



SPJEU: a self-sufficient plaintext-related JPEG image encryption scheme based on a unified key^{*#}

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Abstract: In recent research on image encryption, many schemes associate the key generation mechanism with the plaintext to resist chosen plaintext attacks. However, when the sender encrypts many images, a large amount of additional data related to the plaintext need to be transmitted, which leads to problems such as high transmission costs, high requirements for key storage space, and complex key management. Therefore, in this paper, we propose a self-sufficient plaintext-related JPEG image encryption scheme based on a unified key (SPJEU). This scheme establishes the connection between the plaintext and the key by selecting the direct current (DC) coefficients in the JPEG image through a unified key. Homomorphic encryption is applied to the selected DC coefficients, allowing plaintext information to be decrypted directly from the ciphertext domain using a specific calculation method. The remaining DC coefficients are encrypted through group diffusion, and the alternating current (AC) coefficients are grouped and permuted based on the run length. Extensive experiments show that our scheme can resist chosen plaintext attacks, avoid transmitting plaintext-related additional data in the communication channel, and simplify key management. This scheme also ensures the security and format compatibility of the ciphertext image, and the file increment after encryption is very small.

Key words: Image encryption; Self-sufficient; Plaintext-related; JPEG; Homomorphic encryption

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1 Introduction

Digital images are important multimedia resources on the Internet, and many are posted on network platforms every day. For convenience, users store or share a large amount of online image data to the cloud. To

prevent privacy leakage, the most common solution is image encryption (Li M et al., 2022). However, traditional encryption methods such as advanced encryption standard (AES) and data encryption standard (DES) are not suitable for image encryption because the data contained in the image are redundant and correlated (Liu et al., 2016). Effective image encryption can be performed in either the spatial domain or the frequency domain. Spatial domain encryption involves encrypting the pixels of the image directly. Frequency domain encryption means that the image is transformed from the spatial domain to the frequency domain using transforms such as Fourier, discrete cosine, or wavelet, and the coefficients in the

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frequency domain are encrypted (Refregier and Javidi, 1995).

The main techniques used in both spatial image encryption and frequency image encryption are scrambling and diffusion (Zheng et al., 2017; Yi et al., 2018; Mohammadi et al., 2020; Xian et al., 2022). For example, Yi et al. (2018) and Mohammadi et al. (2020) used a stream cipher to encrypt images by block-based scrambling and pixel-XOR diffusion. Zheng et al. (2017) combined DNA encoding with an XOR operation. Xian et al. (2022) used the spiral-transform-based fractal sorting matrix (STFSM) chaotic system to scramble and diffuse images. At present, the most commonly used image format on the Internet is JPEG, so it is meaningful to encrypt JPEG images (Li WH and Yuan, 2007). Most JPEG encryption algorithms encrypt direct current (DC) and alternating current (AC) coefficients. Li WH and Yuan (2007) and Li SS and Zhang (2016) performed global scrambling of DC coefficients in the frequency domain of images. Qin et al. (2023) proposed an adaptive DC coefficient prediction and partial run/size (RS) pair permutation encryption algorithm, which does not increase the size of the ciphertext image. In the algorithm of Ting et al. (2019), the prediction error of the DC coefficient was encrypted by the group, and the scrambling of the RS pair was used for the AC coefficient. He K et al. (2016) performed modulo-operation encryption only on the DC coefficients and the first 14 AC coefficients sorted by “Zigzag.” Li PY and Lo (2019) changed the size of sub-blocks, performed discrete cosine transformation (DCT) on sub-blocks with a size of 16×16 , and then changed the size of the sub-blocks to 8×8 in the quantization process, followed by global scrambling and DC coefficient XOR between sub-blocks. Ong et al. (2015) performed regional scrambling on DC coefficients and extracted all RS pairs in sub-blocks for global scrambling. Li PY and Lo (2017, 2018) used a new orthogonal transform to replace the discrete cosine transform and achieved a good compression effect. Researchers have also proposed encryption algorithms that are based on the JPEG bitstream in the entropy coding stage. Qian et al. (2014, 2018) encrypted the additional bits of DC and AC coefficients using a stream cipher; then, they performed encryption operations on the quantization table and the DCA (DC appended) bits and performed in-block

scrambling on the RS pairs of the AC coefficients (Qian et al. 2019). He JH et al. (2018, 2019) permuted the DC code with the same sign and scrambled the AC code with the same run length.

The encryption mechanisms proposed by Li WH and Yuan (2007), Li SS and Zhang (2016), Yi et al. (2018), and Mohammadi et al. (2020) are not associated with plaintext, and only the key and ciphertext need to be transmitted during transmission. However, such encryption mechanisms are fragile to chosen plaintext attacks and known plaintext attacks. Qu et al. (2022) pointed out that the encryption methods of Yi et al. (2018) and Mohammadi et al. (2020) could not resist a known plaintext attack and proposed an improved method to generate the key associated with the plaintext by using a hash algorithm. Li PY and Lo (2019) obtained contours of plaintext images (Li WH and Yuan, 2007; Li SS and Zhang, 2016) by chosen plaintext attacks and non-zero count attacks.

Therefore, to improve security, researchers have proposed encryption mechanisms associated with plaintext (Zheng et al., 2017; He JH et al. 2018; Xian et al., 2022; Qin et al., 2023), which use hash algorithms to associate secret keys with the plaintext of the image. Zheng et al. (2017) and Qin et al. (2023) used the SHA-256 hash algorithm, Xian et al. (2022) used the SHA-512 algorithm, and He JH et al. (2018) used the SHA3-512 hash algorithm. However, if someone encrypts and transmits a large number of ciphertext images, there will be many problems. For example, since the key is associated with the plaintext, the additional data related to the plaintext need to be transmitted together with the key and ciphertext image. When multiple ciphertext images are sent to the receiver, the amount of extra data transmitted increases significantly, thereby increasing the transmission cost. Moreover, different ciphertext images must be decrypted using different decryption keys, which consist of the encryption keys and the data related to the plaintext. Managing so many different decryption keys is a huge challenge for the receiver. The receiver must know the one-to-one match between the decryption key and the ciphertext image. If there is a slight error in the correspondence, multiple ciphertext images may not be decrypted. In addition, current JPEG encryption schemes have their own drawbacks. For example, in the schemes proposed by Li WH and Yuan (2007),

Li SS and Zhang (2016), and He K et al. (2016), security was improved, but the file size change rate was increased. In the encryption processes of Ong et al. (2015) and Qin et al. (2023), the DC and AC coefficients in sub-blocks could overflow. Therefore, Qin et al. (2023) embedded these overflow data into the ciphertext image to ensure the compatibility of the encrypted image format. The schemes proposed by Ting et al. (2019) and He JH et al. (2018, 2019) require multiple rounds of encryption to avoid file format incompatibility and ensure image security. If the sender needs to encrypt a large number of images, it will cost a huge amount of time. The XOR operation of the DC coefficient by Li PY and Lo (2019) causes the DC coefficient to overflow, leading to format incompatibility.

