errors with and without access point (AP) weighting on GeotecDatabase (top) and SODIndoorLoc (bottom) (References to color refer to the online version of this figure)



**Fig. 12** Comparison of distance errors against  $K$  values without using ND-DKA on three datasets

A minimum value of  $K = 3$  satisfies the geometric constraint that three points must be coplanar to ensure the basic computational functionality of Algorithm 1 for the convex hull area. The maximum value of  $K = 30$  is chosen as a reasonable upper limit based on experimental observations. The frequency of larger  $K$  values decreases significantly, indicating their limited contribution to classification performance. The selection of  $K = 30$  balances algorithmic efficiency with the requirements of diverse datasets.

In Fig. 12, the prediction errors across the three datasets exhibit a peak at a specific  $K$  value. Beyond this point, the errors increase as  $K$  continues to grow. However, compared with the method employing ND-DKA, the errors remain higher. Additionally, the optimal  $K$  value that achieves the best overall prediction performance varies across datasets. The optimal solution for the static  $K$  value is a global optimum calculated based on the average error across the entire dataset. However, it may not reflect

the most suitable number of neighbors for an individual sample. Due to the heterogeneity in feature distributions across samples, some samples may rely heavily on a small number of highly correlated RPs, whereas others require more RPs to synthesize information effectively. Therefore, although the static  $K$ -value method is appropriate at a global level, it may not suit every individual sample. The core advantage of ND-DKA lies in its ability to adaptively adjust the  $K$  value according to the characteristics of each sample, achieving a local optimum. As illustrated in Fig. 13, on Testing-CETC331, the  $K$ -value distribution for the ND-DKA method reveals that high-frequency  $K$  values are concentrated between 3 and 6. This indicates that most samples require only a small number of highly correlated RPs to achieve better prediction results. Simultaneously, the dynamic distribution includes some larger  $K$  values (e.g., above 10) to account for samples requiring additional RPs. These additional RPs may have lower ED correlations but can provide significant potential

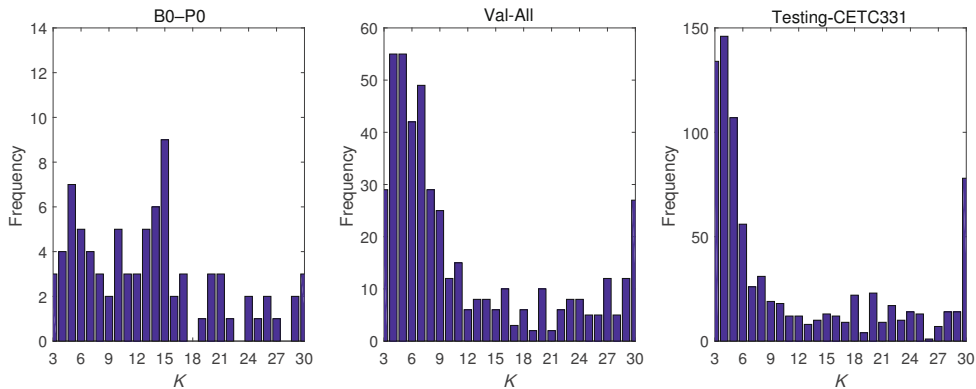


Fig. 13 Frequency distribution histogram of  $K$  values selected using ND-DKA on three datasets

contributions. Furthermore, on different datasets, the selected  $K$ -value distributions vary, demonstrating that ND-DKA optimizes at the individual sample level through its adaptive mechanism. This approach avoids completely excluding RPs with low ED correlations and comprehensively considers the contributions of all RPs across different scenarios. Consequently, ND-DKA outperforms the static method as a whole. In summary, our approach demonstrates robustness and effectiveness.