To address the shortcomings of the current image encryption mechanisms associated with plaintext, in this paper, we propose a self-sufficient plaintext-related image encryption model based on a unified key (SPEU), in which the required information associated with the plaintext can be extracted from the encrypted image itself by the legal receiver with the secret keys. An illustration of the three types of image encryption schemes mentioned above, i.e., the traditional scheme, the plaintext-related scheme, and SPEU, is provided in the supplementary materials.

Based on SPEU, we propose a self-sufficient plaintext-related JPEG image encryption scheme based on a unified key (SPJEU). In SPJEU, the DC coefficients related to the plaintext are directly selected in the plaintext image through a unified key to generate different key streams for different images, and different encryption effects are achieved for different images. The selected DC coefficients are encrypted by the homomorphic technology, so that the same information associated with the plaintext can be extracted in the ciphertext domain using a specific homomorphic calculation method. Therefore, in the decryption process, the receiver can extract the plaintext information and cooperate with the key to generate different decryption key streams for different images. The remaining DC coefficients are encrypted in groups to decrease the damage to the correlation of the DC coefficients, so the file size change rate is small. The AC coefficients are first grouped according to the run length and then permuted into groups; finally, the sub-blocks except the DC coefficients are globally scrambled. The proposed

encryption mechanism not only has the ability to resist the chosen plaintext attacks but also does not generate additional information associated with the plaintext, which solves the fundamental problems in existing plaintext-related image encryption mechanisms. The transmission cost is greatly reduced, the required key storage space is small, and the unified key is easy to manage. The receiver can obtain the decryption key using the transmitted unified key and the ciphertext image to be decrypted. The relationship between the decryption key and the corresponding ciphertext image is very clear, which ensures the correct decryption of multiple images. Furthermore, compared with current JPEG encryption algorithms, the JPEG encryption scheme proposed here can ensure the security and format compatibility of the image without paying extra overhead and additional costs of multiple rounds of encryption, and the file growth rate is small.

The main contributions of this paper are as follows:

1. We propose SPEU, which overcomes the shortcomings of existing plaintext-related encryption mechanisms. SPEU enables the legal receiver to extract the required plaintext-related information from the encrypted image itself using secret keys.
2. Based on SPEU, we propose SPJEU for widely used JPEG images. This scheme selects DC coefficients related to the plaintext in the plaintext image through a unified key, generating different key streams for different images and achieving more secure encryption effects.
3. We conduct a comprehensive evaluation, which shows that our scheme effectively resists chosen plaintext attacks and avoids transmitting plaintext-related data, thereby reducing transmission costs and minimizing key storage. Additionally, the scheme has passed various security analyses, ensuring the security of the ciphertext image.

2 Basic SPEU

The basic SPEU is shown in Fig. 1. To achieve self-sufficiency and plaintext-relatedness simultaneously, the plaintext-related information must be computed directly from the original image or the encrypted image. Therefore, the image should be divided into a plaintext-related part and a remaining part. The first

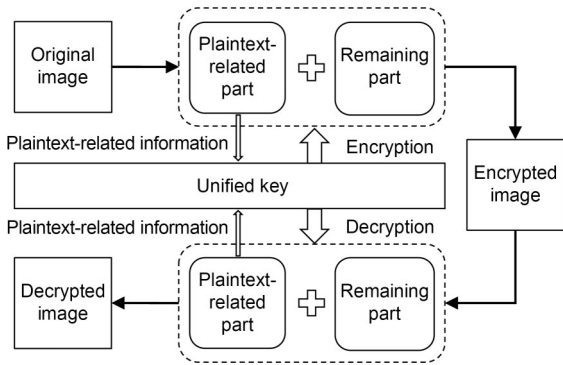


Fig. 1 Illustration of the basic SPEU

part is used for computing the plaintext-related information and is encrypted homomorphically, so that the same information associated with the plaintext can be extracted from the encrypted image. The second part is encrypted by the unified key with the plaintext-related information obtained from the image itself. Although the unified key is consistent, the plaintext-related information is different, and the pseudo-random sequences generated by the unified key and the plaintext-related information for encrypting different images are different, which can resist the chosen plaintext attacks effectively. The plaintext-related part of the image to be encrypted is securely selected by the unified key and can also be

found from the encrypted image in the decryption process according to the secret key. When decryption is performed, the plaintext-related information is first extracted from the plaintext-related part of the encrypted image itself based on homomorphic computing. Then, the pseudo-random sequences used to decrypt the target image can be obtained by combining the unified key and the plaintext-related information, and the decryption can be successful. In SPEU, the plaintext-related information involved in key generation is contained in the plaintext or ciphertext image. During encryption or decryption, any additional plaintext-related information does not need to be transmitted separately since it can be extracted from the image through a unified key. Therefore, this model is “self-sufficient.”

3 Proposed SPJEU

JPEG encoding includes four main steps: block division, DCT, quantization, and entropy encoding (Li PY and Lo, 2020). The encryption process mainly encrypts the quantized coefficients. Fig. 2 describes the entire encryption process of SPJEU. First, the image is subjected to block division, DCT, and quantization

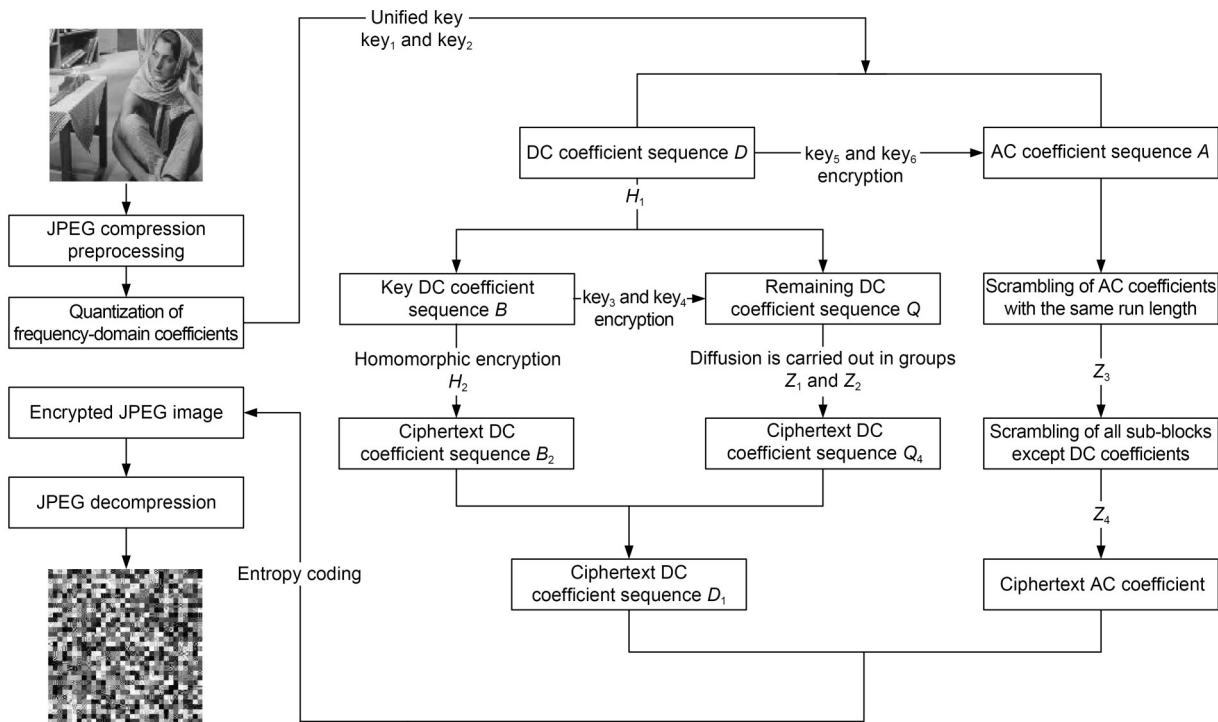


Fig. 2 Flowchart of SPJEU

processing, and then the quantized DC and AC coefficients are encrypted. After encryption, entropy encoding is performed to obtain an encrypted JPEG image. Only the secret keys, including key_1 – key_6 , should be sent to the receiver through a secure channel, which is the same as that in other symmetric encryption schemes. No additional plaintext-related data are required for transmission. Although the secret keys are unified, the generated key streams are different since the encryption is still plaintext-related. The main symbols in the proposed scheme are shown in Table 1.

The range of the quantized DC coefficients is $[\min, \max]$. The values of \max and \min are obtained by Eq. (1):

$$\max = \frac{1023}{\text{Qua}}, \min = \frac{-1024}{\text{Qua}}, \quad (1)$$

where Qua is the value of the DC coefficient in the quantization table; the quantization tables under different quantization factors are different.

The key streams required for encryption of the quantized DC and AC coefficients are different (z_1 and z_2 are used for DC coefficients, and z_3 and z_4 are used for AC coefficients), and the generation of the key streams is related to the plaintext (see details in the supplementary materials).

3.1 Encryption of quantized DC coefficients

The quantized DC coefficient sequence D is divided into two parts: $D = \{B, Q\}$. The number of DC coefficients contained in B is 16, and the number contained in Q is $S_1 = S - 16$. First, the DC coefficient sequence B that constitutes the initial key is encrypted, and then the remaining DC coefficient sequence Q is encrypted. The two encryption methods are different. After encryption, the two parts of the DC coefficients are recombined according to the original position (see details in the supplementary materials).

3.1.1 Encryption of the DC coefficients used for computing the initial key

Since the DC coefficients used for computing the initial key contain coefficients less than 0, to facilitate encryption operations, all the coefficients in B need to be added to $|\min|$ to obtain B_1 , and the range of B_1 is $[0, \max + |\min|]$. In addition, to extract the same plaintext-related information from plaintext and ciphertext, it is necessary to map operations on ciphertext to plaintext, ensuring that the encryption is not affected by information extraction. To solve this problem, it is necessary to consider both the encryption method and information extraction method. This scheme adopts the modulo $(L = \max + |\min| + 1)$ -based homomorphic

Table 1 Definitions of several symbols used to describe our SPJEU

| Symbol | Description |
|--|--|
| M, N | Height and width of the original image |
| $\text{key}_1, \text{key}_2, \text{key}_3, \text{key}_4, \text{key}_5, \text{key}_6$ | Six unified keys |
| z_1, z_2, z_3, z_4 | Pseudo-random sequences generated by different initial values |
| S | Number of 8×8 sub-blocks in the image |
| k_1, k_2 | Pseudo-random sequences generated by key_1 and key_2 |
| H_1, H_2 | Sequences obtained from k_1 and k_2 after processing |
| W | Sequence formed by the first 16 elements of H_1 |
| \min, \max | The minimum and maximum values of the quantized DC coefficients |
| B | Sequence of 16 DC coefficients extracted from sub-blocks based on W |
| L | Parameter used for modulo operations, $L = \max + \min + 1$ |
| A | AC coefficient sequence |
| Q | Sequence of remaining DC coefficients after extracting B |
| Qua | Value of the DC coefficient in the quantization table |
| D | Sequence of all quantized DC coefficients |
| Z_1, Z_2, Z_3, Z_4 | Key stream sequences |
| A_i | Set of AC coefficients with the same run length i |

technique to encrypt the DC coefficients that are used for computing the initial key. The process of the homomorphic encryption algorithm using the generated key stream is as follows: $C = E_n(B_1, H_2) = (B_1 + H_2) \bmod L = (b_i + h_i) \bmod L = c_i, \forall i = 1, 2, \dots, 16$, where b_i, h_i , and c_i represent the DC coefficient of B_1 , the random number in the key stream H_2 , and the ciphertext DC coefficient, respectively. The decryption process is as follows: $D_n(C, H_2) = (c_i - h_i) \bmod L = b_i \bmod L, \forall i = 1, 2, \dots, 16$.

Homomorphic encryption means that the results obtained by data operations in the ciphertext domain and the plaintext domain are consistent; i.e., computing before decryption is equivalent to computing after decryption (Xie et al., 2019).

The homomorphic encryption algorithm based on modulo L can control only the range of the encrypted DC coefficients in $[0, \max + |\min|]$. When subtracting $|\min|$ from the encrypted DC coefficient, the coefficient range is $[\min, \max]$, so the problem of DC coefficient overflow does not occur (see the supplementary materials for homomorphism proof).

After homomorphic encryption, we scramble B_2 using a pseudo-random sequence k derived from a pseudo-random generator, such as those of Haider et al. (2023) and Ramesh and Jain (2015), which are based on $\text{key}_1 + \text{key}_2$ and an initial value Init_x computed by $(\text{initial}_1 + \text{initial}_2) \bmod L$ (Eq. (S5) in the supplementary materials). The scrambling method is similar to that of Qin et al. (2023).