## 5 Conclusions

In conclusion, we have introduced a DKNN method based on strong AP credibility for indoor positioning (SAPC-DKNN). Leveraging the progression of the RSS path loss model, this method quantifies AP credibility and devises an RSS distance measurement technique incorporating strong AP weighting. In comparison with alternative weighting methods, SAPC-DKNN uses both the order and strength information at the AP level to mitigate similarity errors arising from RSS fluctuations, thereby significantly enhancing positioning accuracy. Furthermore, through integration with a dynamic  $K$ -value algorithm based on NN density, SAPC-DKNN achieves heightened precision and stability in real-time positioning. Our results demonstrate that SAPC-DKNN adeptly addresses key challenges inherent in KNN, such as the mismatch between RSS similarity and physical distance, RSSI instability, and uncertainty in optimal  $K$ -value solutions. Experimental findings reveal a substantial reduction in the average positioning error, ranging from 15.41% to 64.74%, surpassing the performance of the tradi-

tional KNN method. In future research endeavors, we aim to extend the application of the attenuation model's prior knowledge to more intricate prediction models, striving for even more precise indoor positioning solutions.

## Contributors

Yuting YANG designed the research, processed the data, and drafted the paper. Tao ZHANG and Wu HUANG revised and finalized the paper.

## Conflict of interest

All the authors declare that they have no conflict of interest.

## Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

## References

- Alitaleshi A, Jazayeriy H, Kazemitabar J, 2023. EA-CNN: a smart indoor 3D positioning scheme based on WiFi fingerprinting and deep learning. *Eng Appl Artif Intell*, 117:105509. <https://doi.org/10.1016/j.engappai.2022.105509>
- Arslantas H, Okdem S, 2024. Indoor localization with an autoencoder-based convolutional neural network. *IEEE Access*, (12):46059-46066. <https://doi.org/10.1109/ACCESS.2024.3382135>
- Ayinla SL, Aziz AA, Driberg M, 2024. SALoc: an accurate target localization in WiFi-enabled indoor environments via SAE-ALSTM. *IEEE Access*, 12:19694-19710. <https://doi.org/10.1109/ACCESS.2024.3360228>
- Bahl P, Padmanabhan VN, 2000. RADAR: an in-building RF-based user location and tracking system. Proc IEEE INFOCOM Conf on Computer Communications and 19<sup>th</sup> Annual Joint Conf of the IEEE Computer and Communications Societies, p.775-784. <https://doi.org/10.1109/INFCOM.2000.832252>