3.1.2 Encryption of the remaining DC coefficients

To prevent the overflow of DC coefficients and avoid increasing the compression rate of ciphertext files, we encrypt the remaining DC coefficients sequence Q in groups. Four consecutive DC coefficients are grouped into one group diffused using the same random number. The specific process is as follows:

Step 1: Perform encryption preprocessing on the remaining DC coefficients, where $Q_1 = Q + |\min|$.

Step 2: Group the remaining DC coefficients; the DC coefficients are grouped into sets of 4, with any remaining coefficients (if < 4) as a final group, yielding $m+n$ groups in total. The DC coefficient sequence after grouping is $Q_2 = \{q_1, q_2, \dots, q_{m+n}\}$, where $q_i = \{a_1, a_2, a_3, a_4\}$. a_i refers to the remaining DC coefficients, and fix refers to the quotient function.

$$m = \text{fix}\left(\frac{S - 16}{4}\right), n = (S - 16) \bmod 4. \quad (2)$$

Step 3: Perform Eqs. (3) and (4) on the pseudo-random sequences z_1 and z_2 to obtain key stream sequences Z_1 and Z_2 .

$$Z_1 = ((z_1 + z_2) \times 10^{13}) \bmod L, \quad (3)$$

$$Z_2 = Z_1(1:(m+n)). \quad (4)$$

Step 4: Diffusion is performed in units of groups, and Eq. (5) is performed on Q_2 to obtain the encrypted result Q_3 after diffusion.

$$Q_3(i) = (Q_2(i) + Z_2(i)) \bmod L, i = 1, 2, \dots, m+n. \quad (5)$$

Step 5: $Q_4 = Q_3 - |\min|$. Q_4 is the sequence of final encrypted residual DC coefficient.

The encrypted DC coefficient sequence B_2 and the encrypted residual DC coefficient sequence Q_4 are recombined according to the original position. Finally, the sequence of all encrypted DC coefficients is $D_1 = \{B_2, Q_4\}$.

3.2 Encryption of AC coefficients

We adopt two encryption methods for the AC coefficients, namely, scrambling the AC coefficients of the same run length and globally scrambling the sub-blocks except for the DC coefficients. The AC coefficient coding is determined by the run length and value. By scrambling only the AC coefficients with the same run length and the sub-blocks except the DC coefficients, the amount of compression of the ciphertext image does not change (see details in the supplementary materials).

3.2.1 Globally scrambling AC coefficients with the same run length

Step 1: First, the coefficients in all sub-blocks in the DCT image are sorted by Zigzag scan, and then the AC coefficients are grouped according to their run lengths, where A_i is the set of AC coefficients whose run length is i . The frequency of the run length of different images is different, and not all run lengths will appear, so $i \in \{0, 1, 2, \dots, 63\}$, as shown in the supplementary materials.

Step 2: Group the pseudo-random sequence z_3 according to the number of AC coefficients in A_i , where Z_{3i} is the key stream required to scramble A_i .

Step 3: Scramble the AC coefficients of the same run length. Z_{3i} is sorted in ascending order, and the sorted index value is used to scramble the AC coefficient set A_i , whose run length is i . The scrambling method is similar to that of Qin et al. (2023).

Step 4: Reintegrate the scrambled AC coefficients according to the initial positions.

3.2.2 Globally scrambling sub-blocks except for DC coefficients

Step 1: Generate the key stream sequence Z_4 required for scrambling the subblocks, $Z_4=z_4(1:S)$.

Step 2: Sort Z_4 in ascending order and use the sorted index value index_2 to scramble the sub-blocks, except for the DC coefficients.

3.3 Decryption process

Decryption is the reverse process of encryption (the flowchart of decryption is provided in the supplementary materials). The specific process is as follows:

Step 1: Entropy decoding is performed on the ciphertext JPEG image to obtain the ciphertext image in the frequency domain. The DC coefficient sequence B_2 , which is used to compute the initial key, is then extracted by H_1 generated by key_1 .

Step 2: According to homomorphism, Initx can be extracted from the ciphertext by performing $\text{sum}(B_2(1:16)) \bmod L$. Initx can be extracted because the following equation is always established regardless of whether B_2 is permuted or not: $\text{sum}(B_2(1:16)) \bmod L = ((B_2(1:8)) \bmod L + (B_2(9:16)) \bmod L) \bmod L$. According to Section 3.1.1 (main text) and Section 2 (supplementary materials), we have $\text{sum}(B_2(1:16)) \bmod L = (\text{initial}_1 + \text{initial}_2) \bmod L = \text{Initx}$. Then, generate the pseudo-random sequence k using the pseudo-random generator based on $\text{key}_1 + \text{key}_2$ and the initial value Initx , and perform inverse scrambling operations on B_2 according to k to restore scrambling.

Step 3: Perform homomorphic computation on the restored B_2 to obtain the plaintext-related information initial_1 and initial_2 , and combine them with key_3 and key_4 to generate key stream sequences Z_1 and Z_2 . Group the remaining encrypted DC coefficients sequence Q_4 , and then perform inverse diffusion

according to the key stream to obtain the decrypted remaining DC coefficient sequence Q .

Step 4: B_2 is decrypted using H_2 generated by key_2 . Recombine the decrypted DC coefficient sequence B and the remaining DC coefficient sequence Q to obtain all the DC coefficients sequence D . Combining the DC coefficient sequence D and keys key_5 and key_6 generates key stream sequences Z_3 and Z_4 . All sub-blocks except the DC coefficients in the frequency-domain image are inversely scrambled according to the key stream sequence Z_4 . The AC coefficients of the same run length are inversely scrambled according to the key stream sequence Z_3 .

Step 5: Inverse quantization, inverse DCT, and sub-block merging are performed on the decrypted DCT image to obtain the plaintext.

4 Experimental results and security analysis

We took the grayscale images “Cameraman,” “Pepper,” “Barbara,” and “Booby” and the color image “Squirrel” with a size of 256×256 as examples. Besides these five commonly used images, we tested the first 1000 512×512 images selected from the BOWS2 database. All algorithms were implemented by MATLAB R2020b. The computer had an Intel® Core™ i7-8700 @ 3.20 GHz CPU, 8 GB memory, and Microsoft Windows 10. Images with a quality factor of 85 were used to compare the performances of different schemes. We evaluated the proposed SPJEU in terms of image quality, JPEG format compatibility, file size change rate, and security analysis to verify the effectiveness, algorithm efficiency, additional data transmission and key storage space, and superiority of the scheme. Note that our encryption scheme is also suitable for grayscale images and color images of different sizes since the color channels can be processed individually in the same manner as the grayscale images. Users can choose the number of DC coefficients as the initial key according to the size of the image and their own needs.

4.1 Visual perception and image quality

In this subsection, we describe the evaluation of the visual perception and quality of the encrypted images. First, the five test images were encrypted and

decrypted, and the results are shown in Fig. 3. There was no observable connection between the encrypted images and the original images, indicating that our encryption scheme is visually secure. Additionally, we measured the quality of the encrypted images using mean square error (MSE), peak signal-to-noise ratio (PSNR), and structural similarity index measure (SSIM) (Murillo-Escobar et al., 2019) to verify the effectiveness and security of the encryption scheme. The measured data are shown in Table 2. The quality factor was set to 85.

4.2 JPEG format compatibility

The quantized DC coefficients of JPEG images have a fixed range, and these ranges vary under different quantization factors. Section 3.1 shows that the range of the quantized DC coefficients is $[\min, \max]$. If the encrypted DC coefficient exceeds this range, the DC coefficient overflows, causing the JPEG format to be incompatible and impacting the visual effect of the image. For example, the scheme proposed by Ong et al. (2015) adopted the RS pair scrambling method, which could result in more than 63 AC coefficients in the sub-blocks of a JPEG image, making the image format incompatible with JPEG. In our scheme, the encryption method of the DC coefficients is based on modulo L . This method fixes the range of the DC coefficients at $[\min, \max]$, ensuring that the value of the encrypted DC coefficients will not overflow. The

encryption of the AC coefficients adopts two scrambling methods: one for AC coefficients with the same run length and another for all the sub-blocks except the DC coefficients in the JPEG image. Neither method will cause the number of AC coefficients in a sub-block to exceed 63. Therefore, SPJEU has good compatibility with the JPEG format.

When designing a JPEG encryption scheme, the file size change rate of the encrypted JPEG image should be considered. Table 3 shows the file size change rate after encryption of different JPEG images under different quality factors (including 50, 60, 70, 80, and 85). The JPEG encryption scheme we designed slightly increases the file size while ensuring security. However, under different quality factors, the file size change rate is controlled at 2%, which is negligible relative to the original data volume of the ciphertext.

We conducted comparative experiments with other algorithms in terms of the file size change rate, which is computed by dividing the original file size by the difference between the encrypted file size and the original file size (Table 4). The experimental result represents the average value obtained from tests on the BOWS2 database. Relative to the schemes of Ong et al. (2015), Li PY and Lo (2017, 2018), and Yuan et al. (2024), our file size change rate is small. Compared with Qin et al. (2023), Qian et al. (2014), He JH et al. (2018), and Hua et al. (2023), our file size change rate is slightly large. However, the method of Hua

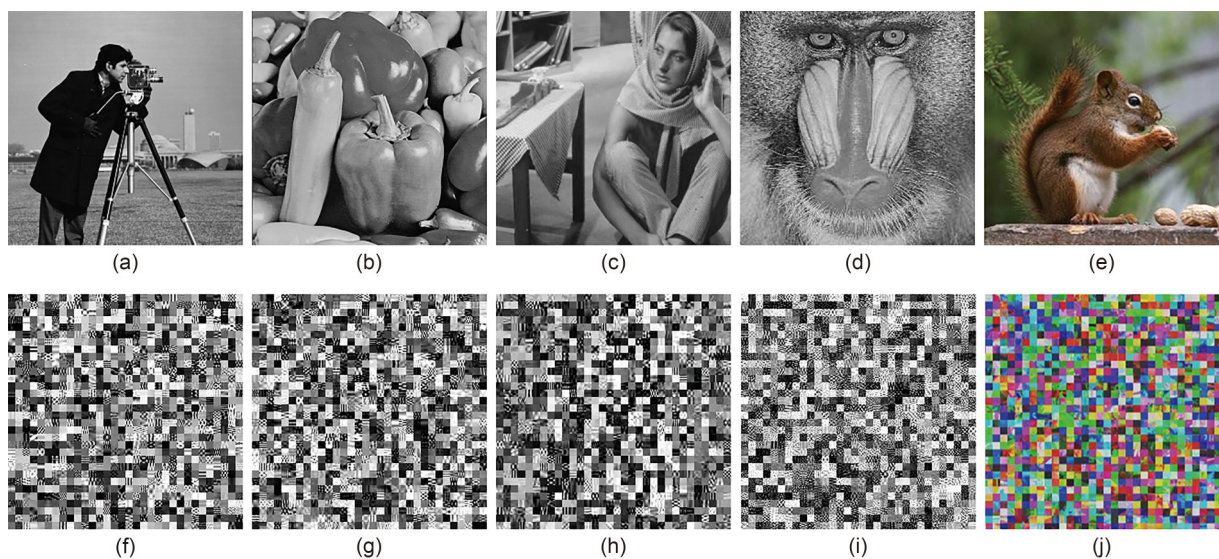


Fig. 3 Encryption results: (a) and (f) Cameraman; (b) and (g) Pepper; (c) and (h) Barbara; (d) and (i) Baboon; (e) and (j) Squirrel. (a)–(e) are the original images, and (f)–(j) are the encrypted images

Table 2 Image quality

| Image | SSIM | PSNR (dB) | MSE |
|-----------|--------|-----------|--------|
| Cameraman | 0.0009 | 7.99 | 10 308 |
| Pepper | 0.0012 | 8.82 | 8536 |
| Barbara | 0.0003 | 8.35 | 9590 |
| Baboon | 0.0008 | 9.05 | 8078 |
| Squirrel | 0.0013 | 9.02 | 9235 |

Table 3 File size change rate under different quality factors

| Image | File size change rate (%) | | | | |
|-----------|---------------------------|-------|-------|-------|-------|
| | Quality factor=50 | 60 | 70 | 80 | 85 |
| Cameraman | 1.101 | 1.062 | 1.239 | 1.091 | 0.897 |
| Pepper | 1.161 | 1.045 | 0.966 | 0.826 | 0.679 |
| Barbara | 0.813 | 0.665 | 0.746 | 0.603 | 0.546 |
| Baboon | 0.582 | 0.610 | 0.568 | 1.486 | 0.409 |
| Squirrel | 1.202 | 1.068 | 0.985 | 0.793 | 0.682 |

Table 4 File size change rate compared to other schemes

| Scheme | File size change rate (%) |
|---------------------|---------------------------|
| Ours | 0.624 |
| Li PY and Lo (2018) | 3.752 |
| He JH et al. (2018) | 0.093 |
| Li PY and Lo (2017) | 7.208 |
| Ong et al. (2015)+ | 1.632 |
| Ong et al. (2015)- | 1.381 |
| Qian et al. (2014) | 0.098 |
| Qin et al. (2023) | -1.321 |
| Hua et al. (2023) | 0.076 |
| Yuan et al. (2024) | 1.149 |