- Bi JX, Wang YJ, Yu BG, et al., 2022. Supplementary open dataset for WiFi indoor localization based on received signal strength. *Satell Navig*, 3(1):25. <https://doi.org/10.1186/s43020-022-00086-y>
- Brunato M, Battiti R, 2005. Statistical learning theory for location fingerprinting in wireless LANs. *Comput Netw*, 47(6):825-845. <https://doi.org/10.1016/j.comnet.2004.09.004>
- Cha J, Lim E, 2022. A hierarchical auxiliary deep neural network architecture for large-scale indoor localization based on WiFi fingerprinting. *Appl Soft Comput*, 120:108624. <https://doi.org/10.1016/j.asoc.2022.108624>
- Chen GK, Guo XY, Liu K, et al., 2022. RWKNN: a modified WKNN algorithm specific for the indoor localization problem. *IEEE Sens J*, 22(7):7258-7266. <https://doi.org/10.1109/JSEN.2022.3155902>
- Chon HD, Jun S, Jung H, et al., 2004. Using RFID for accurate positioning. *J Glob Posit Syst*, 3(1):32-39. <https://doi.org/10.5081/jgps.3.1.32>
- Ciurana M, Cugno S, Barcelo-Arroyo F, 2007. WLAN indoor positioning based on TOA with two reference points. Proc 4<sup>th</sup> Workshop on Positioning, Navigation and Communication, p.23-28. <https://doi.org/10.1109/WPNC.2007.353607>
- Costa JA, Patwari N, Hero AOIII, 2006. Distributed weighted-multidimensional scaling for node localization in sensor networks. *ACM Trans Sens Netw*, 2(1):39-64. <https://doi.org/10.1145/1138127.1138129>
- Dag T, Arsan T, 2018. Received signal strength based least squares lateration algorithm for indoor localization. *Comput Electr Eng*, 66:114-126. <https://doi.org/10.1016/j.compeleceng.2017.08.014>
- Dong YH, Arslan T, Yang YJ, 2022. An encoded LSTM network model for WiFi-based indoor positioning. Proc IEEE 12<sup>th</sup> Int Conf on Indoor Positioning and Indoor Navigation, p.1-6. <https://doi.org/10.1109/IPIN54987.2022.9918116>
- Dong ZY, Xu WM, Zhuang H, 2019. Research on ZigBee indoor technology positioning based on RSSI. *Proc Comput Sci*, 154:424-429. <https://doi.org/10.1016/j.procs.2019.06.060>
- Gu YY, Lo A, Niemegeers I, 2009. A survey of indoor positioning systems for wireless personal networks. *IEEE Commun Surv Tut*, 11(1):13-32. <https://doi.org/10.1109/SURV.2009.090103>
- He SN, Chan SHG, 2016. WiFi fingerprint-based indoor positioning: recent advances and comparisons. *IEEE Commun Surv Tut*, 18(1):466-490. <https://doi.org/10.1109/COMST.2015.2464084>
- Hegarty CJ, Chatre E, 2008. Evolution of the Global Navigation Satellite System (GNSS). *Proc IEEE*, 96(12):1902-1917. <https://doi.org/10.1109/JPROC.2008.2006090>
- Hoang MT, Zhu YZ, Yuen B, et al., 2018. A soft range limited  $K$ -nearest neighbor algorithm for indoor localization enhancement. *IEEE Sens J*, 18(24):10208-10216. <https://doi.org/10.1109/JSEN.2018.2874453>
- Hu JS, Liu HL, Liu DW, 2018. Toward a dynamic  $K$  in  $K$ -nearest neighbor fingerprint indoor positioning. Proc IEEE Int Conf on Information Reuse and Integration, p.308-314. <https://doi.org/10.1109/IRI.2018.00054>