“+” means non-optimized and “-” means optimized

et al. (2023) has a change rate close to 0 because the file size change rate stems only from byte padding. The schemes of Qian et al. (2014) and He JH et al. (2018) have lower change rates because they are based on bitstream encryption, and few elements in a JPEG bitstream can be used for encryption, so the encryption effect is not good enough. The scheme of He JH et al. (2018) needs to iterate approximately 15 times to encrypt the DC algorithm to ensure image security, and the calculation cost is high. The encryption algorithm of Qin et al. (2023), which has a negative file size change rate (the encrypted file size is smaller than

the original file size), may lead to overflow of DC and AC coefficients, and it is necessary to embed the overflowed data into the ciphertext image to ensure the compatibility of the file format. Therefore, in view of its superiority in terms of self-sufficiency and plaintext relation, the file size change rate of our scheme is still satisfactory. Compared with other encryption algorithms, we can ensure the security, efficiency, and format compatibility of the encryption simultaneously without paying extra costs.

4.3 Security analysis

In addition to the security proof of SPJEU (see details in the supplementary materials), we evaluated the security of SPJEU from several aspects, including key sensitivity analysis, outline attacks, histogram analysis, differential cryptanalysis, and information entropy.

4.3.1 Key sensitivity analysis

If the key changes slightly, the ciphertext image cannot be decrypted at all, indicating that the algorithm is very sensitive to the key. We used key_1 and key_2 to encrypt the Barbara image, where $key_2=key_1+10^{-14}$. The results (Fig. 4) show that our algorithm is very sensitive to the keys.

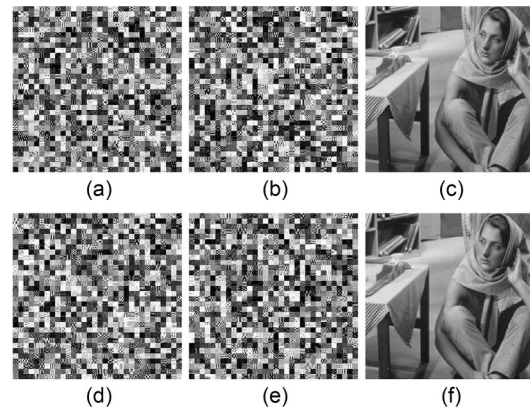


Fig. 4 Evaluation of key sensitivity: (a) encrypted Barbara with key_1 ; (b) decrypted (a) with key_2 ; (c) decrypted (a) with key_1 ; (d) encrypted Barbara with key_2 ; (e) decrypted (d) with key_1 ; (f) decrypted (d) with key_2

4.3.2 Outline attacks

Fig. 5 shows the results obtained after the non-zero coefficient count (NCC), energy of AC coefficients (EAC), and position of last nonzero coefficients (PLZ) (Minemura et al., 2012) attacks are performed

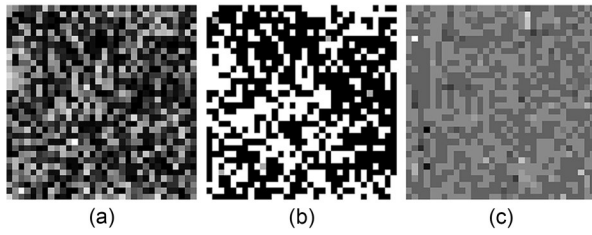


Fig. 5 Results obtained by attacking ciphertext images using outline attacks: (a) NCC; (b) EAC; (c) PLZ

on the ciphertext image of “Barbara.” Clearly, the outline of the plaintext image cannot be identified, indicating that our proposed SPJEU can effectively resist these outline attacks and ensure the security of the encryption algorithm.

4.3.3 Histogram analysis

Fig. 6 shows the histograms of the original images of “Cameraman,” “Pepper,” “Barbara,” “Baboon,” and “Squirrel” with a size of 256×256 and their corresponding ciphertext images. Compared with the histograms of ordinary images, the ciphertext has a uniform pixel distribution, which means that our scheme is resistant to statistical attacks. The histogram bins at 0 and 255 in Fig. 6 are significantly higher because of the encryption of the AC and DC coefficients, which makes it difficult to judge the range of the encrypted pixel values. We control values greater than 255 and values less than 0 to 0, but the pixel values in $[0, 255]$ are still uniformly distributed, indicating that our proposed SPJEU can effectively resist histogram analysis.

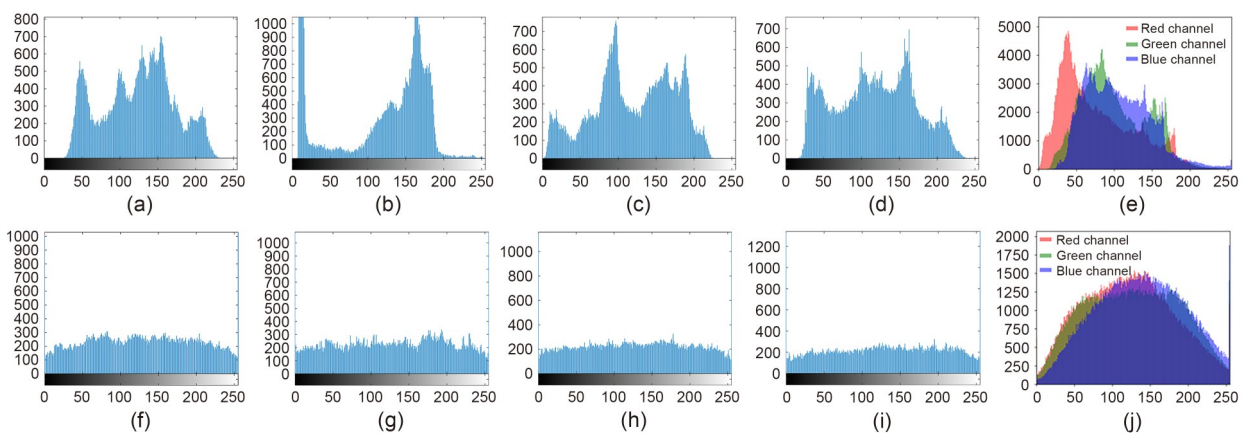


Fig. 6 Histogram analysis: (a) and (f) Cameraman; (b) and (g) Pepper; (c) and (h) Barbara; (d) and (i) Baboon; (e) and (j) Squirrel. (a)–(e) represent histograms of the original images, and (f)–(j) represent histograms of the corresponding encrypted images. The horizontal and vertical axes denote the pixel value and the number of pixels, respectively. References to color refer to the online version of this figure

4.3.4 Differential cryptanalysis

Differential attack is an important analysis method to test the sensitivity of an algorithm to plaintext, which can be measured by the number of pixel change rate (NPCR) and the unified average change intensity (UACI) (Toughi et al., 2017). A higher NPCR/UACI represents better resistance to differential attacks. Theoretically, the values of NPCR and UACI should be close to 99.61% and 33.46%, respectively (Zhang et al., 2020). Table 5 shows NPCR and UACI values of five images with a quality factor of 85. Our encryption scheme achieves NPCR values ranging from 99.31% to 99.62% and UACI values from 32.90% to 34.75% for the five test images. These values are close to the theoretical expectations, indicating strong resistance to differential attacks.

In addition, we conducted a comparative analysis of the NPCR and UACI values of our proposed scheme and several other algorithms. The data presented in Table 6 represent the average NPCR and UACI values calculated for each scheme based on the BOWS2 database. Table 6 shows that our scheme achieves an NPCR of 99.63% and a UACI of 35.68%, which is competitive with those of the other schemes. In some cases, it is even superior to other schemes. For instance, while the scheme of Li PY and Lo (2018) has a lower NPCR of 96.12%, it exhibits a higher UACI of 38.34%. Conversely, the scheme of He JH et al. (2018) achieves an NPCR of 99.37% but a lower UACI of 25.76%. The NPCR and UACI values of Li PY and Lo (2017) are not ideal because their DC coefficients

Table 5 Values of NPCR and UACI of different images

| Image | NPCR (%) | UACI (%) |
|-----------|----------|----------|
| Cameraman | 99.48 | 33.62 |
| Pepper | 99.41 | 34.27 |
| Barbara | 99.31 | 34.75 |
| Baboon | 99.57 | 32.91 |
| Squirrel | 99.62 | 32.90 |

Table 6 Comparison of NPCR and UACI values

| Scheme | NPCR (%) | UACI (%) |
|---------------------|----------|----------|
| Ours | 99.63 | 35.68 |
| Li PY and Lo (2018) | 96.12 | 38.34 |
| He JH et al. (2018) | 99.37 | 25.76 |
| Li PY and Lo (2017) | 99.38 | 21.49 |
| Qin et al. (2023) | 99.48 | 35.26 |
| Hua et al. (2023) | 99.36 | 26.21 |
| Yuan et al. (2024) | 99.68 | 33.35 |

overflow, causing pixels to exceed this range. The UACI value of Hua et al. (2023) is lower because their encryption is restricted. The indicators of the schemes of Yuan et al. (2024) and Qin et al. (2023) are more ideal and have higher security in terms of differential attack. Our scheme strikes a balance, providing robust differential attack resistance with NPCR and UACI values close to the theoretical optimum. The comparison indicates that our approach offers effective security measures while maintaining performance, as evidenced by a consistently high NPCR and appropriate UACI values across different scenarios.

4.3.5 Information entropy

Information entropy can be used to measure the random distribution of gray values of ciphertext images. Table 7 lists the entropy values of the test images, where the quality factor is 85, and the calculated results are close to the ideal value of 8.

Additionally, we tested the average information entropy of encrypted images from the BOWS2 database using our encryption algorithm and other algorithms, with the quality factor set to 85. Table 8 presents a comparison with the results of other algorithms. The results from Tables 7 and 8 demonstrate that our encryption algorithm achieves high information entropy, close to the ideal value, indicating strong resistance to statistical attacks. Our scheme's average information

Table 7 Information entropy of different images

| Image | Plaintext entropy | Ciphertext entropy |
|-----------|-------------------|--------------------|
| Cameraman | 7.21 | 7.80 |
| Pepper | 7.42 | 7.79 |
| Barbara | 7.56 | 7.78 |
| Baboon | 7.33 | 7.79 |
| Squirrel | 7.86 | 7.63 |

Table 8 Comparison of average information entropy among different schemes

| Scheme | Average information entropy |
|---------------------|-----------------------------|
| Ours | 7.82 |
| Li PY and Lo (2018) | 7.31 |
| He JH et al. (2018) | 7.79 |
| Li PY and Lo (2017) | 7.61 |
| Qin et al. (2023) | 7.85 |
| Hua et al. (2023) | 7.56 |
| Yuan et al. (2024) | 7.78 |

entropy is 7.82, which is competitive with those of the other schemes. These comparisons confirm that our algorithm provides robust encryption, ensuring high randomness and security in ciphertext images.

4.4 Algorithm efficiency

Apart from security performance, encryption efficiency is important, especially in practical applications. The time complexity of the encryption algorithm is a crucial metric for evaluating its practicality. In our proposed encryption algorithm for an MN grayscale image, the time complexities for different operations are as follows: The time complexity is $O(MN)$ for the block operation, $O(MN \log(MN))$ for the DCT, and $O(MN)$ for the quantization operation. The time complexity is $O(S)$ for generating key streams to encrypt the quantized DC coefficients, generating random sequences k_1 and k_2 and processing them to obtain H_1 and H_2 , $O(1)$ for selecting the first 16 elements from H_1 and extracting DC coefficients, and approximately $O(1)$ for generating the initial key. For encrypting the quantized DC coefficients used for computing the initial key, the time complexity is approximately $O(1)$; for the grouped encryption for the remaining DC coefficients, involving preprocessing, grouping, and diffusion, it is $O(MN)$. For the AC coefficients, the time complexity of scrambling the AC coefficients

with the same run length is approximately $O(MN)$; for the global scrambling of sub-blocks excluding the DC coefficients, it is $O(MN)$. Overall, the total time complexity of the entire encryption process is dominated mainly by the image size MN , resulting in approximately $O(MN\log(MN))$. Table 9 compares the encryption runtime of different images with those of other encryption schemes. The encryption speed of our scheme performs well and is sufficient for practical applications.

4.5 Additional data transmission and key storage space

In this subsection, we compare the additional data transmission and key storage space of our scheme with those of other plaintext-related image encryption mechanisms. Additional data are plaintext-related information that needs to be transmitted in the public channel for image transmission. The key storage space is the space required to store decryption key data, including the secret key and additional data to be calculated using the key.

In most of the existing plaintext-related image encryption schemes, the additional data and the key storage space increase significantly with increasing number of images. This is because the plaintext-related information is separate from the image and should be transmitted alone in the communication channel. However, our proposed scheme fundamentally solves the problem of excessive plaintext-related data generation when encrypting massive images in existing plaintext-related image encryption systems. In our model, plaintext-related information exists in the carrier image and can be extracted securely for decryption by legal users who have secret keys. Therefore, for

both a single image and a large number of images, our scheme maintains consistent and efficient performance in terms of additional data transmission and key storage space (Table 10). Our scheme has superior performance when the number of images is large.