- Hu JS, Liu Dw, Yan Z, et al., 2019. Experimental analysis on weight  $K$ -nearest neighbor indoor fingerprint positioning. *IEEE Int Things J*, 6(1):891-897. <https://doi.org/10.1109/JIOT.2018.2864607>
- Hu XK, Shang JG, Gu FQ, et al., 2015. Improving WiFi indoor positioning via AP sets similarity and semi-supervised affinity propagation clustering. *Int J Distrib Sens Netw*, 11:109642. <https://doi.org/10.1155/2015/109642>
- Jin RC, Xu H, Che ZP, et al., 2015. Experimental evaluation of reducing ranging-error based on receive signal strength indication in wireless sensor networks. *IET Wirel Sens Syst*, 5(5):228-234. <https://doi.org/10.1049/iet-wss.2013.0139>
- Latif E, Parasuraman R, 2022. Online indoor localization using DOA of wireless signals. <https://arxiv.org/abs/2201.05105>
- Le YF, Zhang HN, Shi WB, et al., 2021. Received signal strength based indoor positioning algorithm using advanced clustering and kernel ridge regression. *Front Inform Technol Electron Eng*, 22(6):827-838. <https://doi.org/10.1631/FITEE.2000093>
- Lee I, Kwak M, Han D, 2016. A dynamic  $K$ -nearest neighbor method for WLAN-based positioning systems. *J Comput Inform Syst*, 56(4):295-300. <https://doi.org/10.1080/08874417.2016.1164000>
- Li D, Zhang BX, Li C, 2015. A feature-scaling-based  $K$ -nearest neighbor algorithm for indoor positioning systems. *IEEE Int Things J*, 3(4):590-597. <https://doi.org/10.1109/JIOT.2015.2495229>
- Lin H, Purmehdi H, Fei XN, et al., 2023. Two-stage clustering for improve indoor positioning accuracy. *Autom Constr*, 154:104981. <https://doi.org/10.1016/j.autcon.2023.104981>
- Liu H, Darabi H, Banerjee P, et al., 2007. Survey of wireless indoor positioning techniques and systems. *IEEE Trans Syst Man Cybern Part C (Appl Rev)*, 37(6):1067-1080. <https://doi.org/10.1109/TSMCC.2007.905750>
- Liu S, Jiang YX, Striegel A, 2014. Face-to-face proximity estimation using Bluetooth on smartphones. *IEEE Trans Mob Comput*, 13(4):811-823. <https://doi.org/10.1109/TMC.2013.44>
- Liu SY, de Lacerda R, Fiorina J, 2022. Performance analysis of adaptive  $K$  for weighted  $K$ -nearest neighbor based indoor positioning. Proc IEEE 95<sup>th</sup> Vehicular Technology Conf, p.1-5. <https://doi.org/10.1109/VTC2022-Spring54318.2022.9860699>
- Lohan ES, Torres-Sospedra J, Richter P, et al., 2017. Crowdsourced WiFi database and benchmark software for indoor positioning. Zenodo Repository. <https://doi.org/10.5281/zenodo.889798>
- Ma J, Li XS, Tao XP, et al., 2008. Cluster filtered KNN: a WLAN-based indoor positioning scheme. Proc Int Symp on a World of Wireless, Mobile and Multimedia Networks, p.1-8. <https://doi.org/10.1109/WOWMOM.2008.4594840>
- Ma R, Guo Q, Hu CZ, et al., 2015. An improved WiFi indoor positioning algorithm by weighted fusion. *Sensors*, 15(9):21824-21843. <https://doi.org/10.3390/s150921824>
- Madigan D, Einahrawy E, Martin RP, et al., 2005. Bayesian indoor positioning systems. Proc IEEE 24<sup>th</sup> Annual Joint Conf of the IEEE Computer and Communications Societies, p.1217-1227. <https://doi.org/10.1109/INFCOM.2005.1498348>

- Nabati M, Ghorashi SA, 2023. A real-time fingerprint-based indoor positioning using deep learning and preceding states. *Expert Syst Appl*, 213:118889. <https://doi.org/10.1016/j.eswa.2022.118889>
- Nguyen SM, Le DV, Havinga PJM, 2023. Learning the world from its words: anchor-agnostic Transformers for fingerprint-based indoor localization. *Proc IEEE Int Conf on Pervasive Computing and Communications*, p.150-159. <https://doi.org/10.1109/PERCOM56429.2023.10099376>
- Nguyen SM, Le DV, Havinga PJM, 2024. Seeing the world from its words: all-embracing Transformers for fingerprint-based indoor localization. *Perv Mob Comput*, 100:101912. <https://doi.org/10.1016/j.pmcj.2024.101912>
- Ni LM, Liu YH, Lau YC, et al., 2003. LANDMARC: indoor location sensing using active RFID. *Proc 1<sup>st</sup> IEEE Int Conf on Pervasive Computing and Communication*, p.407-415. <https://doi.org/10.1109/PERCOM.2003.1192765>
- Oh J, Kim J, 2018. Adaptive  $K$ -nearest neighbour algorithm for WiFi fingerprint positioning. *ICT Expr*, 4(2):91-94. <https://doi.org/10.1016/j.ict.2018.04.004>
- Peng YR, Fan WT, Dong X, et al., 2016. An iterative weighted KNN (IW-KNN) based indoor localization method in Bluetooth low energy (BLE) environment. *Proc Int IEEE Conf on Ubiquitous Intelligence & Computing, Advanced and Trusted Computing, Scalable Computing and Communications, Cloud and Big Data Computing, Internet of People, and Smart World Congress*, p.794-800. <https://doi.org/10.1109/UIC-ATC-ScalCom-CBDCCom-IoP-SmartWorld.2016.0127>
- Pu YC, You PC, 2018. Indoor positioning system based on BLE location fingerprinting with classification approach. *Appl Math Modell*, 62:654-663. <https://doi.org/10.1016/j.apm.2018.06.031>
- Ren QQ, Wang Y, Liu SN, et al., 2023. FSTNet: learning spatial-temporal correlations from fingerprints for indoor positioning. *Ad Hoc Netw*, 149:103244. <https://doi.org/10.1016/j.adhoc.2023.103244>
- Rusli ME, Ali M, Jamil N, et al., 2016. An improved indoor positioning algorithm based on RSSI-trilateration technique for Internet of Things (IoT). *Proc Int Conf on Computer and Communication Engineering*, p.72-77. <https://doi.org/10.1109/ICCCE.2016.28>
- Sadowski S, Spachos P, Plataniotis KN, 2020. Memoryless techniques and wireless technologies for indoor localization with the Internet of Things. *IEEE Int Things J*, 7(11):10996-11005. <https://doi.org/10.1109/JIOT.2020.2992651>
- Salamah AH, Tamazin M, Sharkas MA, et al., 2016. An enhanced WiFi indoor localization system based on machine learning. *Proc Int Conf on Indoor Positioning and Indoor Navigation*, p.1-8. <https://doi.org/10.1109/IPIN.2016.7743586>
- Song XD, Fan XC, Xiang CC, et al., 2019. A novel convolutional neural network based indoor localization framework with WiFi fingerprinting. *IEEE Access*, 7:110698-110709. <https://doi.org/10.1109/ACCESS.2019.2933921>
- Torres-Sospedra J, Montoliu R, Martínez-Usó A, et al., 2014. UJIIndoorLoc: a new multi-building and multi-floor database for WLAN fingerprint-based indoor localization problems. *Proc Int Conf on Indoor Positioning and Indoor Navigation*, p.261-270. <https://doi.org/10.1109/IPIN.2014.7275492>
- Torres-Sospedra J, Montoliu R, Trilles S, et al., 2015. Comprehensive analysis of distance and similarity measures for WiFi fingerprinting indoor positioning systems. *Expert Syst Appl*, 42(23):9263-9278. <https://doi.org/10.1016/j.eswa.2015.08.013>
- Torres-Sospedra J, Montoliu R, Mendoza-Silva GM, et al., 2016. Providing databases for different indoor positioning technologies: pros and cons of magnetic field and WiFi based positioning. *Mob Inform Syst*, 2016(1):6092618. <https://doi.org/10.1155/2016/6092618>
- Umair MY, Ramana KV, Yang DK, 2014. An enhanced  $K$ -nearest neighbor algorithm for indoor positioning systems in a WLAN. *Proc IEEE Computers, Communications and IT Applications Conf*, p.19-23.
- Wu D, Xu YB, Ma L, 2009. Research on RSS based indoor location method. *Proc Pacific-Asia Conf on Knowledge Engineering and Software Engineering*, p.205-208. <https://doi.org/10.1109/KESE.2009.67>
- Xia MZ, Chen JB, Song CL, et al., 2015. The indoor positioning algorithm research based on improved location fingerprinting. *Proc 27<sup>th</sup> Chinese Control and Decision Conf*, p.5736-5739. <https://doi.org/10.1109/CCDC.2015.7161827>
- Xie YQ, Wang Y, Nallanathan A, et al., 2016. An improved  $K$ -nearest-neighbor indoor localization method based on Spearman distance. *IEEE Signal Process Lett*, 23(3):351-355. <https://doi.org/10.1109/LSP.2016.2519607>
- Yang CC, Shao HR, 2015. WiFi-based indoor positioning. *IEEE Commun Mag*, 53(3):150-157. <https://doi.org/10.1109/MCOM.2015.7060497>
- Yu XJ, Li QQ, Queralta JP, et al., 2021. Applications of UWB networks and positioning to autonomous robots and industrial systems. *Proc 10<sup>th</sup> Mediterranean Conf on Embedded Computing*, p.1-6. <https://doi.org/10.1109/MECO52532.2021.9460266>
- Zhang H, Wang ZK, Xia WC, et al., 2022. Weighted adaptive KNN algorithm with historical information fusion for fingerprint positioning. *IEEE Wirel Commun Lett*, 11(5):1002-1006. <https://doi.org/10.1109/LWC.2022.3152610>
- Zhang J, Mao HQ, 2022. WKNN indoor positioning method based on spatial feature partition and basketball motion capture. *Alexandr Eng J*, 61(1):125-134. <https://doi.org/10.1016/j.aej.2021.04.078>
- Zhao YM, Gong W, Li L, et al., 2024. An efficient and robust fingerprint based localization method for multifloor indoor environment. *IEEE Int Things J*, 11(3):3927-3941. <https://doi.org/10.1109/JIOT.2023.3298603>
- Zou H, Jin M, Jiang H, et al., 2017. WinIPS: WiFi-based non-intrusive indoor positioning system with online radio map construction and adaptation. *IEEE Trans Wirel Commun*, 16(12):8118-8130. <https://doi.org/10.1109/TWC.2017.2757472>