4.6 Comprehensive comparison of performance with other schemes

To compare existing JPEG encryption schemes with our scheme comprehensively, we summarize the characteristics of each scheme, including file size preservation, format compatibility, encryption runtime, security, whether it is related to plaintext, and whether it requires additional transmission and extra cost. Table 11 shows that our algorithm is good enough based on its performance across a range of characteristics.

In Table 11, the extra transmission refers to the schemes of Qin et al. (2023) and He JH et al. (2018), in which the hash value associated with the plaintext needs to be transmitted. The extra cost refers to the extra cost incurred to maintain the size, format compatibility, and security of the ciphertext file. The scheme of Qin et al. (2023) needs to embed the overflowed data into the ciphertext, and that of He JH et al. (2018) needs at least 15 iterations to guarantee visual security.

5 Conclusions

In this paper, we propose SPJEU to solve the problems of additional transmission of information related to the plaintext and difficult management of a large number of different decryption keys in traditional plaintext-related image mechanisms. Our proposed scheme first selects the quantized DC coefficients in the DCT image through a unified key and

Table 9 Encryption runtime of different schemes

| Scheme | Encryption runtime (s) | | | | | |
|---------------------|------------------------|-----------|--------|---------|----------|---------|
| | Pepper | Cameraman | Baboon | Barbara | Squirrel | Average |
| Qin et al. (2023) | 3.87 | 3.74 | 4.09 | 3.35 | 4.13 | 3.84 |
| Ong et al. (2015) | 3.67 | 3.85 | 3.98 | 3.24 | 3.86 | 3.72 |
| Li PY and Lo (2018) | 2.08 | 1.93 | 3.18 | 2.86 | 3.21 | 2.65 |
| Li PY and Lo (2017) | 2.98 | 2.86 | 3.24 | 2.74 | 3.32 | 3.03 |
| He JH et al. (2018) | 1.12 | 1.09 | 1.85 | 1.15 | 1.91 | 1.42 |
| Hua et al. (2023) | 0.76 | 0.68 | 1.10 | 0.84 | 1.21 | 0.92 |
| Yuan et al. (2024) | 1.73 | 1.68 | 1.95 | 1.72 | 1.88 | 1.79 |
| Ours | 1.89 | 1.96 | 1.87 | 1.61 | 1.90 | 1.85 |

Table 10 Comparison of additional data transmission and key storage space

| Scheme | Metric | Value | | | | |
|---------------------|-------------------------|-------|------|-------|--------|-----------|
| | | Num=1 | 10 | 100 | 1000 | 10 000 |
| Ours | Secret key (bit) | 48 | 48 | 48 | 48 | 48 |
| | Additional data (bit) | 0 | 0 | 0 | 0 | 0 |
| | Key storage space (bit) | 48 | 48 | 48 | 48 | 48 |
| He JH et al. (2018) | Secret key (bit) | 32 | 32 | 32 | 32 | 32 |
| | Additional data (bit) | 512 | 5120 | 51200 | 512000 | 5 120 000 |
| | Key storage space (bit) | 544 | 5152 | 51232 | 512032 | 5 120 032 |
| Li PY and Lo (2018) | Secret key (bit) | 32 | 32 | 32 | 32 | 32 |
| | Additional data (bit) | 256 | 2560 | 25600 | 256000 | 2 560 000 |
| | Key storage space (bit) | 464 | 2592 | 25632 | 256032 | 2 560 032 |
| Ong et al. (2015) | Secret key (bit) | 40 | 40 | 40 | 40 | 40 |
| | Additional data (bit) | 512 | 5120 | 51200 | 512000 | 5 120 000 |
| | Key storage space (bit) | 552 | 5160 | 51240 | 512040 | 5 120 040 |
| Qin et al. (2023) | Secret key (bit) | 64 | 64 | 64 | 64 | 64 |
| | Additional data (bit) | 256 | 2560 | 25600 | 256000 | 2 560 000 |
| | Key storage space (bit) | 320 | 2624 | 25664 | 256064 | 2 560 064 |

“Num” represents the number of images

Table 11 Comprehensive performance comparison

| Metric | Qin et al. (2023) | Li PY and Lo (2018) | Li PY and Lo (2017) | He JH et al. (2018) | Ong et al. (2015) | Hua et al. (2023) | Yuan et al. (2024) | Ours |
|------------------------|----------------------|------------------------|------------------------|------------------------|----------------------|----------------------|-----------------------|------|
| File size preservation | *** | * | * | *** | ** | *** | ** | ** |
| Format compatibility | ** | *** | ** | *** | | *** | *** | *** |
| Encryption runtime | * | ** | ** | *** | * | *** | *** | ** |
| Security | *** | ** | ** | ** | * | * | *** | *** |
| Related to plaintext | Yes | No | No | Yes | No | No | Yes | Yes |
| Extra transmission | Yes | No | No | Yes | No | No | Yes | No |
| Extra cost | Yes | No | No | Yes | No | No | Yes | No |

* means average performance, ** means better performance, and *** means excellent

then generates a key stream associated with the plaintext according to the selected DC coefficients. Therefore, different images can be encrypted with different key streams, which can resist chosen plaintext attacks effectively. Since only a unified key needs to be sent in the communication channel, the transmission cost is low, and the potential threat of plaintext information leakage is eliminated. Since the relationship between the unified key and the image can be re-established easily for decryption, the receiver needs only to store the unified key, rather than different key information corresponding to different images, and key management is simple. In addition, experiments and analysis

show that SPJEU ensures the security and format compatibility of the ciphertext image and has little effect on the size of the ciphertext file.

To sum up, the main contribution of this paper is the design of a JPEG image encryption algorithm associated with plaintext that fundamentally solves the problem of too much plaintext-related data generated when encrypting massive images using existing plaintext-related image encryption systems. Since it is relatively simple to establish different decryption keys for different images using SPJEU, transmission cost and key storage space can be saved, and decryption is easy. In the future, we aim to design an encryption

algorithm for JPEG images that has little or no effect on the size of the ciphertext file.

Contributors

Ming LI designed the research. Wenwen ZHOU and Mengdie WANG processed the data and drafted the paper. Yushu ZHANG and Yong XIANG helped organize the paper. Ming LI and Wenwen ZHOU revised and finalized the paper.

Conflict of interest

All the authors declare that they have no conflict of interest.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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List of supplementary materials

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